

R761338

AD 758 642

Report 3980

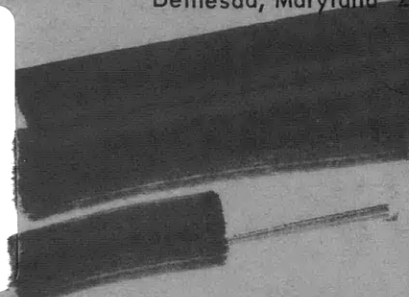


# NAVAL SHIP RESEARCH AND DEVELOPMENT CENTER

Bethesda, Maryland 20034



V393  
.R46



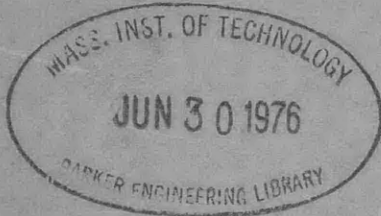
|    |       |  |
|----|-------|--|
| 00 | YNC   |  |
| 01 | SKC   |  |
| 10 | GYSGT |  |
| 11 | YN    |  |
| 12 |       |  |

## THE CONVERGING FACTORS FOR THE SINE AND COSINE INTEGRALS

John W. Wrench, Jr.

and

Vicki Alley



Approved for public release; distribution unlimited.

COMPUTATION AND MATHEMATICS DEPARTMENT  
RESEARCH AND DEVELOPMENT REPORT

September 1972

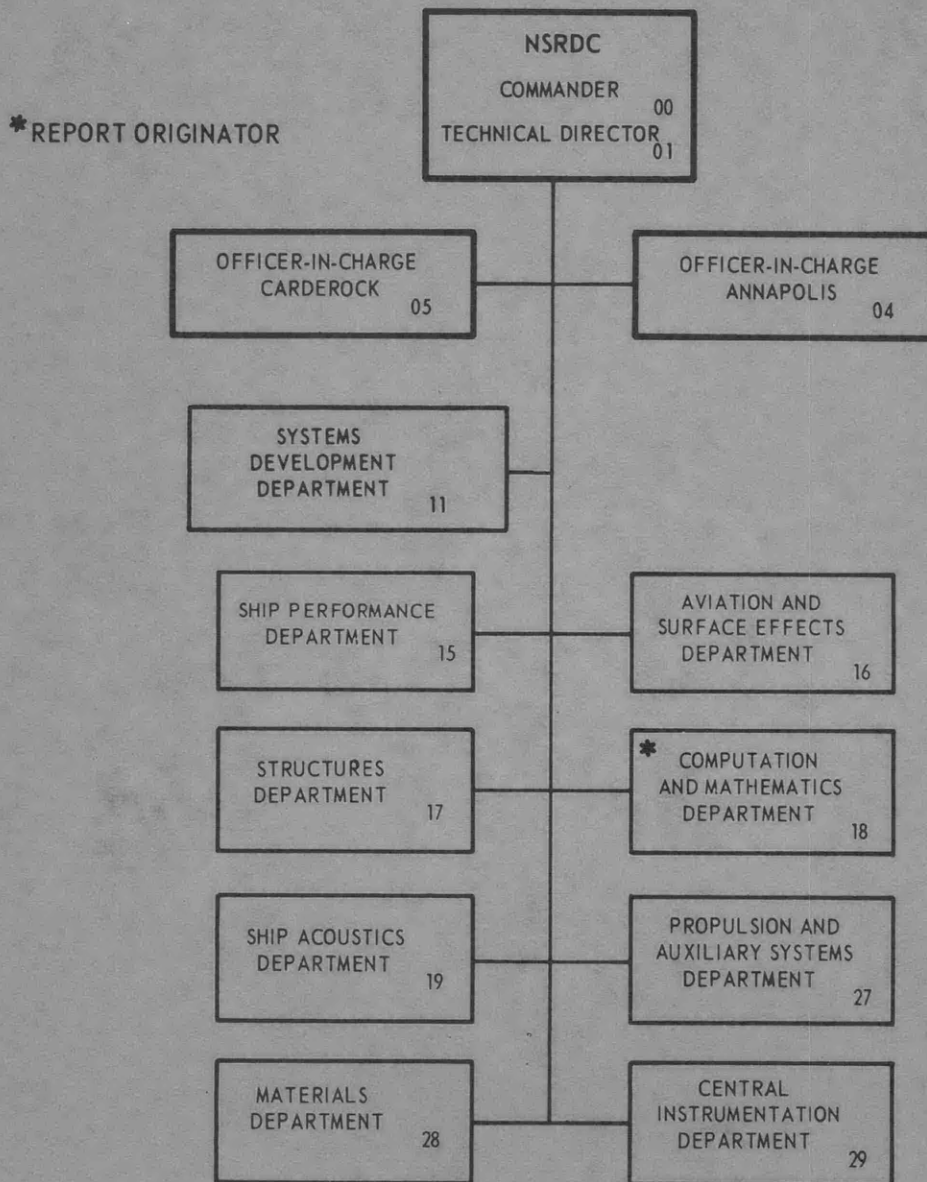
Report 3980

THE CONVERGING FACTORS FOR THE SINE AND COSINE INTEGRALS

The Naval Ship Research and Development Center is a U. S. Navy center for laboratory effort directed at achieving improved sea and air vehicles. It was formed in March 1967 by merging the David Taylor Model Basin at Carderock, Maryland with the Marine Engineering Laboratory at Annapolis, Maryland.

Naval Ship Research and Development Center  
Bethesda, Md. 20034

### MAJOR NSRDC ORGANIZATIONAL COMPONENTS



DEPARTMENT OF THE NAVY  
NAVAL SHIP RESEARCH AND DEVELOPMENT CENTER  
Bethesda, Maryland 20034

THE CONVERGING FACTORS FOR THE  
SINE AND COSINE INTEGRALS

By

John W. Wrench, Jr.

and

Vicki Alley



Approved for public release; distribution unlimited.

September 1972

Report 3980



## TABLE OF CONTENTS

|   | <u>Page</u> |
|---|-------------|
| ABSTRACT.....   | 1           |
| ADMINISTRATIVE INFORMATION.....   | 1           |
| INTRODUCTION .....  | 2           |
| THE SINE AND COSINE INTEGRALS.....  | 3           |
| THE ASYMPTOTIC SERIES FOR THE SINE AND<br>COSINE INTEGRALS AND THEIR CONVERGING<br>FACTORS..... | 4           |
| CALCULATION OF THE CONVERGING FACTORS AND<br>THEIR DERIVATIVES .....                            | 10          |
| APPLICATIONS.....   | 14          |
| ACKNOWLEDGMENTS.....  | 18          |
| APPENDIX A - Values of $\Pi_s(s)$ and of its Reduced<br>Derivatives.....                        | 19          |
| APPENDIX B - Values of $\Pi_{s+1}(s)$ .....   | 89          |
| APPENDIX C - Values of $\Omega_s(s)$ and of $\Omega_{s+1}(s)$ .....                             | 91          |
| APPENDIX D - Values of the Sine and Cosine Integrals .....                                      | 94          |
| REFERENCES.....   | 98          |



LIST OF TABLES

|   | <u>Page</u> |
|---|-------------|
| Table 1 - Coefficients in the asymptotic series   |             |
| $2 \Pi_s(s) \sim 1 + \frac{a_1}{2s} + \frac{a_2}{(2s)^2} + \dots + \frac{a_k}{(2s)^k} + \dots$    | 8           |
| Table 2 - Coefficients in the asymptotic series   |             |
| $2 \Omega_s(s) \sim 1 + \frac{b_1}{2s} + \frac{b_2}{(2s)^2} + \dots + \frac{b_k}{(2s)^k} + \dots$ | 9           |
| Table 3 - Table of $\Pi_s(s)$ and its reduced derivatives $D_i$<br>to 35 D for $s = 2(1)70$       | 20          |
| Table 4 - $\Pi_{s+1}(s)$ to 33 decimal places for $s = 1(1)70$                                    | 90          |
| Table 5 - $\Omega_s(s)$ to 33 decimal places for $s = 1(1)70$                                     | 92          |
| Table 6 - $\Omega_{s+1}(s)$ to 33 decimal places for $s = 1(1)70$                                 | 93          |
| Table 7 - $si(x)$ to 33 decimal places for $x = 1(1)70$   | 95          |
| Table 8 - $Si(x)$ to 33 decimal places for $x = 1(1)70$   | 96          |
| Table 9 - $Ci(x)$ to 33 decimal places for $x = 1(1)70$   | 97          |





## ABSTRACT

The theory of the converging factors for the sine and cosine integrals is developed and then applied to the calculation on a CDC 6700 system of tables of these factors and their reduced derivatives to about 35 decimal places. The factors are then used in conjunction with appropriately truncated asymptotic series to produce tables of  $si(x)$ ,  $Si(x)$ , and  $Ci(x)$  to 28 decimals by a computer program, for successive integer values of  $x$  ranging from 1 to 70, inclusive. Interpolation in the tables by Taylor series is illustrated by numerical examples, which include a new, extended calculation of the Gibbs constant.

## ADMINISTRATIVE INFORMATION

Work on this research was authorized by the Naval Ship Systems Command under the Mathematical Sciences Program. Necessary funds were allocated under Subproject SR 0140301, Task 15324.

## INTRODUCTION

The sine and cosine integrals are known to be simply related to the exponential integral<sup>1,2</sup>. This fact has motivated this study, which derives from a detailed examination by Murnaghan and Wrench<sup>3</sup> of the converging factor for the exponential integral.

The first tables of numerical values of the sine and cosine integrals appear to be those of Bretschneider<sup>4</sup>, which first appeared in 1843. These consisted of 20-decimal approximations corresponding to the first 10 integer arguments. In 1870 Glaisher<sup>5</sup> published more voluminous tables to 11 and 18 decimal places. The British Association for the Advancement of Science<sup>6</sup> has published such tables to 10 and 11 places. The most extensive tabulation has been that of the National Bureau of Standards<sup>7,8</sup> (1940 and 1942) to 9 and 10 decimals (15 decimals near the extrema), occupying three volumes.

In addition to these tables, a large number of others to less precision (ranging from 3 to 7 decimals) have been published. These are listed (along with those cited) by A. Fletcher<sup>9</sup> and his associates.

In this report methods are developed for the evaluation of the converging factors for the sine and cosine integrals to high precision, and these procedures are exemplified by the calculation of appended tables of these factors and their reduced derivatives to 33 and 35 decimal places. Application of these tables is illustrated by specific examples.

These algorithms have been programmed for the CDC 6700 system and were used to calculate 28-place tables of  $si(x)$ ,  $Si(x)$ , and  $Ci(x)$  for  $x = 1(1)70$ , which are also appended to this report (Tables 7-9).

---

<sup>1</sup> A complete list of references is given on pages 98-99.

## THE SINE AND COSINE INTEGRALS

The sine and cosine integrals are generally defined by the relations

$$\text{Si}(z) = \int_0^z \frac{\sin t}{t} dt , \quad (1)$$

$$\text{Ci}(z) = \int_{\infty}^z \frac{\cos t}{t} dt \quad (|\arg z| < \pi) \quad (2)$$

These integrals possess the power-series developments

$$\text{Si}(z) = z - \frac{z^3}{3 \cdot 3!} + \frac{z^5}{5 \cdot 5!} - \dots , \quad (3)$$

$$\text{Ci}(z) = \gamma + \ln z - \frac{z^2}{2 \cdot 2!} + \frac{z^4}{4 \cdot 4!} - \dots , \quad (4)$$

which are convergent for all values of  $z$  (excluding zero in the second expansion). However, for argument  $z$  of absolute value exceeding 10, say, it is preferable to evaluate these functions by asymptotic series, especially when modified by an appropriate converging factor, which is the subject of this report.

Instead of  $\text{Si}(z)$  we shall here consider the complementary integral

$$\text{si}(z) = \int_{\infty}^z \frac{\sin t}{t} dt = \text{Si}(z) - \frac{\pi}{2} \quad (5)$$

Then, if we use the Euler relations

$$\sin z = \frac{e^{iz} - e^{-iz}}{2i} , \quad (6)$$

$$\cos z = \frac{e^{iz} + e^{-iz}}{2} , \quad (7)$$

we can write

$$\text{si}(z) = \frac{1}{2i} \{ \text{Ei}(iz) - \text{Ei}(-iz) \} = -\text{Im Ei}(-iz) , \quad (8)$$

$$\text{Ci}(z) = \frac{1}{2} \{ \text{Ei}(iz) + \text{Ei}(-iz) \} = \text{Re Ei}(-iz) , \quad (9)$$

where  $\text{Ei}(-z)$  is the exponential integral, defined by

$$\text{Ei}(-z) = \int_{\infty}^z \frac{e^{-t}}{t} dt . \quad (10)$$

### THE ASYMPTOTIC SERIES FOR THE SINE AND COSINE INTEGRALS AND THEIR CONVERGING FACTORS

In a previous report<sup>3</sup> F. D. Murnaghan and the present writer developed the series

$$-\text{Ei}(-z) = \frac{e^{-z}}{z} \left\{ 1 - \frac{1}{z} + \frac{2!}{z^2} - \dots + (-1)^{n-1} \frac{(n-1)!}{z^{n-1}} + (-1)^n \frac{n!}{z^n} \Gamma_n(z) \right\}, \quad (11)$$

where  $\Gamma_n(z)$  is the appropriate converging factor, which is given by the integral

$$\Gamma_n(z) = \frac{1}{n!} \int_0^{\infty} \frac{e^{-u} u^n}{1 + \frac{u}{z}} du, \quad n = 1, 2, 3, \dots , \quad (12)$$

and which satisfies both the recurrence relation

$$\Gamma_n(z) = 1 - \frac{n+1}{z} \Gamma_{n+1}(z) \quad (13)$$

and the differential equation

$$\frac{d}{dz} \Gamma_n(z) = \left( \frac{n+1}{z} + 1 \right) \Gamma_n(z) - 1 . \quad (14)$$

From the asymptotic series for  $Ei(-z)$  we then deduce, upon replacing  $z$  by  $iz$ , the series

$$si(z) = -z^{-1} [C(z) \cos z + D(z) \sin z] , \quad (15)$$

$$Ci(z) = z^{-1} [C(z) \sin z - D(z) \cos z] , \quad (16)$$

where

$$C(z) = 1 - \frac{2!}{z^2} + \frac{4!}{z^4} - \dots + \frac{(-1)^k (2k)!}{z^{2k}} \operatorname{Re} \Gamma_{2k}(-iz) , \quad (17)$$

$$D(z) = \frac{1}{z} - \frac{3!}{z^3} + \frac{5!}{z^5} - \dots + \frac{(-1)^k (2k+1)!}{z^{2k+1}} \operatorname{Re} \Gamma_{2k+1}(-iz) , \quad (18)$$

This is equivalent to the corresponding series given by Dingle<sup>10</sup>.

If we set

$$\Pi_n(z) = \operatorname{Re} \Gamma_n(-iz) \quad (19)$$

and

$$\Omega_n(z) = -\operatorname{Im} \Gamma_n(-iz) , \quad (20)$$

so that  $\Gamma_n(-iz) = \Pi_n(z) - i \Omega_n(z)$ , then we deduce from

Equation (12) the representations

$$\Pi_n(z) = \frac{z^2}{n!} \int_0^\infty \frac{e^{-u} u^n}{u^2 + z^2} du \quad (21)$$

$$\Omega_n(z) = \frac{z}{n!} \int_0^{\infty} \frac{e^{-u} u^{n+1}}{u^2+z^2} du = \frac{n+1}{z} \Pi_{n+1}(z) \quad (22)$$

for the components of  $\Gamma_n(-iz)$  as real improper integrals.

In the previously cited report of Murnaghan and Wrench<sup>3</sup> the following series was developed for  $\Gamma_n(z)$ :

$$\Gamma_n(z) = a_0(\beta) + \sum_{j=1}^{\infty} \frac{a_j(\beta)}{z^j} \quad (23)$$

where  $\beta = 1 - \frac{n+1}{z}$ ,  $a_0(\beta) = \frac{1}{2-\beta}$ ,  $a_j(\beta) = \frac{(1-\beta)P_{j-1}(1-\beta)}{(2-\beta)^{2j+1}}$ . Here

$P_j(v)$  is a polynomial in  $v$  of degree  $j$  which satisfies the recurrence

$$P_{j+1}(v) = \{(j+1)v-(j+2)\} P_j(v) - v(v+1) \frac{d}{dv} P_j(v), \quad (24)$$

and  $P_0(v) = 1$ .

If we replace  $n+1$  by  $s$  and  $z$  by  $-is$ , then Equation (23) becomes

$$\Gamma_{s-1}(-is) = \frac{1}{1+i} + i \sum_{j=1}^{\infty} \frac{P_{j-1}(i)}{(1+i)^{2j+1} (-is)^j} \quad (25)$$

Since  $(1+i)^2 = 2i$  and  $\frac{i}{1+i} = \frac{1}{2}(1+i)$ , we have

$$\Gamma_{s-1}(-is) = \frac{1}{2}(1+i) + \frac{1}{2} \sum_{j=1}^{\infty} \frac{(i+i) P_{j-1}(i)}{(2s)^j} \quad (26)$$

Now, if we set  $n = s-1$  and  $z = -is$  in Equation (13) we obtain

$$\Gamma_s(-is) = -i + i \Gamma_{s-1}(-is) \quad (27)$$

and consequently

$$\Gamma_s(-is) = \frac{1-i}{2} - \frac{1-i}{2} \sum_{j=1}^{\infty} \frac{P_{j-1}(i)}{(2s)^j} . \quad (28)$$

Then if we set  $P_{j-1}(i) = A_{j-1} + i B_{j-1}$  and  $\Gamma_s(-is) = \Pi_s(s) - i \Omega_s(s)$ , we can deduce the expansions

$$\Pi_s(s) = \frac{1}{2} - \frac{1}{2} \sum_{j=1}^{\infty} \frac{A_{j-1} + B_{j-1}}{(2s)^j} , \quad (29)$$

$$\Omega_s(s) = \frac{1}{2} - \frac{1}{2} \sum_{j=1}^{\infty} \frac{A_{j-1} - B_{j-1}}{(2s)^j} . \quad (30)$$

When expanded to ten terms these series are explicitly:

$$\begin{aligned} 2\Pi_s(s) = & 1 - \frac{1}{2s} + \frac{1}{(2s)^2} + \frac{3}{(2s)^3} - \frac{55}{(2s)^4} + \frac{599}{(2s)^5} \\ & - \frac{5823}{(2s)^6} + \frac{49595}{(2s)^7} - \frac{266743}{(2s)^8} - \frac{2679473}{(2s)^9} + \dots , \end{aligned} \quad (31)$$

$$\begin{aligned} 2\Omega_s(s) = & 1 - \frac{1}{2s} + \frac{3}{(2s)^2} - \frac{13}{(2s)^3} + \frac{59}{(2s)^4} + \frac{185}{(2s)^5} \\ & - \frac{1309}{(2s)^6} + \frac{45387}{(2s)^7} - \frac{832613}{(2s)^8} + \frac{12609823}{(2s)^9} + \dots . \end{aligned} \quad (32)$$

The coefficients of the first 60 terms of these series have been calculated on the CDC 6700 system in the Computation and Mathematics Department. These numbers are listed in Tables 1 and 2. Dingle<sup>11</sup> has given the first four terms of the series for  $\Pi_s(s)$ .

Table 1. Coefficients in the Asymptotic Series  $2\Pi_s(s) \sim 1 + \frac{a_1}{2s} + \frac{a_2}{(2s)^2} + \dots + \frac{a_k}{(2s)^k} + \dots$

| $k$ |   |
|-----|---|
| 1   | -1  |
| 2   | 1   |
| 3   | 3   |
| 4   | -55   |
| 5   | 599   |
| 6   | -5823   |
| 7   | 49595   |
| 8   | -2 66743  |
| 9   | -26 79473   |
| 10  | 1414 94849  |
| 11  | -36721 18989  |
| 12  | 7 58170 24777   |
| 13  | -126 64772 40185  |
| 14  | 1299 12747 01953  |
| 15  | 17923 98707 48011   |
| 16  | -17 17911 68578 49399   |
| 17  | 716 59803 98678 89919   |
| 18  | -22863 39467 40671 88479  |
| 19  | 5 76116 40787 21862 80803   |
| 20  | -90 11585 44798 12324 81975   |
| 21  | -1373 12307 50976 19279 53481   |
| 22  | 2 08827 66361 59497 57877 31137   |
| 23  | -121 69178 34705 56823 88291 25605  |
| 24  | 5295 89538 42235 03570 16979 45737  |
| 25  | -1 80060 61784 78714 07644 38106 73233  |
| 26  | 38 70985 50168 53454 95003 48440 97729  |
| 27  | 575 64405 63347 88761 72446 90115 85171   |
| 28  | -1 32841 41270 98610 05858 45187 08904 90743  |
| 29  | 100 59880 30170 79671 32956 30131 03499 51975   |
| 30  | -5583 41244 86055 82565 91489 36677 75596 18047   |
| 31  | 2 40688 17733 73565 56430 16266 63551 20113 85291   |
| 32  | -66 90276 55197 81316 73940 23591 71494 76892 11319   |
| 33  | -873 49040 62898 01147 70021 68810 80337 18961 51201  |
| 34  | 3 08000 42883 70745 45808 33044 38889 13997 13900 48641   |
| 35  | -290 10482 67598 45285 57593 91632 86685 98363 80589 03357  |
| 36  | 19689 33992 82099 13521 69504 34830 04316 43651 44815 14185   |
| 37  | -10 34072 99385 11278 31517 20921 97977 24902 35095 70716 56681   |
| 38  | 356 86003 97030 06463 95679 13958 18354 95970 27925 04263 91617   |
| 39  | 3588 99401 42698 42841 94933 08667 97198 33484 27823 51377 51675  |
| 40  | -20 64813 95753 43537 60156 72538 37790 22993 00971 16709 49585 96343   |
| 41  | 2349 60566 39679 01453 08948 61122 67508 16108 92946 38376 22570 19407  |
| 42  | -1 89473 27778 42918 87985 91212 55888 86504 68617 79745 75943 85298 38271  |
| 43  | 117 91722 63715 57621 15102 32208 14097 06618 23380 34471 85365 60087 25491   |
| 44  | -4907 28266 58743 83887 14849 19447 01286 51575 12453 28196 37606 73405 72663                                       |
| 45  | -29797 28133 29637 10521 39806 95000 06566 15158 20186 13645 48786 56528 43705                                      |
| 46  | 340 64847 73622 23828 31451 06589 35986 33707 83513 35598 02634 32491 29789 79713                                   |
| 47  | -45885 73677 84107 80684 30731 45132 94459 49454 86234 99213 90637 35756 08895 33909                                |
| 48  | 43 05638 64711 71002 77183 42821 19221 44479 49301 90002 02124 26970 21302 56795 62441                              |
| 49  | -3110 91560 27407 29951 86287 82994 84793 07137 69780 55510 09573 06512 50598 50285 99361                           |
| 50  | 1 52730 79571 90567 01688 74512 39868 91212 92923 03511 39709 64279 59443 81626 96170 00961                         |
| 51  | 1 91322 22017 39457 89638 47636 98943 98465 88405 54367 41276 93922 13890 71451 39287 29123                         |
| 52  | -12280 53122 55014 72109 45158 53605 55350 76773 86800 63743 91838 04909 08616 66713 36514 06775                    |
| 53  | 19 29474 74559 70016 33925 96926 65353 85197 52172 92567 25779 87742 11522 07835 74319 54520 39799                  |
| 54  | -2073 66136 07247 90292 32251 73859 65224 47290 80849 25190 33914 10336 57622 79532 48551 99786 54783               |
| 55  | 1 71230 94592 20203 94758 19900 48941 31813 56579 44574 68805 10624 16846 17523 37980 46532 88713 05435             |
| 56  | -97 48060 42776 36270 36599 43865 77461 66159 36041 92477 73953 66847 87021 65290 62340 90075 29500 40183           |
| 57  | 417 49016 24812 41456 47834 59374 16700 43255 46624 92017 90962 54729 97237 17768 25801 10013 43198 48047           |
| 58  | 8 82988 57479 96115 00047 04993 57741 02488 46439 60048 96198 75897 80145 41578 54541 94556 33066 30883 07649       |
| 59  | -1600 75508 90374 34137 17615 59182 55519 41104 42840 07901 60435 37033 65376 52020 88695 73923 34392 07823 04429   |
| 60  | 1 94624 64634 90560 13581 39582 74924 00188 06076 33146 81917 88932 32355 46478 98704 80577 75033 64438 87627 40617 |



Table 2—Coefficients in the asymptotic series  $2\Omega_s(s) \sim 1 + \frac{b_1}{2s} + \frac{b_2}{(2s)^2} + \dots + \frac{b_k}{(2s)^k} + \dots$

| $k$ |   |
|-----|---|
| 1   | -1  |
| 2   | 3   |
| 3   | -13   |
| 4   | 59  |
| 5   | -185  |
| 6   | -1309   |
| 7   | 45387   |
| 8   | -8 32613  |
| 9   | 128 09823   |
| 10  | -1585 44573   |
| 11  | 12292 07011   |
| 12  | 1 50570 55875   |
| 13  | -109 97350 18057  |
| 14  | 3710 31774 22819  |
| 15  | -87331 59462 67205  |
| 16  | 20 35485 18552 11419  |
| 17  | -282 34789 05805 13521  |
| 18  | -3874 95248 92383 40157   |
| 19  | 4 72305 89051 68228 81747   |
| 20  | -235 62407 44709 18718 94981  |
| 21  | 8875 23874 81860 79837 00775  |
| 22  | -2 62358 66661 97428 97245 67069  |
| 23  | 48 57059 91475 85708 18302 43627  |
| 24  | 740 93368 72921 48923 85310 98267   |
| 25  | -1 39099 86832 33864 03020 66299 25377  |
| 26  | 93 03390 26282 18638 75980 16052 16067  |
| 27  | -4801 75759 56348 23548 54556 08635 32349   |
| 28  | 1 77240 28703 25442 25818 19923 05477 53915   |
| 29  | -43 59018 76303 41339 84392 44776 66009 27337   |
| 30  | -615 76092 33188 27345 02887 51595 71341 63741  |
| 31  | 1 74959 86777 99747 31890 62842 65491 97959 54075   |
| 32  | -148 41051 46152 42851 24862 70236 81614 35137 42181  |
| 33  | 9147 50507 70271 89509 45876 26680 58176 20147 76559  |
| 34  | -4 37028 52738 33341 66805 33455 17658 22379 10509 78877  |
| 35  | 135 92842 50114 88023 52209 29284 72900 62988 94235 92627   |
| 36  | 1589 14129 61157 47470 18682 11318 39244 57202 58536 49979  |
| 37  | -7 06297 67842 72401 48588 07380 35804 11391 49380 37207 85145  |
| 38  | 733 41235 57018 54905 83030 13823 21644 95347 20648 81845 36291   |
| 39  | -54421 81228 22082 04076 45680 88650 36250 17577 00924 54428 56693  |
| 40  | 31 20490 47916 37097 64302 19353 83331 57005 71059 23618 93066 54107  |
| 41  | -1186 26960 90930 46670 66941 44871 16369 24714 76743 69220 24778 05857   |
| 42  | -9700 67408 74282 53374 26028 16667 71292 68894 11398 64509 94755 16093   |
| 43  | 75 55624 81596 27088 87348 76333 62307 80466 74007 07305 45567 01151 85571  |
| 44  | -9374 41995 89447 16499 99825 07533 25982 05381 70423 37314 14820 66732 63685                                     |
| 45  | 8 17290 01061 70519 73995 37103 09357 24501 06069 02025 69904 76130 88140 87543                                   |
| 46  | -549 26176 21184 89669 72576 38017 51793 15292 20389 96705 31055 08323 51763 25661                                |
| 47  | 24887 20967 23615 13375 03777 10884 27537 26545 41957 76776 71543 38864 98278 54715                               |
| 48  | 93540 88016 13077 37377 82349 27323 80133 74690 63134 11720 17070 31499 12983 16699                               |
| 49  | -1888 51879 92401 03534 41768 84369 86584 31956 28789 73889 96469 57774 96815 10170 75761                         |
| 50  | 2 71983 02777 46247 19320 84231 18998 35109 57980 66996 84097 73474 91556 67510 12596 82243                       |
| 51  | -273 58437 57929 89528 33305 83746 86076 84141 11205 23363 30723 01135 46334 30226 22748 52973                    |
| 52  | 21188 60204 99088 88703 34338 87272 51841 86990 05167 25652 78299 86749 50279 27210 46854 98939                   |
| 53  | -11 21274 92550 73261 98498 67414 17185 91459 04188 99590 75554 18029 08804 29939 57148 70249 33145               |
| 54  | 18 05532 41839 37968 34242 70004 31365 48344 48871 45469 16522 62362 64747 37709 15150 92563 71171                |
| 55  | 95991 70184 71188 72077 88041 24401 03812 23277 86490 22975 16342 60260 72789 04694 32585 41755 09227             |
| 56  | -182 19241 31412 91972 60607 60673 12843 34147 08145 74273 37312 82273 80902 23331 26893 77107 95707 92283        |
| 57  | 18585 72464 89004 13535 89252 42867 24215 93218 78802 14093 81038 13998 47917 38411 16185 57876 33804 56383       |
| 58  | -18 30997 62388 74849 55533 21168 05025 88471 11338 80884 13762 10740 25401 65085 92098 01757 16985 18956 91453   |
| 59  | 984 60021 05358 29807 32006 24397 02453 78492 47166 61160 28679 14998 42716 89544 12465 76381 25971 14467 94371   |
| 60  | -7249 05537 14774 98649 38846 60138 89944 35077 12688 30741 77085 09661 43777 34047 12143 93197 12535 34266 30725 |

**CALCULATION OF THE CONVERGING FACTORS  
AND THEIR DERIVATIVES**

The recurrence formula for  $\Gamma_n(z)$  implies that

$$\Gamma_n(-ix) = 1 - i \left( \frac{n+1}{x} \right) \Gamma_{n+1}(-ix) \quad (33)$$

from which we infer in particular that

$$\Pi_s(s) = 1 - \left( 1 + \frac{1}{s} \right) \Omega_{s+1}(s) \quad , \quad (34)$$

$$\Omega_s(s) = \left( 1 + \frac{1}{s} \right) \Pi_{s+1}(s) \quad . \quad (35)$$

Clearly, if we can develop a Taylor-series expansion of  $\Pi_s(s+h)$  and of  $\Omega_s(s+h)$  which is convergent for  $|h| \leq 1$ , then we can derive numerical values of  $\Pi_{s+1}(s)$  and  $\Omega_{s+1}(s)$  from those of  $\Pi_{s+1}(s+1)$  and  $\Omega_{s+1}(s+1)$ , and thence deduce values of  $\Pi_s(s)$  and  $\Omega_s(s)$ . For large  $s$ , the values of  $\Pi_s(s)$  and  $\Omega_s(s)$  are obtainable from the asymptotic series (29) and (30). This iterative process can then be used to derive a table of values of these converging factors for consecutive integral values of  $s$  in descending order.

Thus, there remains the derivation of the Taylor series for  $\Pi_s(s+h)$  and  $\Omega_s(s+h)$ , which are required for interpolation in the tables.

First, we observe that

$$\begin{aligned} \frac{d}{dz} \Gamma_s(-iz) &= -i \frac{d}{d(-iz)} \Gamma_s(-iz) \\ &= \left( \frac{s+1}{z} - i \right) \left( \Pi_s(z) - i \Omega_s(z) \right) + i \quad , \quad (36) \end{aligned}$$

whence

$$\begin{aligned}\frac{d}{dz} \Pi_s(z) &= \operatorname{Re} \frac{d}{dz} \Gamma_s(-iz) \\ &= \frac{s+1}{z} \Pi_s(z) - \Omega_s(z)\end{aligned}\quad (37)$$

and

$$\begin{aligned}\frac{d}{dz} \Omega_s(z) &= -\operatorname{Im} \frac{d}{dz} \Gamma_s(-iz) \\ &= \frac{s+1}{z} \Omega_s(z) + \Pi_s(z) - 1.\end{aligned}\quad (38)$$

If we set  $d_j = \frac{d^j}{dz^j} \Pi_s(z)$  and  $\delta_j = \frac{d^j}{dz^j} \Omega_s(z)$ , evaluated at  $z=s$ ,

then these relations can be written

$$d_1 = \left(1 + \frac{1}{s}\right) d_0 - \delta_0 \quad (39)$$

$$\delta_1 = \left(1 + \frac{1}{s}\right) \delta_0 + d_0 - 1 \quad (40)$$

Next we differentiate both sides of the equation

$$z \frac{d}{dz} \Gamma_s(-iz) = [(s+1) - iz] [\Pi_s(z) - i\Omega_s(z)] + iz \quad (41)$$

with respect to  $z$  and then set  $z=s$ . This yields the equation

$$d_1 - i\delta_2 + s(d_2 - i\delta_2) = -i(d_0 - i\delta_0) + (s+1-is)(d_1 - i\delta_1) + i, \quad (42)$$

which implies

$$d_2 = d_1 - \delta_1 - \frac{\delta_0}{s} \quad (43)$$

and

$$\delta_2 = d_1 + \delta_1 - \frac{1 - d_0}{s}. \quad (44)$$

In a similar manner we find

$$d_3 = (1 - \frac{1}{s})d_2 - \delta_2 - \frac{2}{s} \delta_1 , \quad (45)$$

$$\delta_3 = (1 - \frac{1}{s})\delta_2 + d_2 + \frac{2}{s} d_1 ; \quad (46)$$

and in general

$$d_k = (1 - \frac{k-2}{s})d_{k-1} - \delta_{k-1} - \frac{k-1}{s} \delta_{k-2} , \quad (47)$$

$$\delta_k = (1 - \frac{k-2}{s})\delta_{k-1} + d_{k-1} + \frac{k-1}{s} d_{k-2} , \quad (48)$$

valid for  $k \geq 3$ .

Then the Taylor series for  $\Pi_s(s+h)$  and  $\Omega_s(s+h)$  can be written

$$\Pi_s(s+h) = d_0 + d_1 h + \frac{d_2}{2!} h^2 + \frac{d_3}{3!} h^3 + \dots , \quad (49)$$

$$\Omega_s(s+h) = \delta_0 + \delta_1 h + \frac{\delta_2}{2!} h^2 + \frac{\delta_3}{3!} h^3 + \dots . \quad (50)$$

Thus we have computed appended Table 3 of the converging factor  $\Pi_s(s)$ , designated by  $d_0$ , and its reduced derivatives  $d_j/j!$  (designated as  $D_j$ ) to 35 decimal places for  $s = 2(1)70$ , that is, for all integer values of  $s$  from 2 to 70, inclusive.

As useful by-products, there evolved tables of the converging factors  $\Pi_{s+1}(s)$ ,  $\Omega_s(s)$ , and  $\Omega_{s+1}(s)$ , which have been rounded to 33 decimal places, and appear as Tables 4-6, respectively. (Appendixes B and C),.

For small values of  $z$  and even integer values of  $s$ , the following series given by Dingle<sup>11</sup> is useful:

$$\begin{aligned} \Pi_s(z) = & \frac{z^2}{s(s-1)} - \frac{z^4}{s(s-1)(s-2)(s-3)} + \dots + (-1)^{(s-2)/2} \frac{z^s}{s!} \\ & + \frac{(-1)^{s/2} z^{s+1}}{s!} \left\{ \frac{\pi}{2} \cos z - \sum_{k=0}^{\infty} \frac{(-1)^k z^{2k+1} (\psi(2k+1) - \ln z)}{(2k+1)!} \right\}, \end{aligned} \quad (51)$$

where  $\psi(n) = -\gamma + 1 + \frac{1}{2} + \dots + \frac{1}{n}$ ,  $\psi(0) = -\gamma$ , and  $\gamma$  is Euler's constant.

For odd integer values of  $s$ , Dingle gives the companion series

$$\begin{aligned} \Pi_s(z) = & \frac{z^2}{s(s-1)} - \frac{z^4}{s(s-1)(s-2)(s-3)} + \dots + (-1)^{(s-3)/2} \frac{z^{s-1}}{s!} \\ & + \frac{(-1)^{(s-1)/2} z^{s+1}}{s!} \left\{ \frac{\pi}{2} \sin z + \sum_{k=0}^{\infty} \frac{(-1)^k z^{2k} (\psi(2k) - \ln z)}{(2k)!} \right\}. \end{aligned} \quad (52)$$

When  $z=1$  these series simplify appreciably; thus, we obtain

$$\Pi_1(1) = \frac{\pi}{2} \sin 1 + \psi(0) - \frac{\psi(2)}{2!} + \frac{\psi(4)}{4!} - \frac{\psi(6)}{6!} + \dots, \quad (53)$$

$$2\Pi_2(1) = 1 - \frac{\pi}{2} \cos 1 + \psi(1) - \frac{\psi(3)}{3!} + \frac{\psi(5)}{5!} - \dots; \quad (54)$$

and from Equation (35) we obtain the relation,  $2\Pi_2(1) = \Omega_1(1)$ .

The corresponding numerical values to 45D, obtained from evaluating 20 terms of each of these series, are:

$$\Pi_1(1) = 0.34337\ 79615\ 56427\ 03283\ 25330\ 03858\ 31243\ 40012\ 44019,$$

$$\Omega_1(1) = 0.37855\ 03757\ 64186\ 64236\ 07342\ 71784\ 66067\ 61068\ 35323.$$

The values of these converging factors when computed to about 35 decimal places on the CDC 6700 system, as the final step in the descending iterative procedure beginning with  $\Pi_{70}(70)$  and  $\Omega_{70}(70)$ , differed from the above values by less than  $1 \cdot 10^{-33}$ .

## APPLICATIONS

In the approximation of a function with a discontinuity by a finite number of terms of its expansion in a Fourier series, a paradoxical situation occurs that is known as the Gibbs phenomenon, named after the physicist J.W. Gibbs, who first described it in 1898.

To illustrate this phenomenon consider the Fourier series

$\sum_{n=1}^{\infty} \frac{\sin nt}{n}$  which has the values  $(\pi-t)/2$  for  $0 < t < \pi$ ,  $(t-\pi)/2$  for

$-\pi < t < 0$ , and 0 for  $t = 0$  or  $\pi$ . The approximating curves

$y_n = \sum_{\nu=1}^n \frac{\sin \nu t}{\nu} = f_n(t)$  behave in an extraordinary manner; namely,

near zero the  $n^{\text{th}}$  curve remains above the highest point,  $\frac{\pi}{2}$ , of the straight line by a definite ratio  $K = \frac{2}{\pi} \int_0^{\pi} \frac{\sin t}{t} dt$ , which is called Gibbs' constant.

To evaluate this constant to high precision, we note that

$$K = \frac{2}{\pi} \text{Si}(\pi) = 1 + \frac{2}{\pi} \text{si}(\pi), \quad (55)$$

and then calculate  $\text{si}(\pi)$  by means of the truncated asymptotic series

$$\text{si}(\pi) = \pi^{-1} - 2\pi^{-3} + 24\pi^{-5} \Pi_4(\pi). \quad (56)$$

The converging factor  $\Pi_4(\pi)$  can be calculated from the Taylor series

$$\Pi_4(\pi) = \Pi_4(4) + d_1 h + \frac{d_2}{2!} h^2 + \dots, \quad (57)$$

where  $h = \pi - 4$ , and the coefficients are the reduced derivatives of  $\Pi_s(s)$  evaluated at  $s = 4$ . If 43 terms of this series are summed, each carried to 35 decimal places, there results the value

$$\Pi_4(\pi) = 0.34852\ 97445\ 99239\ 66719\ 19407\ 36171\ 10389.$$

Multiplying this converging factor by  $24\pi^{-5}$  and adding the product to  $\pi^{-1} - 2\pi^{-3}$ , we obtain

$$\text{si}(\pi) = 0.28114\ 07251\ 87569\ 55112\ 97316\ 78518\ 4\dots$$

As a check on the accuracy of this approximation, the value of  $\text{si}(\pi)$  was recalculated by means of the series

$$\text{si}(\pi) = \frac{\pi}{2} - \frac{\pi^3}{3 \cdot 3!} + \frac{\pi^5}{5 \cdot 5!} - \frac{\pi^7}{7 \cdot 7!} + \dots, \quad (58)$$

of which a total of 27 terms sufficed to give the 45-place value

$$\text{si}(\pi) = 0.28114\ 07251\ 87569\ 55112\ 97316\ 78518\ 24000\ 15518\ 69618.$$

This shows that the value computed by means of the asymptotic series as modified by the introduction of an appropriate converging factor is in error by less than  $2 \cdot 10^{-31}$ .

The value of Gibbs' constant is then calculated to be

$$K = 1.17897\ 97444\ 72167\ 27023\ 20288\ 45824\ 90979\ 25874\ 21979\dots$$

to 45 decimal places. This confirms the accuracy of a value calculated to 24 decimal places by D.H. Lehmer<sup>12</sup>.

As a by-product of this calculation we infer from the relation in Equation (5) that

$$\text{Si}(\pi) = 1.85193\ 70519\ 82466\ 17036\ 10533\ 70157\ 99144\ 36504\ 54318\dots$$

A companion calculation consists of evaluating  $\text{Ci}(\pi)$  by the truncated asymptotic series

$$\text{Ci}(\pi) = \pi^{-2} - 6\pi^{-4} \Pi_3(\pi), \quad (59)$$

where the converging factor can be evaluated from the Taylor series

$$\Pi_3(\pi) = \Pi_3(3) + d_1 h + \frac{d_2}{2!} h^2 + \dots, \quad (60)$$

and  $h = \pi - 3$ . Here the coefficients  $d_k/k!$  are the reduced derivatives of  $\Pi_s(s)$  evaluated at  $s = 3$ . A total of 24 terms of this series yield the value

$$\Pi_3(\pi) = 0.44894\ 66750\ 45702\ 27893\ 45552\ 80548\ 12960.$$

If we multiply this converging factor by  $6\pi^{-4}$  and subtract the product from  $\pi^{-2}$ , we obtain

$$Ci(\pi) = 0.07366\ 79120\ 46425\ 48599\ 01009\ 65230\ 0\dots$$

As a check, a total of 27 terms of the series

$$Ci(\pi) = \gamma + \ln \pi - \frac{\pi^2}{2 \cdot 2!} + \frac{\pi^4}{4 \cdot 4!} - \frac{\pi^6}{6 \cdot 6!} + \dots \quad (61)$$

yielded the value

$$Ci(\pi) = 0.07366\ 79120\ 46425\ 48599\ 01009\ 65230\ 14967\ 18698\ 77462,$$

which reveals an error in the previous result of about  $1.5 \cdot 10^{-31}$ .

For  $x = \pi$  we conclude that the calculation of  $Si(x)$  and  $Ci(x)$  to a specified high accuracy by power series involves less computation than that by asymptotic series in conjunction with converging factors.

However, for an argument such as  $2\pi$  this situation is reversed. Thus, by means of the series

$$si(2\pi) = -\frac{1}{2\pi} + \frac{2!}{(2\pi)^3} - \frac{4!}{(2\pi)^5} + \frac{6!}{(2\pi)^7} \Pi_6(2\pi) \quad (62)$$

we find the value

$$si(2\pi) = -0.15264\ 47506\ 62268\ 16898\ 55415\ 29340\ 00201,$$



after determining the converging factor to 35 decimal places from  $\Pi_6(6)$ , using 23 terms of the corresponding Taylor series. On the other hand, the calculation of this value by the power series requires the evaluation of 30 terms, each to at least 35 places. Again, by Equation (5) we deduce the value

$$\text{Si}(2\pi) = 1.41815\ 15761\ 32628\ 45024\ 57801\ 62299\ 74943\ ,$$

to 35 decimal places.

Similarly,  $\text{Ci}(2\pi)$  can be calculated to 35 places from the series

$$\text{Ci}(2\pi) = -\frac{1}{(2\pi)^2} + \frac{3!}{(2\pi)^4} - \frac{5!}{(2\pi)^6} + \frac{7!}{(2\pi)^8} \Pi_7(2\pi) \quad (63)$$

when the converging factor is evaluated to that precision from  $\Pi_7(7)$ , using 30 terms of the Taylor series. This result is

$$\text{Ci}(2\pi) = -0.02256\ 06617\ 46346\ 06764\ 35387\ 78543\ 04643\ ;$$

it was checked by evaluating 32 terms of the corresponding power series.

## ACKNOWLEDGMENTS

The authors wish to acknowledge the contribution of Richard H. Serafin in adapting to the CDC 6700 system the multiprecision subroutines\* used in calculating the tables in this report. Also, the assistance of Professor F. D. Murnaghan in the derivation of the mathematical equations is gratefully acknowledged.

---

\* Informally documented in CMD Technical Note 45-71, entitled "The Lehmer-Weinberger Multiprecision Integer Subroutine Package," October 1971.

## APPENDIX A

### VALUES OF $\Pi_s(s)$ AND OF ITS REDUCED DERIVATIVES

In this appendix are tabulated to 35 decimal places the values of the converging factor  $\Pi_s(s)$  and its reduced derivatives  $D_i$ , defined as  $\frac{1}{i!} \frac{d^i}{dx^i} \Pi_s(x)$  at  $x = s$ . This table (Table 3) has been photographically reproduced from computer sheets upon which the output was left-justified. Accordingly, the position of the decimal point for each tabular entry may be inferred from the right-hand indentation.

TABLE 3 - TABLE OF  $\Pi_s(s)$  AND ITS REDUCED DERIVATIVES  $D_1$   
TO 35 D FOR  $s = 2(1)70$

S = 2

| I  | C SUB I |       |       |       |
|----|---------|-------|-------|-------|
| 0  | 40391   | 60456 | 23264 | 61242 |
| 1  | 18405   | 52205 | 84226 | 60047 |
| 2  | - 31749 | 17027 | 01893 | 24140 |
| 3  | 14915   | 11505 | 50193 | 16393 |
| 4  | 14719   | 99540 | 24558 | 56275 |
| 5  | - 78780 | 80540 | 88462 | 88072 |
| 6  | 29876   | 07055 | 61404 | 27293 |
| 7  | - 99959 | 38707 | 51720 | 35272 |
| 8  | 31867   | 02613 | 50387 | 23845 |
| 9  | - 10023 | 83255 | 37755 | 49637 |
| 10 | 31682   | 17075 | 27209 | 28651 |
| 11 | - 10160 | 69307 | 07700 | 28635 |
| 12 | 33227   | 20561 | 59410 | 46276 |
| 13 | - 11102 | 14122 | 42406 | 15288 |
| 14 | 37914   | 01406 | 50098 | 13763 |
| 15 | - 13224 | 82622 | 06427 | 04766 |
| 16 | 47062   | 51380 | 19091 | 74048 |
| 17 | - 17063 | 04525 | 18092 | 81018 |
| 18 | 62937   | 76720 | 57185 | 18185 |
| 19 | - 23584 | 81220 | 69028 | 50965 |
| 20 | 89670   | 39740 | 15971 | 49404 |
| 21 | - 34549 | 03157 | 88150 | 04468 |
| 22 | 13474   | 56820 | 51330 | 85498 |
| 23 | - 53144 | 02111 | 28118 | 38602 |
| 24 | 21177   | 08327 | 00721 | 22615 |
| 25 | - 85192 | 45078 | 02162 | 61556 |
| 26 | 34573   | 69507 | 20721 | 20513 |
| 27 | - 14145 | 50721 | 23165 | 95898 |
| 28 | 58313   | 00465 | 42916 | 21580 |
| 29 | - 24207 | 93082 | 18400 | 02411 |
| 30 | 10115   | 52525 | 11252 | 32812 |
| 31 | - 42527 | 55059 | 87133 | 47645 |
| 32 | 17581   | 80538 | 53847 | 85218 |
| 33 | - 76440 | 35526 | 16466 | 27581 |
| 34 | 32658   | 57409 | 39527 | 48292 |
| 35 | - 14119 | 34580 | 61531 | 76074 |
| 36 | 80450   | 02640 | 24164 | 6015  |
| 37 | - 26175 | 47615 | 38867 | 3016  |
| 38 | 11379   | 47827 | 15075 | 4301  |
| 39 | - 49657 | 83428 | 72745 | 246   |
| 40 | 21747   | 32747 | 25700 | 233   |
| 41 | - 95564 | 82927 | 83697 | 70    |
| 42 | 42130   | 00220 | 36516 | 38    |
| 43 | - 10630 | 23801 | 22703 | 12    |
| 44 | 82625   | 84481 | 25898 | 2     |
| 45 | - 36747 | 29514 | 61598 | 8     |
| 46 | 16386   | 72158 | 87505 | 0     |
| 47 | - 73259 | 66282 | 79573 |       |
| 48 | 32831   | 90245 | 37749 |       |
| 49 | - 14748 | 25523 | 29174 |       |
| 50 | 66398   | 25319 | 4170  |       |
| 51 | - 29557 | 43061 | 1264  |       |
| 52 | 13544   | 00851 | 6529  |       |
| 53 | - 61354 | 95688 | 036   |       |
| 54 | 27847   | 02146 | 424   |       |
| 55 | - 12662 | 03441 | 715   |       |
| 56 | 57675   | 50245 | 64    |       |
| 57 | - 26316 | 22569 | 08    |       |
| 58 | 12627   | 21052 | 00    |       |
| 59 | - 55054 | 54951 | 5     |       |
| 60 | 25239   | 73800 | 4     |       |
| 61 | - 11588 | 23554 | 3     |       |
| 62 | 53280   | 62461 |       |       |
| 63 | - 24531 | 25408 |       |       |
| 64 | 11309   | 70926 |       |       |
| 65 | - 52208 | 8159  |       |       |
| 66 | 24131   | 2654  |       |       |
| 67 | - 11167 | 1783  |       |       |
| 68 | 51738   | 987   |       |       |
| 69 | - 23598 | 728   |       |       |
| 70 | 11143   | 965   |       |       |
| 71 | - 51803 | 43    |       |       |
| 72 | 24106   | 33    |       |       |
| 73 | - 11229 | 10    |       |       |
| 74 | 52358   | 5     |       |       |
| 75 | - 24436 | 9     |       |       |
| 76 | 11415   | 9     |       |       |
| 77 | - 53379 |       |       |       |
| 78 | 24981   |       |       |       |
| 79 | - 11701 |       |       |       |
| 80 | 5485    |       |       |       |
| 81 | - 2573  |       |       |       |
| 82 | 1208    |       |       |       |
| 83 | - 567   |       |       |       |
| 84 | 267     |       |       |       |
| 85 | - 125   |       |       |       |
| 86 | 55      |       |       |       |
| 87 | - 27    |       |       |       |
| 88 | 13      |       |       |       |
| 89 | - 6     |       |       |       |
| 90 | 2       |       |       |       |
| 91 | - 1     |       |       |       |

S = 3

| I  | D SUE I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 43050   | 94642 | 81085 | 40741 | 01666 | 92627 | 25099 |
| 1  | 13258   | 35246 | 98383 | 77782 | 73629 | 17844 | 89729 |
| 2  | - 16820 | 54841 | 05703 | 41502 | 11000 | 32173 | 7465  |
| 3  | 50276   | 76456 | 83257 | 90903 | 94528 | 45706 | 73    |
| 4  | 41108   | 56382 | 57077 | 15632 | 26495 | 46383 | 58    |
| 5  | - 15180 | 34612 | 18376 | 18923 | 52516 | 15167 | 87    |
| 6  | 37422   | 85848 | 94707 | 39411 | 02755 | 63914 | 1     |
| 7  | - 78049 | 55634 | 60656 | 55096 | 69517 | 50684 |       |
| 8  | 14755   | 95156 | 69832 | 01356 | 74199 | 39462 |       |
| 9  | - 25948 | 31138 | 33191 | 14833 | 78945 | 5772  |       |
| 10 | 42552   | 75261 | 16953 | 31899 | 77356 | 275   |       |
| 11 | - 63529 | 60391 | 84789 | 04772 | 81621 | 73    |       |
| 12 | 78915   | 69777 | 51644 | 30914 | 60616 | 2     |       |
| 13 | - 49549 | 52895 | 99196 | 30006 | 40966 |       |       |
| 14 | - 15147 | 30631 | 62851 | 15999 | 13199 |       |       |
| 15 | 90385   | 68225 | 37728 | 16657 | 5038  |       |       |
| 16 | - 32995 | 31426 | 64789 | 51594 | 3003  |       |       |
| 17 | 10413   | 19009 | 22300 | 28987 | 4796  |       |       |
| 18 | - 30806 | 99488 | 62592 | 92105 | 419   |       |       |
| 19 | 88197   | 26836 | 12069 | 76009 | 58    |       |       |
| 20 | - 24815 | 74932 | 76085 | 40357 | 60    |       |       |
| 21 | 69207   | 00450 | 40835 | 96627 | 4     |       |       |
| 22 | - 19225 | 88789 | 50297 | 63025 | 6     |       |       |
| 23 | 53365   | 60484 | 59458 | 50326 |       |       |       |
| 24 | - 14828 | 79647 | 85567 | 43245 |       |       |       |
| 25 | 41299   | 52424 | 64170 | 4790  |       |       |       |
| 26 | - 11537 | 41913 | 48579 | 8071  |       |       |       |
| 27 | 32344   | 35094 | 07024 | 016   |       |       |       |
| 28 | - 91018 | 68670 | 54844 | 48    |       |       |       |
| 29 | 25713   | 64219 | 23436 | 81    |       |       |       |
| 30 | - 72931 | 80804 | 13879 | 7     |       |       |       |
| 31 | 20767   | 47208 | 40061 | 7     |       |       |       |
| 32 | - 59366 | 11241 | 42752 |       |       |       |       |
| 33 | 17035   | 11621 | 43905 |       |       |       |       |
| 34 | - 49063 | 51608 | 2677  |       |       |       |       |
| 35 | 14181   | 76251 | 7406  |       |       |       |       |
| 36 | - 41134 | 67290 | 274   |       |       |       |       |
| 37 | 11971   | 24783 | 632   |       |       |       |       |
| 38 | - 34951 | 95799 | 25    |       |       |       |       |
| 39 | 10236   | 51571 | 46    |       |       |       |       |
| 40 | - 30069 | 78823 | 1     |       |       |       |       |
| 41 | 88584   | 27535 |       |       |       |       |       |
| 42 | - 26168 | 76006 |       |       |       |       |       |
| 43 | 77511   | 0996  |       |       |       |       |       |
| 44 | - 23017 | 3210  |       |       |       |       |       |
| 45 | 68519   | 400   |       |       |       |       |       |
| 46 | - 20445 | 600   |       |       |       |       |       |
| 47 | 61147   | 01    |       |       |       |       |       |
| 48 | - 18327 | 48    |       |       |       |       |       |
| 49 | 55048   | 8     |       |       |       |       |       |
| 50 | - 16568 | 2     |       |       |       |       |       |
| 51 | 49964   |       |       |       |       |       |       |
| 52 | - 15095 |       |       |       |       |       |       |
| 53 | 4569    |       |       |       |       |       |       |
| 54 | - 1385  |       |       |       |       |       |       |
| 55 | 420     |       |       |       |       |       |       |
| 56 | - 128   |       |       |       |       |       |       |
| 57 | 39      |       |       |       |       |       |       |
| 58 | - 11    |       |       |       |       |       |       |
| 59 | 3       |       |       |       |       |       |       |
| 60 | - 1     |       |       |       |       |       |       |

S = 4

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 44554   | 95690 | 46484 | 46885 | 07495 | 58466 | 67808 |  |
| 1  | 10400   | 23226 | 45417 | 56348 | 53247 | 00395 | 70667 |  |
| 2  | - 10474 | 60219 | 75494 | 69616 | 29661 | 48012 | 1640  |  |
| 3  | 22026   | 34557 | 28394 | 87790 | 96976 | 11909 | 22    |  |
| 4  | 16447   | 75006 | 97940 | 64443 | 98764 | 62808 | 29    |  |
| 5  | - 45389 | 81576 | 99321 | 64452 | 54073 | 69632 | 7     |  |
| 6  | 82006   | 39392 | 42102 | 58645 | 82558 | 53512 |       |  |
| 7  | - 12051 | 28584 | 81101 | 99437 | 32228 | 45679 |       |  |
| 8  | 15057   | 81204 | 60041 | 71227 | 24701 | 8963  |       |  |
| 9  | - 15448 | 77106 | 05234 | 57159 | 56232 | 931   |       |  |
| 10 | 10170   | 86934 | 04116 | 85845 | 46102 | 83    |       |  |
| 11 | 61137   | 15450 | 69142 | 60775 | 82912 |       |       |  |
| 12 | - 42852 | 00264 | 41185 | 60028 | 88071 |       |       |  |
| 13 | 11691   | 71474 | 51475 | 73343 | 00507 |       |       |  |
| 14 | - 25866 | 53966 | 75997 | 23841 | 9826  |       |       |  |
| 15 | 52307   | 06426 | 22721 | 48660 | 729   |       |       |  |
| 16 | - 10103 | 44948 | 63209 | 28709 | 416   |       |       |  |
| 17 | 19044   | 15953 | 48877 | 79326 | 91    |       |       |  |
| 18 | - 35452 | 67051 | 80750 | 55571 | 6     |       |       |  |
| 19 | 65659   | 56086 | 70126 | 29249 |       |       |       |  |
| 20 | - 12154 | 04229 | 00850 | 58316 |       |       |       |  |
| 21 | 22553   | 95738 | 99988 | 9367  |       |       |       |  |
| 22 | - 42039 | 14348 | 58745 | 739   |       |       |       |  |
| 23 | 78806   | 04605 | 13740 | 31    |       |       |       |  |
| 24 | - 14868 | 85217 | 74562 | 10    |       |       |       |  |
| 25 | 28248   | 89795 | 48086 | 4     |       |       |       |  |
| 26 | - 54053 | 74112 | 35597 |       |       |       |       |  |
| 27 | 10417   | 77103 | 89773 |       |       |       |       |  |
| 28 | - 20222 | 06094 | 7063  |       |       |       |       |  |
| 29 | 39529   | 54146 | 799   |       |       |       |       |  |
| 30 | - 77801 | 23408 | 64    |       |       |       |       |  |
| 31 | 15414   | 46172 | 84    |       |       |       |       |  |
| 32 | - 30736 | 05074 | 4     |       |       |       |       |  |
| 33 | 61665   | 47302 |       |       |       |       |       |  |
| 34 | - 12445 | 30377 |       |       |       |       |       |  |
| 35 | 25260   | 0453  |       |       |       |       |       |  |
| 36 | - 51549 | 645   |       |       |       |       |       |  |
| 37 | 10575   | 010   |       |       |       |       |       |  |
| 38 | - 21802 | 36    |       |       |       |       |       |  |
| 39 | 45165   | 0     |       |       |       |       |       |  |
| 40 | - 93991 |       |       |       |       |       |       |  |
| 41 | 19646   |       |       |       |       |       |       |  |
| 42 | - 4123  |       |       |       |       |       |       |  |
| 43 | 869     |       |       |       |       |       |       |  |
| 44 | - 183   |       |       |       |       |       |       |  |
| 45 | 39      |       |       |       |       |       |       |  |
| 46 | - 8     |       |       |       |       |       |       |  |
| 47 | 1       |       |       |       |       |       |       |  |

S = 5

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 45523   | 70588 | 04917 | 28727 | 42872 | 20562 | 70980 |
| 1  | 85708   | 24288 | 59819 | 56121 | 90664 | 86225 | 4647  |
| 2  | - 71677 | 67335 | 41081 | 76012 | 56897 | 20697 | 536   |
| 3  | 11266   | 21312 | 04918 | 53617 | 71493 | 29568 | 73    |
| 4  | 79164   | 99391 | 11338 | 93014 | 88195 | 69132 | 1     |
| 5  | - 17398 | 53823 | 42393 | 97572 | 21273 | 38345 | 0     |
| 6  | 24629   | 03184 | 92338 | 90650 | 70386 | 48470 |       |
| 7  | - 27312 | 12827 | 58467 | 03616 | 38113 | 2960  |       |
| 8  | 23748   | 43486 | 29823 | 97200 | 34694 | 236   |       |
| 9  | - 12790 | 75741 | 70633 | 83057 | 90890 | 64    |       |
| 10 | - 63406 | 42894 | 76011 | 25688 | 56902 |       |       |
| 11 | 34294   | 62211 | 12072 | 32489 | 61099 |       |       |
| 12 | - 71822 | 04031 | 45119 | 84204 | 2115  |       |       |
| 13 | 11997   | 96014 | 11506 | 23468 | 9661  |       |       |
| 14 | - 18029 | 87827 | 35033 | 82783 | 818   |       |       |
| 15 | 25492   | 16996 | 91292 | 81095 | 98    |       |       |
| 16 | - 34670 | 26445 | 18613 | 70514 | 7     |       |       |
| 17 | 45926   | 02069 | 55554 | 85577 |       |       |       |
| 18 | - 59693 | 75523 | 97773 | 1725  |       |       |       |
| 19 | 76458   | 01393 | 97558 | 737   |       |       |       |
| 20 | - 96695 | 61294 | 72495 | 99    |       |       |       |
| 21 | 12074   | 98314 | 05821 | 57    |       |       |       |
| 22 | - 14857 | 90859 | 15400 | 2     |       |       |       |
| 23 | 17927   | 78487 | 94177 |       |       |       |       |
| 24 | - 21018 | 99451 | 7777  |       |       |       |       |
| 25 | 23529   | 93466 | 108   |       |       |       |       |
| 26 | - 24234 | 89871 | 31    |       |       |       |       |
| 27 | 20773   | 07639 | 6     |       |       |       |       |
| 28 | - 87482 | 6079  |       |       |       |       |       |
| 29 | - 19849 | 9765  |       |       |       |       |       |
| 30 | 79406   | 300   |       |       |       |       |       |
| 31 | - 19549 | 458   |       |       |       |       |       |
| 32 | 41326   | 75    |       |       |       |       |       |
| 33 | - 81206 | 6     |       |       |       |       |       |
| 34 | 15308   | 6     |       |       |       |       |       |
| 35 | - 28125 |       |       |       |       |       |       |
| 36 | 5081    |       |       |       |       |       |       |
| 37 | - 907   |       |       |       |       |       |       |
| 38 | 160     |       |       |       |       |       |       |
| 39 | - 28    |       |       |       |       |       |       |
| 40 | 4       |       |       |       |       |       |       |

S = 6

| I  | D SUB I |       |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|-------|
| 0  |         | 46200 | 07695 | 48806 | 52637 | 10099 | 53089 | 58386 |
| 1  |         | 72955 | 07296 | 53203 | 90317 | 34121 | 26900 | 7795  |
| 2  | -       | 52200 | 64852 | 82343 | 94371 | 70191 | 92048 | 843   |
| 3  |         | 63915 | 44126 | 27590 | 73346 | 10340 | 99471 | 2     |
| 4  |         | 42980 | 12634 | 48898 | 74713 | 95086 | 84541 | 6     |
| 5  | -       | 78352 | 43311 | 02051 | 28244 | 47408 | 13618 |       |
| 6  |         | 90712 | 00899 | 36966 | 90958 | 03480 | 1000  |       |
| 7  | -       | 79346 | 19403 | 94529 | 07610 | 55064 | 565   |       |
| 8  |         | 49142 | 60749 | 22494 | 66151 | 18328 | 65    |       |
| 9  | -       | 74743 | 35756 | 28030 | 15639 | 25337 |       |       |
| 10 | -       | 38211 | 99562 | 31010 | 40342 | 27183 |       |       |
| 11 |         | 81783 | 31208 | 50613 | 95216 | 0797  |       |       |
| 12 | -       | 11891 | 95244 | 29071 | 92726 | 4912  |       |       |
| 13 |         | 14702 | 70419 | 77061 | 09397 | 350   |       |       |
| 14 | -       | 16485 | 67428 | 88888 | 90101 | 95    |       |       |
| 15 |         | 17203 | 42147 | 57889 | 69273 | 4     |       |       |
| 16 | -       | 16862 | 01123 | 66908 | 62911 |       |       |       |
| 17 |         | 15474 | 88403 | 87988 | 8932  |       |       |       |
| 18 | -       | 13034 | 99132 | 32266 | 720   |       |       |       |
| 19 |         | 94933 | 55569 | 78807 | 4     |       |       |       |
| 20 | -       | 47412 | 99741 | 54835 |       |       |       |       |
| 21 | -       | 14066 | 06184 | 7616  |       |       |       |       |
| 22 |         | 92317 | 83312 | 470   |       |       |       |       |
| 23 | -       | 19135 | 96043 | 014   |       |       |       |       |
| 24 |         | 31673 | 66568 | 38    |       |       |       |       |
| 25 | -       | 47596 | 55227 | 1     |       |       |       |       |
| 26 |         | 67914 | 05263 |       |       |       |       |       |
| 27 | -       | 93976 | 5566  |       |       |       |       |       |
| 28 |         | 12758 | 9196  |       |       |       |       |       |
| 29 | -       | 17116 | 763   |       |       |       |       |       |
| 30 |         | 22795 | 15    |       |       |       |       |       |
| 31 | -       | 30229 | 7     |       |       |       |       |       |
| 32 |         | 40008 |       |       |       |       |       |       |
| 33 | -       | 5292  |       |       |       |       |       |       |
| 34 |         | 700   |       |       |       |       |       |       |
| 35 | -       | 92    |       |       |       |       |       |       |
| 36 |         | 12    |       |       |       |       |       |       |
| 37 | -       | 1     |       |       |       |       |       |       |



S = 7

| I  | D SUE I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 46699   | 13110 | 61784 | 03082 | 68894 | 97670 | 49347 |
| 1  | 63540   | 02606 | 71043 | 92071 | 35748 | 90286 | 4991  |
| 2  | - 39741 | 39989 | 38954 | 91638 | 93780 | 07062 | 162   |
| 3  | 39073   | 02778 | 47304 | 92543 | 63874 | 40918 | 7     |
| 4  | 25410   | 65652 | 20332 | 28247 | 34116 | 64389 | 9     |
| 5  | - 39529 | 09780 | 07664 | 16107 | 51532 | 87784 |       |
| 6  | 38569   | 22190 | 21476 | 10082 | 03183 | 4234  |       |
| 7  | - 27453 | 97634 | 35901 | 71206 | 92485 | 248   |       |
| 8  | 12157   | 54004 | 92525 | 33533 | 18335 | 98    |       |
| 9  | 25378   | 67229 | 32832 | 50111 | 08197 |       |       |
| 10 | - 13811 | 45044 | 27553 | 55609 | 06323 |       |       |
| 11 | 20637   | 23264 | 23960 | 94230 | 6010  |       |       |
| 12 | - 23226 | 62662 | 08487 | 23270 | 157   |       |       |
| 13 | 22441   | 00635 | 02342 | 72034 | 15    |       |       |
| 14 | - 19342 | 32523 | 08275 | 45593 | 0     |       |       |
| 15 | 14918   | 58986 | 52492 | 37439 |       |       |       |
| 16 | - 99555 | 85516 | 44518 | 344   |       |       |       |
| 17 | 50065   | 20322 | 12900 | 16    |       |       |       |
| 18 | - 41533 | 31209 | 73431 |       |       |       |       |
| 19 | - 36380 | 73883 | 30011 |       |       |       |       |
| 20 | 70897   | 13551 | 6627  |       |       |       |       |
| 21 | - 99498 | 70853 | 955   |       |       |       |       |
| 22 | 12271   | 13676 | 201   |       |       |       |       |
| 23 | - 14125 | 96653 | 76    |       |       |       |       |
| 24 | 15592   | 14613 | 8     |       |       |       |       |
| 25 | - 16744 | 17816 |       |       |       |       |       |
| 26 | 17648   | 7635  |       |       |       |       |       |
| 27 | - 18362 | 920   |       |       |       |       |       |
| 28 | 18933   | 67    |       |       |       |       |       |
| 29 | - 19398 | 5     |       |       |       |       |       |
| 30 | 19786   |       |       |       |       |       |       |
| 31 | - 2011  |       |       |       |       |       |       |
| 32 | 204     |       |       |       |       |       |       |
| 33 | - 20    |       |       |       |       |       |       |
| 34 | 2       |       |       |       |       |       |       |

S = 8

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 47082   | 51123 | 20588 | 52328 | 73241 | 13458 | 10303 |  |
| 1  | 56296   | 33874 | 21036 | 57669 | 13643 | 26977 | 1388  |  |
| 2  | - 31280 | 82175 | 84145 | 22022 | 83337 | 21935 | 208   |  |
| 3  | 25278   | 89825 | 27979 | 70353 | 45054 | 59039 | 8     |  |
| 4  | 16011   | 76916 | 62335 | 10832 | 36043 | 37558 | 1     |  |
| 5  | - 21703 | 65455 | 94010 | 86956 | 58116 | 00911 |       |  |
| 6  | 18248   | 29790 | 59734 | 98964 | 73965 | 1468  |       |  |
| 7  | - 10819 | 58432 | 09176 | 99855 | 40754 | 449   |       |  |
| 8  | 33760   | 92043 | 63845 | 40556 | 65045 | 5     |       |  |
| 9  | 20494   | 06461 | 92995 | 38846 | 20769 |       |       |  |
| 10 | - 49827 | 59046 | 50806 | 51275 | 0194  |       |       |  |
| 11 | 58326   | 94482 | 18892 | 45457 | 190   |       |       |  |
| 12 | - 53180 | 99931 | 13928 | 65879 | 54    |       |       |  |
| 13 | 41221   | 75508 | 60952 | 14032 | 2     |       |       |  |
| 14 | - 27464 | 96987 | 09568 | 58599 |       |       |       |  |
| 15 | 14912   | 74792 | 80389 | 3049  |       |       |       |  |
| 16 | - 49469 | 60708 | 59533 | 32    |       |       |       |  |
| 17 | - 21238 | 82523 | 27573 | 7     |       |       |       |  |
| 18 | 65830   | 39144 | 97683 |       |       |       |       |  |
| 19 | - 89621 | 13466 | 9143  |       |       |       |       |  |
| 20 | 98324   | 76132 | 461   |       |       |       |       |  |
| 21 | - 96991 | 25369 | 61    |       |       |       |       |  |
| 22 | 89609   | 71759 | 2     |       |       |       |       |  |
| 23 | - 79084 | 44704 |       |       |       |       |       |  |
| 24 | 67385   | 6036  |       |       |       |       |       |  |
| 25 | - 55755 | 614   |       |       |       |       |       |  |
| 26 | 44909   | 26    |       |       |       |       |       |  |
| 27 | - 35201 | 0     |       |       |       |       |       |  |
| 28 | 26753   |       |       |       |       |       |       |  |
| 29 | - 1954  |       |       |       |       |       |       |  |
| 30 | 134     |       |       |       |       |       |       |  |
| 31 | - 8     |       |       |       |       |       |       |  |

S = 9

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 47386   | 24328 | 69194 | 14993 | 42317 | 43801 | 00225 |
| 1  | 50546   | 47550 | 49676 | 30295 | 93601 | 21220 | 5967  |
| 2  | - 25269 | 07945 | 19697 | 02726 | 52968 | 41988 | 079   |
| 3  | 17100   | 25259 | 51073 | 09134 | 17442 | 52435 | 7     |
| 4  | 10602   | 09133 | 49910 | 63786 | 81847 | 52560 | 8     |
| 5  | - 12724 | 77200 | 07183 | 36981 | 53064 | 99599 |       |
| 6  | 93789   | 49639 | 60278 | 45866 | 87292 | 640   |       |
| 7  | - 47168 | 13451 | 82771 | 31198 | 72247 | 21    |       |
| 8  | 99754   | 22190 | 96038 | 21641 | 73644 |       |       |
| 9  | 11320   | 94304 | 32542 | 25590 | 99819 |       |       |
| 10 | - 19063 | 76683 | 57341 | 19479 | 4514  |       |       |
| 11 | 18388   | 90439 | 75480 | 29805 | 140   |       |       |
| 12 | - 13946 | 37909 | 82728 | 68920 | 32    |       |       |
| 13 | 87933   | 22716 | 27114 | 99023 |       |       |       |
| 14 | - 44607 | 52584 | 11392 | 6957  |       |       |       |
| 15 | 14325   | 19794 | 10779 | 695   |       |       |       |
| 16 | 37025   | 55219 | 00375 | 7     |       |       |       |
| 17 | - 12454 | 52527 | 43804 | 3     |       |       |       |
| 18 | 15161   | 31754 | 13004 |       |       |       |       |
| 19 | - 14459 | 82219 | 0262  |       |       |       |       |
| 20 | 12185   | 39920 | 593   |       |       |       |       |
| 21 | - 94629 | 66424 | 4     |       |       |       |       |
| 22 | 68941   | 64620 |       |       |       |       |       |
| 23 | - 47407 | 9236  |       |       |       |       |       |
| 24 | 30675   | 492   |       |       |       |       |       |
| 25 | - 18391 | 37    |       |       |       |       |       |
| 26 | 97971   |       |       |       |       |       |       |
| 27 | - 4056  |       |       |       |       |       |       |
| 28 | 41      |       |       |       |       |       |       |
| 29 | 17      |       |       |       |       |       |       |
| 30 | - 2     |       |       |       |       |       |       |

S = 10

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 47632   | 79825 | 24009 | 77020 | 41272 | 49830 | 83659 |  |
| 1  | 45869   | 30025 | 41280 | 95038 | 79163 | 59913 | 2747  |  |
| 2  | - 20842 | 29448 | 31042 | 88941 | 16810 | 21331 | 021   |  |
| 3  | 11992   | 52804 | 78884 | 66874 | 14559 | 98006 | 8     |  |
| 4  | 73046   | 43931 | 89132 | 58452 | 27162 | 30327 |       |  |
| 5  | - 78622 | 69978 | 72942 | 45893 | 15455 | 0837  |       |  |
| 6  | 51498   | 51182 | 21843 | 34508 | 79301 | 404   |       |  |
| 7  | - 22291 | 05827 | 56772 | 23247 | 80574 | 65    |       |  |
| 8  | 29413   | 46596 | 18132 | 53556 | 11874 |       |       |  |
| 9  | 59130   | 66521 | 24207 | 36118 | 4290  |       |       |  |
| 10 | - 77973 | 86152 | 31361 | 40678 | 571   |       |       |  |
| 11 | 63832   | 36463 | 52048 | 08008 | 05    |       |       |  |
| 12 | - 40983 | 58894 | 94778 | 82226 | 5     |       |       |  |
| 13 | 21144   | 03410 | 16966 | 26429 |       |       |       |  |
| 14 | - 78047 | 95419 | 91028 | 350   |       |       |       |  |
| 15 | 44694   | 47215 | 09598 | 2     |       |       |       |  |
| 16 | 27359   | 80684 | 09620 | 4     |       |       |       |  |
| 17 | - 35062 | 78171 | 18012 |       |       |       |       |  |
| 18 | 31334   | 64721 | 2359  |       |       |       |       |  |
| 19 | - 23769 | 08849 | 426   |       |       |       |       |  |
| 20 | 16183   | 24550 | 94    |       |       |       |       |  |
| 21 | - 10074 | 55245 | 0     |       |       |       |       |  |
| 22 | 57251   | 4193  |       |       |       |       |       |  |
| 23 | - 28945 | 409   |       |       |       |       |       |  |
| 24 | 11937   | 38    |       |       |       |       |       |  |
| 25 | - 25605 |       |       |       |       |       |       |  |
| 26 | - 2042  |       |       |       |       |       |       |  |
| 27 | 386     |       |       |       |       |       |       |  |
| 28 | - 42    |       |       |       |       |       |       |  |
| 29 | 3       |       |       |       |       |       |       |  |

S = 11

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 47836   | 92135 | 27719 | 26957 | 07035 | 84154 | 28736 |
| 1  | 41988   | 93742 | 72430 | 90743 | 48207 | 73466 | 1937  |
| 2  | - 17487 | 30026 | 38868 | 47719 | 24067 | 73235 | 571   |
| 3  | 86650   | 14498 | 00369 | 38461 | 52613 | 56861 |       |
| 4  | 51995   | 23923 | 83013 | 38330 | 65485 | 77792 |       |
| 5  | - 50709 | 58504 | 53445 | 93673 | 67454 | 3870  |       |
| 6  | 29847   | 72499 | 56901 | 52396 | 34586 | 574   |       |
| 7  | - 11253 | 98936 | 63695 | 52453 | 69102 | 33    |       |
| 8  | 76058   | 13812 | 81512 | 51206 | 4450  |       |       |
| 9  | 31076   | 96985 | 27549 | 77242 | 9270  |       |       |
| 10 | - 33976 | 78718 | 95856 | 33081 | 695   |       |       |
| 11 | 24079   | 67980 | 93250 | 27576 | 61    |       |       |
| 12 | - 13254 | 48455 | 44634 | 40830 | 3     |       |       |
| 13 | 55916   | 35874 | 38296 | 4207  |       |       |       |
| 14 | - 13443 | 74752 | 53322 | 322   |       |       |       |
| 15 | - 50044 | 30435 | 76785 | 3     |       |       |       |
| 16 | 10112   | 80642 | 28562 | 7     |       |       |       |
| 17 | - 93168 | 48297 | 6451  |       |       |       |       |
| 18 | 67362   | 03477 | 259   |       |       |       |       |
| 19 | - 42155 | 21357 | 06    |       |       |       |       |
| 20 | 23456   | 11166 | 7     |       |       |       |       |
| 21 | - 11522 | 98688 |       |       |       |       |       |
| 22 | 47316   | 870   |       |       |       |       |       |
| 23 | - 12772 | 50    |       |       |       |       |       |
| 24 | - 24351 |       |       |       |       |       |       |
| 25 | 7545    |       |       |       |       |       |       |
| 26 | - 799   |       |       |       |       |       |       |
| 27 | 66      |       |       |       |       |       |       |
| 28 | - 4     |       |       |       |       |       |       |

S = 12

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 48008   | 69007 | 75239 | 68016 | 15505 | 64374 | 18352 |
| 1  | 38716   | 94961 | 03773 | 20174 | 28049 | 45791 | 3308  |
| 2  | - 14883 | 38105 | 17504 | 11051 | 73505 | 82393 | 855   |
| 3  | 64198   | 49190 | 07864 | 26605 | 30933 | 67021 |       |
| 4  | 38033   | 25325 | 55455 | 18927 | 92634 | 60675 |       |
| 5  | - 33898 | 76624 | 73589 | 95444 | 80148 | 3831  |       |
| 6  | 18096   | 50994 | 48868 | 95278 | 57196 | 585   |       |
| 7  | - 60038 | 73102 | 81540 | 10679 | 03529 | 2     |       |
| 8  | 87067   | 31080 | 27876 | 07389 | 301   |       |       |
| 9  | 16730   | 78600 | 41657 | 41572 | 5482  |       |       |
| 10 | - 15677 | 36674 | 75068 | 13754 | 827   |       |       |
| 11 | 97603   | 24775 | 53582 | 74735 | 3     |       |       |
| 12 | - 46494 | 58212 | 16890 | 31099 |       |       |       |
| 13 | 15920   | 22389 | 75141 | 6505  |       |       |       |
| 14 | - 17647 | 00619 | 69677 | 84    |       |       |       |
| 15 | - 29568 | 03265 | 78207 | 5     |       |       |       |
| 16 | 34408   | 74663 | 10762 |       |       |       |       |
| 17 | - 25558 | 11219 | 2265  |       |       |       |       |
| 18 | 15495   | 70941 | 186   |       |       |       |       |
| 19 | - 81056 | 87561 | 0     |       |       |       |       |
| 20 | 36547   | 38091 |       |       |       |       |       |
| 21 | - 13315 | 7072  |       |       |       |       |       |
| 22 | 27926   | 72    |       |       |       |       |       |
| 23 | 11224   | 0     |       |       |       |       |       |
| 24 | - 20377 |       |       |       |       |       |       |
| 25 | 1819    |       |       |       |       |       |       |
| 26 | - 131   |       |       |       |       |       |       |
| 27 | 8       |       |       |       |       |       |       |

S = 13

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 48155   | 22582 | 58320 | 87716 | 19357 | 50801 | 31532 |
| 1  | 35920   | 15362 | 86211 | 41060 | 00577 | 30174 | 8016  |
| 2  | - 12821 | 59642 | 26484 | 34867 | 79728 | 32939 | 564   |
| 3  | 48594   | 11702 | 76379 | 15823 | 94279 | 44656 |       |
| 4  | 28471   | 60003 | 64422 | 94883 | 86047 | 02158 |       |
| 5  | - 23359 | 01799 | 10684 | 35956 | 20937 | 2009  |       |
| 6  | 11398   | 43453 | 49813 | 03934 | 32901 | 551   |       |
| 7  | - 33563 | 16023 | 57390 | 59313 | 20499 | 7     |       |
| 8  | - 10056 | 70110 | 87183 | 97659 | 7292  |       |       |
| 9  | 92732   | 88009 | 65971 | 56681 | 410   |       |       |
| 10 | - 76124 | 05284 | 27985 | 69524 | 55    |       |       |
| 11 | 42108   | 29755 | 36266 | 51355 | 2     |       |       |
| 12 | - 17483 | 60896 | 01022 | 16317 |       |       |       |
| 13 | 47826   | 50863 | 28296 | 565   |       |       |       |
| 14 | 15341   | 27274 | 61941 | 3     |       |       |       |
| 15 | - 13450 | 00000 | 21938 | 9     |       |       |       |
| 16 | 11808   | 30672 | 12914 |       |       |       |       |
| 17 | - 73957 | 96018 | 793   |       |       |       |       |
| 18 | 38251   | 83106 | 75    |       |       |       |       |
| 19 | - 16747 | 13921 | 2     |       |       |       |       |
| 20 | 59271   | 5075  |       |       |       |       |       |
| 21 | - 13039 | 306   |       |       |       |       |       |
| 22 | - 28594 | 7     |       |       |       |       |       |
| 23 | 61192   |       |       |       |       |       |       |
| 24 | - 5167  |       |       |       |       |       |       |
| 25 | 342     |       |       |       |       |       |       |
| 26 | - 19    |       |       |       |       |       |       |
| 27 | 1       |       |       |       |       |       |       |

S = 14

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 48281   | 70369 | 79771 | 77667 | 62017 | 84125 | 92488 |
| 1  | 33501   | 70448 | 14687 | 97979 | 71517 | 64591 | 1962  |
| 2  | - 11161 | 02655 | 51938 | 64268 | 96948 | 38283 | 930   |
| 3  | 37469   | 92485 | 42458 | 72574 | 66726 | 12714 |       |
| 4  | 21742   | 16462 | 37823 | 06734 | 58090 | 41786 |       |
| 5  | - 16521 | 03460 | 09972 | 12145 | 43968 | 9152  |       |
| 6  | 74183   | 56022 | 46279 | 85975 | 54418 | 58    |       |
| 7  | - 19531 | 69867 | 86452 | 29656 | 08826 | 2     |       |
| 8  | - 13225 | 00110 | 66631 | 94952 | 5684  |       |       |
| 9  | 52943   | 66242 | 53750 | 82656 | 588   |       |       |
| 10 | - 38678 | 24032 | 71318 | 21032 | 46    |       |       |
| 11 | 19184   | 42929 | 64448 | 45256 | 0     |       |       |
| 12 | - 69806 | 77732 | 12123 | 5025  |       |       |       |
| 13 | 14831   | 93464 | 90783 | 968   |       |       |       |
| 14 | 30872   | 82023 | 93413 | 3     |       |       |       |
| 15 | - 58127 | 78267 | 59666 |       |       |       |       |
| 16 | 41928   | 51833 | 3360  |       |       |       |       |
| 17 | - 22665 | 21404 | 487   |       |       |       |       |
| 18 | 10086   | 32072 | 91    |       |       |       |       |
| 19 | - 36642 | 13531 |       |       |       |       |       |
| 20 | 94089   | 660   |       |       |       |       |       |
| 21 | - 75957 |       |       |       |       |       |       |
| 22 | - 20281 | 4     |       |       |       |       |       |
| 23 | 18113   |       |       |       |       |       |       |
| 24 | - 1158  |       |       |       |       |       |       |
| 25 | 63      |       |       |       |       |       |       |
| 26 | - 3     |       |       |       |       |       |       |



S = 15

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 48391   | 97479 | 27790 | 70479 | 43700 | 52906 | 22885 |
| 1  | 31389   | 46648 | 28422 | 10283 | 23422 | 93148 | 7375  |
| 2  | - 98037 | 95741 | 06042 | 99299 | 88582 | 73902 | 96    |
| 3  | 29363   | 19221 | 63880 | 05674 | 14322 | 13642 |       |
| 4  | 16893   | 09089 | 75428 | 79177 | 95726 | 92120 |       |
| 5  | - 11951 | 97784 | 11382 | 92720 | 99502 | 6894  |       |
| 6  | 49670   | 56758 | 51940 | 89360 | 51284 | 25    |       |
| 7  | - 11769 | 93269 | 34952 | 74010 | 07768 | 1     |       |
| 8  | - 11784 | 39530 | 17482 | 93084 | 1511  |       |       |
| 9  | 31098   | 35959 | 95872 | 89839 | 381   |       |       |
| 10 | - 20462 | 01692 | 13736 | 77427 | 06    |       |       |
| 11 | 91700   | 55285 | 03943 | 93162 |       |       |       |
| 12 | - 29361 | 57862 | 81743 | 0255  |       |       |       |
| 13 | 46124   | 38845 | 04785 | 67    |       |       |       |
| 14 | 21122   | 79096 | 42375 | 8     |       |       |       |
| 15 | - 25155 | 18596 | 22031 |       |       |       |       |
| 16 | 15520   | 24193 | 2765  |       |       |       |       |
| 17 | - 73432 | 63575 | 36    |       |       |       |       |
| 18 | 28209   | 47360 | 0     |       |       |       |       |
| 19 | - 83255 | 4693  |       |       |       |       |       |
| 20 | 12340   | 475   |       |       |       |       |       |
| 21 | 61533   | 7     |       |       |       |       |       |
| 22 | - 74152 |       |       |       |       |       |       |
| 23 | 4886    |       |       |       |       |       |       |
| 24 | - 258   |       |       |       |       |       |       |
| 25 | 11      |       |       |       |       |       |       |

S = 16

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 48488   | 96408 | 92146 | 53510 | 79695 | 22529 | 00881 |  |
| 1  | 29528   | 58924 | 14359 | 49099 | 68607 | 32923 | 5568  |  |
| 2  | - 86801 | 88164 | 94524 | 25869 | 07183 | 40354 | 41    |  |
| 3  | 23340   | 52006 | 99017 | 64397 | 35026 | 16210 |       |  |
| 4  | 13326   | 40381 | 91828 | 77883 | 75933 | 13959 |       |  |
| 5  | - 88196 | 05165 | 44967 | 43306 | 62820 | 437   |       |  |
| 6  | 34094   | 89264 | 22855 | 92750 | 97932 | 67    |       |  |
| 7  | - 73131 | 29482 | 33004 | 88802 | 86733 |       |       |  |
| 8  | - 93778 | 41754 | 80287 | 78683 | 688   |       |       |  |
| 9  | 18759   | 34036 | 06840 | 74821 | 188   |       |       |  |
| 10 | - 11222 | 76054 | 76489 | 94782 | 78    |       |       |  |
| 11 | 45736   | 80771 | 89080 | 46605 |       |       |       |  |
| 12 | - 12924 | 61253 | 78265 | 7183  |       |       |       |  |
| 13 | 13674   | 22783 | 56086 | 85    |       |       |       |  |
| 14 | 12187   | 61165 | 85997 | 6     |       |       |       |  |
| 15 | - 11101 | 40340 | 63800 |       |       |       |       |  |
| 16 | 59960   | 57316 | 745   |       |       |       |       |  |
| 17 | - 25058 | 80274 | 30    |       |       |       |       |  |
| 18 | 83025   | 07781 |       |       |       |       |       |  |
| 19 | - 19084 | 9609  |       |       |       |       |       |  |
| 20 | 13727   | 5     |       |       |       |       |       |  |
| 21 | 31595   | 2     |       |       |       |       |       |  |
| 22 | - 24251 |       |       |       |       |       |       |  |
| 23 | 1312    |       |       |       |       |       |       |  |
| 24 | - 59    |       |       |       |       |       |       |  |
| 25 | 2       |       |       |       |       |       |       |  |

S = 17

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 48574   | 93298 | 64189 | 70348 | 41325 | 62883 | 93744 |  |
| 1  | 27876   | 61300 | 52230 | 76893 | 24025 | 77514 | 1872  |  |
| 2  | - 77394 | 46109 | 12075 | 84744 | 74211 | 69370 | 70    |  |
| 3  | 18789   | 36733 | 25239 | 35480 | 51111 | 91433 |       |  |
| 4  | 10655   | 07332 | 34375 | 39890 | 77671 | 34630 |       |  |
| 5  | - 66231 | 62770 | 27259 | 73914 | 97000 | 848   |       |  |
| 6  | 23923   | 10174 | 10304 | 59453 | 62946 | 05    |       |  |
| 7  | - 46686 | 67022 | 86058 | 34209 | 79821 |       |       |  |
| 8  | - 71349 | 16028 | 06758 | 78388 | 443   |       |       |  |
| 9  | 11598   | 43845 | 57268 | 63194 | 793   |       |       |  |
| 10 | - 63578 | 63132 | 07646 | 34255 | 7     |       |       |  |
| 11 | 23693   | 74580 | 89866 | 09850 |       |       |       |  |
| 12 | - 59209 | 39678 | 51242 | 631   |       |       |       |  |
| 13 | 33921   | 90512 | 14584 | 1     |       |       |       |  |
| 14 | 66881   | 15194 | 31797 |       |       |       |       |  |
| 15 | - 50302 | 98663 | 9828  |       |       |       |       |  |
| 16 | 24146   | 28578 | 267   |       |       |       |       |  |
| 17 | - 89684 | 37505 | 7     |       |       |       |       |  |
| 18 | 25499   | 18110 |       |       |       |       |       |  |
| 19 | - 41843 | 036   |       |       |       |       |       |  |
| 20 | - 93139 | 8     |       |       |       |       |       |  |
| 21 | 12945   | 4     |       |       |       |       |       |  |
| 22 | - 7797  |       |       |       |       |       |       |  |
| 23 | 361     |       |       |       |       |       |       |  |
| 24 | - 14    |       |       |       |       |       |       |  |

S = 18

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 48651   | 65733 | 28839 | 68722 | 26367 | 91275 | 18990 |  |
| 1  | 26400   | 15066 | 30670 | 26536 | 20133 | 60363 | 5197  |  |
| 2  | - 69438 | 97684 | 64959 | 34255 | 33753 | 22328 | 60    |  |
| 3  | 15297   | 72957 | 07010 | 23280 | 92230 | 52719 |       |  |
| 4  | 86219   | 65233 | 67399 | 98897 | 09104 | 2466  |       |  |
| 5  | - 50518 | 96464 | 56453 | 11301 | 51484 | 696   |       |  |
| 6  | 17117   | 17930 | 86211 | 15687 | 62495 | 58    |       |  |
| 7  | - 30532 | 45551 | 10876 | 18466 | 95259 |       |       |  |
| 8  | - 53281 | 48916 | 84318 | 45281 | 830   |       |       |  |
| 9  | 73357   | 74666 | 79675 | 54752 | 32    |       |       |  |
| 10 | - 37084 | 68200 | 62660 | 23432 | 7     |       |       |  |
| 11 | 12699   | 33792 | 24730 | 51543 |       |       |       |  |
| 12 | - 28094 | 31110 | 78751 | 849   |       |       |       |  |
| 13 | 29347   | 98645 | 04553 |       |       |       |       |  |
| 14 | 36274   | 72035 | 62491 |       |       |       |       |  |
| 15 | - 23454 | 61508 | 6326  |       |       |       |       |  |
| 16 | 10112   | 89418 | 240   |       |       |       |       |  |
| 17 | - 33519 | 20823 | 6     |       |       |       |       |  |
| 18 | 80977   | 5969  |       |       |       |       |       |  |
| 19 | - 75896 | 64    |       |       |       |       |       |  |
| 20 | - 59922 | 2     |       |       |       |       |       |  |
| 21 | 50164   |       |       |       |       |       |       |  |
| 22 | - 2540  |       |       |       |       |       |       |  |
| 23 | 102     |       |       |       |       |       |       |  |
| 24 | - 3     |       |       |       |       |       |       |  |

S = 19

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 48720   | 55106 | 65459 | 04487 | 07447 | 01341 | 71691 |  |
| 1  | 25072   | 58331 | 83210 | 80065 | 32490 | 14877 | 2194  |  |
| 2  | - 62651 | 03986 | 14256 | 50194 | 55493 | 31318 | 87    |  |
| 3  | 12582   | 36490 | 14292 | 59910 | 32369 | 43136 |       |  |
| 4  | 70522   | 50096 | 80405 | 73597 | 15244 | 9565  |       |  |
| 5  | - 39076 | 24444 | 46670 | 64496 | 14930 | 907   |       |  |
| 6  | 12463   | 70983 | 31861 | 56369 | 39093 | 95    |       |  |
| 7  | - 20404 | 64211 | 87028 | 56973 | 54334 |       |       |  |
| 8  | - 39535 | 21719 | 44808 | 72475 | 013   |       |       |  |
| 9  | 47377   | 49944 | 17296 | 68701 | 33    |       |       |  |
| 10 | - 22209 | 98836 | 67535 | 85995 | 1     |       |       |  |
| 11 | 70187   | 41602 | 94601 | 5860  |       |       |       |  |
| 12 | - 13749 | 46607 | 98458 | 244   |       |       |       |  |
| 13 | - 49159 | 94682 | 17380 |       |       |       |       |  |
| 14 | 19756   | 00405 | 30342 |       |       |       |       |  |
| 15 | - 11254 | 89939 | 8799  |       |       |       |       |  |
| 16 | 43936   | 96712 | 03    |       |       |       |       |  |
| 17 | - 13028 | 88836 | 7     |       |       |       |       |  |
| 18 | 26306   | 4149  |       |       |       |       |       |  |
| 19 | - 33666 | 3     |       |       |       |       |       |  |
| 20 | - 30108 | 3     |       |       |       |       |       |  |
| 21 | 19297   |       |       |       |       |       |       |  |
| 22 | - 848   |       |       |       |       |       |       |  |
| 23 | 30      |       |       |       |       |       |       |  |

S = 20

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 48782   | 75391 | 14022 | 43657 | 35804 | 59681 | 21257 |
| 1  | 23872   | 42526 | 57610 | 19839 | 03981 | 36959 | 0845  |
| 2  | - 56812 | 68663 | 10104 | 57704 | 11409 | 25802 | 66    |
| 3  | 10444   | 71424 | 54122 | 74076 | 28708 | 67596 |       |
| 4  | 58245   | 85052 | 85903 | 84298 | 13271 | 6452  |       |
| 5  | - 30608 | 48939 | 28780 | 53258 | 55703 | 344   |       |
| 6  | 92195   | 33884 | 01832 | 20934 | 01405 | 7     |       |
| 7  | - 13905 | 10431 | 54936 | 69837 | 22196 |       |       |
| 8  | - 29332 | 75121 | 88738 | 38986 | 910   |       |       |
| 9  | 31193   | 06370 | 31373 | 43716 | 77    |       |       |
| 10 | - 13624 | 74043 | 26546 | 95653 | 5     |       |       |
| 11 | 39886   | 04491 | 87406 | 4572  |       |       |       |
| 12 | - 69148 | 46119 | 85242 | 89    |       |       |       |
| 13 | - 56908 | 81708 | 42077 |       |       |       |       |
| 14 | 10882   | 74450 | 45609 |       |       |       |       |
| 15 | - 55536 | 84208 | 229   |       |       |       |       |
| 16 | 19751   | 24939 | 25    |       |       |       |       |
| 17 | - 52466 | 28991 |       |       |       |       |       |
| 18 | 86201   | 081   |       |       |       |       |       |
| 19 | 76774   | 6     |       |       |       |       |       |
| 20 | - 14086 | 6     |       |       |       |       |       |
| 21 | 7508    |       |       |       |       |       |       |
| 22 | - 292   |       |       |       |       |       |       |
| 23 | 9       |       |       |       |       |       |       |

S = 21

| I  | C SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 48839   | 19475 | 71404 | 47552 | 31501 | 35649 | 35086 |
| 1  | 22782   | 14172 | 22652 | 05847 | 69514 | 71132 | 8907  |
| 2  | - 51754 | 58035 | 68013 | 73826 | 85516 | 18204 | 26    |
| 3  | 87431   | 19053 | 49551 | 49404 | 81500 | 0563  |       |
| 4  | 48531   | 80209 | 74598 | 88281 | 89657 | 7486  |       |
| 5  | - 24250 | 89838 | 43187 | 05563 | 64756 | 802   |       |
| 6  | 69178   | 36150 | 79134 | 03179 | 82848 | 9     |       |
| 7  | - 96451 | 07774 | 40996 | 24325 | 7352  |       |       |
| 8  | - 21835 | 89794 | 08012 | 51622 | 817   |       |       |
| 9  | 20905   | 00406 | 75194 | 49575 | 21    |       |       |
| 10 | - 85432 | 37952 | 62951 | 23239 |       |       |       |
| 11 | 23247   | 97883 | 62431 | 9315  |       |       |       |
| 12 | - 35616 | 52406 | 32347 | 58    |       |       |       |
| 13 | - 46380 | 11420 | 84688 |       |       |       |       |
| 14 | 60840   | 98249 | 6494  |       |       |       |       |
| 15 | - 28145 | 44726 | 811   |       |       |       |       |
| 16 | 91642   | 50365 | 6     |       |       |       |       |
| 17 | - 21809 | 14502 |       |       |       |       |       |
| 18 | 27889   | 148   |       |       |       |       |       |
| 19 | 65104   | 0     |       |       |       |       |       |
| 20 | - 64583 |       |       |       |       |       |       |
| 21 | 2979    |       |       |       |       |       |       |
| 22 | - 103   |       |       |       |       |       |       |
| 23 | 2       |       |       |       |       |       |       |

S = 22

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 48890   | 63824 | 01013 | 70811 | 10240 | 30677 | 98415 |  |
| 1  | 21787   | 27933 | 39477 | 96928 | 20912 | 35012 | 8404  |  |
| 2  | - 47343 | 54147 | 67594 | 12362 | 94037 | 18070 | 38    |  |
| 3  | 73748   | 99301 | 01811 | 58449 | 88931 | 5194  |       |  |
| 4  | 40763   | 62537 | 30972 | 74680 | 12025 | 4429  |       |  |
| 5  | - 19414 | 50081 | 12261 | 45884 | 51718 | 591   |       |  |
| 6  | 52586   | 23435 | 69467 | 69131 | 76022 | 0     |       |  |
| 7  | - 67989 | 75184 | 46012 | 76072 | 0995  |       |       |  |
| 8  | - 16340 | 40555 | 90873 | 38306 | 904   |       |       |  |
| 9  | 14241   | 60045 | 14929 | 13342 | 18    |       |       |  |
| 10 | - 54655 | 17108 | 25570 | 29398 |       |       |       |  |
| 11 | 13867   | 85083 | 46536 | 7377  |       |       |       |  |
| 12 | - 18730 | 28959 | 01328 | 46    |       |       |       |  |
| 13 | - 33839 | 38040 | 06395 |       |       |       |       |  |
| 14 | 34571   | 24673 | 9561  |       |       |       |       |  |
| 15 | - 14628 | 84120 | 464   |       |       |       |       |  |
| 16 | 43786   | 06802 | 9     |       |       |       |       |  |
| 17 | - 93259 | 5606  |       |       |       |       |       |  |
| 18 | 85622   | 75    |       |       |       |       |       |  |
| 19 | 40796   | 9     |       |       |       |       |       |  |
| 20 | - 29619 |       |       |       |       |       |       |  |
| 21 | 1210    |       |       |       |       |       |       |  |
| 22 | - 37    |       |       |       |       |       |       |  |



S = 23

I

O SUB I

|    |         |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 48937   | 71949 | 97679 | 96182 | 63063 | 66974 | 33126 |
| 1  | 20875   | 81689 | 61957 | 83087 | 32694 | 13415 | 6155  |
| 2  | - 43473 | 65774 | 86325 | 49479 | 29537 | 55138 | 03    |
| 3  | 62645   | 47441 | 76273 | 34832 | 80980 | 0902  |       |
| 4  | 34491   | 21107 | 40401 | 56787 | 73745 | 1750  |       |
| 5  | - 15690 | 98179 | 60855 | 91376 | 75223 | 029   |       |
| 6  | 40450   | 85002 | 88727 | 94714 | 38292 | 5     |       |
| 7  | - 48639 | 30600 | 36247 | 88188 | 5443  |       |       |
| 8  | - 12304 | 86643 | 14317 | 23410 | 503   |       |       |
| 9  | 98503   | 56809 | 39946 | 97888 | 6     |       |       |
| 10 | - 35616 | 36011 | 51517 | 09886 |       |       |       |
| 11 | 84501   | 79144 | 99761 | 707   |       |       |       |
| 12 | - 10027 | 17907 | 41881 | 77    |       |       |       |
| 13 | - 23563 | 92066 | 38956 |       |       |       |       |
| 14 | 19975   | 55793 | 7851  |       |       |       |       |
| 15 | - 77867 | 77303 | 71    |       |       |       |       |
| 16 | 21497   | 51668 | 0     |       |       |       |       |
| 17 | - 40889 | 7148  |       |       |       |       |       |
| 18 | 22582   | 35    |       |       |       |       |       |
| 19 | 23262   | 2     |       |       |       |       |       |
| 20 | - 13719 |       |       |       |       |       |       |
| 21 | 503     |       |       |       |       |       |       |
| 22 | - 14    |       |       |       |       |       |       |

S = 24

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 48980   | 97047 | 00699 | 63996 | 57190 | 50851 | 42793 |  |
| 1  | 20037   | 67378 | 83556 | 88537 | 45840 | 21972 | 4033  |  |
| 2  | - 40059 | 84522 | 83795 | 44533 | 11403 | 70800 | 55    |  |
| 3  | 53558   | 02078 | 30687 | 37021 | 32988 | 5773  |       |  |
| 4  | 29381   | 50003 | 88282 | 57233 | 07910 | 5337  |       |  |
| 5  | - 12792 | 64774 | 01219 | 88768 | 15905 | 845   |       |  |
| 6  | 31456   | 52369 | 60087 | 85243 | 16699 | 9     |       |  |
| 7  | - 35270 | 87980 | 18535 | 04876 | 9956  |       |       |  |
| 8  | - 93291 | 32755 | 99694 | 90863 | 92    |       |       |  |
| 9  | 69095   | 64905 | 31960 | 06533 | 4     |       |       |  |
| 10 | - 23607 | 67426 | 43340 | 87349 |       |       |       |  |
| 11 | 52508   | 09341 | 09859 | 196   |       |       |       |  |
| 12 | - 54487 | 00437 | 84766 | 8     |       |       |       |  |
| 13 | - 16070 | 22389 | 72097 |       |       |       |       |  |
| 14 | 11735   | 80391 | 8724  |       |       |       |       |  |
| 15 | - 42387 | 36058 | 61    |       |       |       |       |  |
| 16 | 10824   | 50647 | 8     |       |       |       |       |  |
| 17 | - 18322 | 8948  |       |       |       |       |       |  |
| 18 | 31417   | 0     |       |       |       |       |       |  |
| 19 | 12793   | 0     |       |       |       |       |       |  |
| 20 | - 6448  |       |       |       |       |       |       |  |
| 21 | 214     |       |       |       |       |       |       |  |
| 22 | - 5     |       |       |       |       |       |       |  |

S = 25

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49020   | 84001 | 67093 | 74833 | 06617 | 04568 | 88525 |  |
| 1  | 19264   | 33312 | 40610 | 46505 | 02201 | 01239 | 0429  |  |
| 2  | - 37033 | 11683 | 63234 | 86260 | 75750 | 41468 | 11    |  |
| 3  | 46062   | 33491 | 70968 | 81197 | 71359 | 7532  |       |  |
| 4  | 25184   | 91909 | 10949 | 44475 | 13206 | 0606  |       |  |
| 5  | - 10513 | 76877 | 46532 | 97638 | 74178 | 444   |       |  |
| 6  | 24708   | 46786 | 03171 | 35903 | 43905 | 4     |       |  |
| 7  | - 25898 | 19484 | 58388 | 39738 | 7375  |       |       |  |
| 8  | - 71227 | 93459 | 10234 | 52065 | 30    |       |       |  |
| 9  | 49104   | 69413 | 55010 | 76682 | 0     |       |       |  |
| 10 | - 15895 | 98111 | 05806 | 40144 |       |       |       |  |
| 11 | 33223   | 38846 | 84439 | 164   |       |       |       |  |
| 12 | - 29963 | 68087 | 68841 | 5     |       |       |       |  |
| 13 | - 10869 | 23986 | 38096 |       |       |       |       |  |
| 14 | 70079   | 41995 | 356   |       |       |       |       |  |
| 15 | - 23564 | 52757 | 43    |       |       |       |       |  |
| 16 | 55798   | 52263 |       |       |       |       |       |  |
| 17 | - 83638 | 396   |       |       |       |       |       |  |
| 18 | - 19762 | 6     |       |       |       |       |       |  |
| 19 | 69489   |       |       |       |       |       |       |  |
| 20 | - 3082  |       |       |       |       |       |       |  |
| 21 | 93      |       |       |       |       |       |       |  |
| 22 | - 2     |       |       |       |       |       |       |  |

S = 26

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49057   | 70953 | 76837 | 24045 | 56530 | 93919 | 28473 |
| 1  | 18548   | 54952 | 50145 | 41388 | 47605 | 04088 | 5929  |
| 2  | - 34337 | 05965 | 31443 | 95197 | 84435 | 78681 | 42    |
| 3  | 39834   | 85979 | 78554 | 44682 | 69763 | 3987  |       |
| 4  | 21712   | 27632 | 17165 | 92820 | 92798 | 1719  |       |
| 5  | - 87052 | 13196 | 74549 | 15774 | 76426 | 00    |       |
| 6  | 19588   | 46789 | 61603 | 61287 | 65367 | 8     |       |
| 7  | - 19237 | 05632 | 76854 | 29116 | 5972  |       |       |
| 8  | - 54766 | 68167 | 76209 | 75558 | 20    |       |       |
| 9  | 35324   | 71907 | 84476 | 13089 | 9     |       |       |
| 10 | - 10860 | 66732 | 66206 | 66865 |       |       |       |
| 11 | 21376   | 84454 | 64190 | 706   |       |       |       |
| 12 | - 16622 | 52046 | 29926 | 4     |       |       |       |
| 13 | - 73404 | 07876 | 7505  |       |       |       |       |
| 14 | 42510   | 37764 | 080   |       |       |       |       |
| 15 | - 13362 | 03745 | 92    |       |       |       |       |
| 16 | 29398   | 61577 |       |       |       |       |       |
| 17 | - 38756 | 065   |       |       |       |       |       |
| 18 | - 26612 | 9     |       |       |       |       |       |
| 19 | 37712   |       |       |       |       |       |       |
| 20 | - 1500  |       |       |       |       |       |       |
| 21 | 41      |       |       |       |       |       |       |

S = 27

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49091   | 90517 | 61210 | 76504 | 23300 | 48626 | 79272 |  |
| 1  | 17884   | 12012 | 88557 | 99914 | 06348 | 22229 | 7667  |  |
| 2  | - 31925 | 18032 | 89313 | 75868 | 76679 | 09977 | 26    |  |
| 3  | 34626   | 31806 | 39436 | 44185 | 33716 | 3674  |       |  |
| 4  | 18818   | 61344 | 80719 | 54428 | 22464 | 3849  |       |  |
| 5  | - 72575 | 13795 | 52498 | 34788 | 12332 | 19    |       |  |
| 6  | 15663   | 14318 | 65844 | 69747 | 49159 | 6     |       |  |
| 7  | - 14443 | 08585 | 35872 | 07248 | 3532  |       |       |  |
| 8  | - 42403 | 44093 | 01332 | 39164 | 02    |       |       |  |
| 9  | 25701   | 87163 | 03607 | 40121 | 4     |       |       |  |
| 10 | - 75217 | 12243 | 62147 | 1020  |       |       |       |  |
| 11 | 13970   | 46459 | 45063 | 765   |       |       |       |  |
| 12 | - 92686 | 84792 | 18714 |       |       |       |       |  |
| 13 | - 49690 | 01150 | 3836  |       |       |       |       |  |
| 14 | 26179   | 05764 | 895   |       |       |       |       |  |
| 15 | - 77190 | 38177 | 6     |       |       |       |       |  |
| 16 | 15807   | 99370 |       |       |       |       |       |  |
| 17 | - 18160 | 067   |       |       |       |       |       |  |
| 18 | - 21824 | 1     |       |       |       |       |       |  |
| 19 | 20574   |       |       |       |       |       |       |  |
| 20 | - 743   |       |       |       |       |       |       |  |
| 21 | 19      |       |       |       |       |       |       |  |

S = 28

| I  | D SUE I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49123   | 70747 | 35576 | 15773 | 27964 | 69603 | 77968 |  |
| 1  | 17265   | 70340 | 98582 | 41106 | 00760 | 39556 | 0662  |  |
| 2  | - 29758 | 88233 | 62998 | 29967 | 41147 | 32618 | 90    |  |
| 3  | 30242   | 82754 | 29356 | 71709 | 99123 | 1873  |       |  |
| 4  | 16391   | 76178 | 49413 | 67960 | 02975 | 5454  |       |  |
| 5  | - 60893 | 82172 | 40912 | 85634 | 89520 | 21    |       |  |
| 6  | 12624   | 57795 | 93163 | 56399 | 94178 | 6     |       |  |
| 7  | - 10952 | 37540 | 78649 | 97192 | 5940  |       |       |  |
| 8  | - 33054 | 83324 | 29865 | 84751 | 94    |       |       |  |
| 9  | 18899   | 96215 | 34293 | 22217 | 1     |       |       |  |
| 10 | - 52755 | 60012 | 99419 | 0030  |       |       |       |  |
| 11 | 92636   | 87113 | 34749 | 38    |       |       |       |  |
| 12 | - 51717 | 77090 | 12968 |       |       |       |       |  |
| 13 | - 33794 | 14631 | 6818  |       |       |       |       |  |
| 14 | 16356   | 14610 | 386   |       |       |       |       |  |
| 15 | - 45378 | 71261 | 8     |       |       |       |       |  |
| 16 | 86633   | 0584  |       |       |       |       |       |  |
| 17 | - 85655 | 23    |       |       |       |       |       |  |
| 18 | - 15543 | 2     |       |       |       |       |       |  |
| 19 | 11321   |       |       |       |       |       |       |  |
| 20 | - 375   |       |       |       |       |       |       |  |
| 21 | 8       |       |       |       |       |       |       |  |

S = 29

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49153   | 35906 | 82622 | 69545 | 38436 | 74775 | 95667 |  |
| 1  | 16688   | 67454 | 77942 | 75853 | 96402 | 24763 | 3520  |  |
| 2  | - 27805 | 90878 | 49437 | 37387 | 61884 | 18190 | 24    |  |
| 3  | 26532   | 25537 | 79300 | 79768 | 65967 | 4851  |       |  |
| 4  | 14344   | 12646 | 09793 | 65040 | 74094 | 5539  |       |  |
| 5  | - 51398 | 03174 | 59596 | 41437 | 91700 | 36    |       |  |
| 6  | 10251   | 25842 | 59720 | 78428 | 63098 | 0     |       |  |
| 7  | - 83828 | 44902 | 66099 | 30445 | 684   |       |       |  |
| 8  | - 25937 | 62686 | 08427 | 85941 | 28    |       |       |  |
| 9  | 14037   | 06378 | 21906 | 41882 | 7     |       |       |  |
| 10 | - 37441 | 35810 | 89187 | 3202  |       |       |       |  |
| 11 | 62265   | 37196 | 94196 | 25    |       |       |       |  |
| 12 | - 28711 | 22376 | 12574 |       |       |       |       |  |
| 13 | - 23122 | 29180 | 0266  |       |       |       |       |  |
| 14 | 10360   | 65577 | 661   |       |       |       |       |  |
| 15 | - 27120 | 45897 | 1     |       |       |       |       |  |
| 16 | 48329   | 0652  |       |       |       |       |       |  |
| 17 | - 40431 | 98    |       |       |       |       |       |  |
| 18 | - 10425 | 5     |       |       |       |       |       |  |
| 19 | 6295    |       |       |       |       |       |       |  |
| 20 | - 192   |       |       |       |       |       |       |  |
| 21 | 4       |       |       |       |       |       |       |  |

S = 30

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49181   | 07088 | 53420 | 89338 | 89345 | 05311 | 50074 |  |
| 1  | 16149   | 00901 | 67674 | 00628 | 15653 | 55212 | 7172  |  |
| 2  | - 26039 | 13219 | 36091 | 73527 | 38488 | 77663 | 33    |  |
| 3  | 23374   | 24334 | 20925 | 95400 | 25403 | 3235  |       |  |
| 4  | 12606   | 71731 | 36543 | 87372 | 95497 | 6029  |       |  |
| 5  | - 43625 | 19063 | 38593 | 96397 | 43195 | 62    |       |  |
| 6  | 83819   | 73345 | 53115 | 57616 | 37667 |       |       |  |
| 7  | - 64721 | 10298 | 29812 | 05337 | 674   |       |       |  |
| 8  | - 20482 | 77782 | 40761 | 15293 | 60    |       |       |  |
| 9  | 10523   | 14819 | 11431 | 19543 | 7     |       |       |  |
| 10 | - 26868 | 24952 | 54884 | 0165  |       |       |       |  |
| 11 | 42386   | 03016 | 48580 | 41    |       |       |       |  |
| 12 | - 15728 | 25658 | 40129 |       |       |       |       |  |
| 13 | - 15928 | 87125 | 5066  |       |       |       |       |  |
| 14 | 66495   | 08848 | 14    |       |       |       |       |  |
| 15 | - 16462 | 22612 | 3     |       |       |       |       |  |
| 16 | 27412   | 9696  |       |       |       |       |       |  |
| 17 | - 18946 | 92    |       |       |       |       |       |  |
| 18 | - 67951 |       |       |       |       |       |       |  |
| 19 | 3541    |       |       |       |       |       |       |  |
| 20 | - 100   |       |       |       |       |       |       |  |
| 21 | 2       |       |       |       |       |       |       |  |



S = 31

| I  | C SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49207   | 02715 | 23966 | 78460 | 78455 | 01975 | 89199 |
| 1  | 15643   | 18816 | 77487 | 97606 | 29483 | 24020 | 4179  |
| 2  | - 24435 | 60556 | 85426 | 69257 | 82674 | 29616 | 65    |
| 3  | 20672   | 83811 | 78880 | 15069 | 56636 | 9418  |       |
| 4  | 11124   | 76364 | 66162 | 91261 | 36317 | 9987  |       |
| 5  | - 37221 | 32139 | 76215 | 16570 | 64104 | 32    |       |
| 6  | 68981   | 25649 | 30212 | 55215 | 07713 |       |       |
| 7  | - 50377 | 13169 | 18409 | 64723 | 089   |       |       |
| 8  | - 16274 | 50737 | 53380 | 36228 | 70    |       |       |
| 9  | 79584   | 25438 | 80797 | 29133 |       |       |       |
| 10 | - 19482 | 08444 | 35835 | 9588  |       |       |       |
| 11 | 29199   | 20644 | 42526 | 85    |       |       |       |
| 12 | - 83927 | 35758 | 0950  |       |       |       |       |
| 13 | - 11053 | 40752 | 7400  |       |       |       |       |
| 14 | 43212   | 99715 | 97    |       |       |       |       |
| 15 | - 10140 | 24720 | 4     |       |       |       |       |
| 16 | 15793   | 2418  |       |       |       |       |       |
| 17 | - 87066 | 6     |       |       |       |       |       |
| 18 | - 43691 |       |       |       |       |       |       |
| 19 | 2016    |       |       |       |       |       |       |
| 20 | - 53    |       |       |       |       |       |       |
| 21 | 1       |       |       |       |       |       |       |

S = 32

| I  | O SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49231   | 38949 | 26733 | 08677 | 70146 | 52381 | 51439 |  |
| 1  | 15168   | 12210 | 15711 | 43861 | 50350 | 24523 | 4412  |  |
| 2  | - 22975 | 81221 | 92845 | 89256 | 74056 | 79384 | 32    |  |
| 3  | 18350   | 99152 | 35422 | 91466 | 20253 | 8234  |       |  |
| 4  | 98544   | 59057 | 39146 | 06992 | 13992 | 374   |       |  |
| 5  | - 31913 | 18358 | 95307 | 27900 | 14743 | 87    |       |  |
| 6  | 57115   | 84308 | 91941 | 69745 | 64505 |       |       |  |
| 7  | - 39512 | 78839 | 54157 | 51922 | 282   |       |       |  |
| 8  | - 13007 | 17047 | 97896 | 89086 | 28    |       |       |  |
| 9  | 60687   | 49392 | 70853 | 18136 |       |       |       |  |
| 10 | - 14264 | 93063 | 65002 | 5144  |       |       |       |  |
| 11 | 20341   | 40510 | 31500 | 28    |       |       |       |  |
| 12 | - 42624 | 46445 | 7908  |       |       |       |       |  |
| 13 | - 77278 | 05819 | 211   |       |       |       |       |  |
| 14 | 28418   | 43447 | 35    |       |       |       |       |  |
| 15 | - 63332 | 60403 |       |       |       |       |       |  |
| 16 | 92328   | 072   |       |       |       |       |       |  |
| 17 | - 38404 | 5     |       |       |       |       |       |  |
| 18 | - 27941 |       |       |       |       |       |       |  |
| 19 | 1162    |       |       |       |       |       |       |  |
| 20 | - 28    |       |       |       |       |       |       |  |

S = 33

| I  | O SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49254   | 30028 | 77475 | 04929 | 96365 | 49918 | 96206 |  |
| 1  | 14721   | 08624 | 52238 | 53438 | 31337 | 48402 | 5023  |  |
| 2  | - 21643 | 06811 | 21813 | 69986 | 06446 | 84937 | 09    |  |
| 3  | 16346   | 41766 | 27841 | 67740 | 24618 | 8693  |       |  |
| 4  | 87605   | 21634 | 18285 | 00213 | 15873 | 356   |       |  |
| 5  | - 27488 | 13232 | 56029 | 99284 | 14037 | 90    |       |  |
| 6  | 47562   | 37122 | 36742 | 55598 | 89017 |       |       |  |
| 7  | - 31214 | 87924 | 74965 | 68302 | 468   |       |       |  |
| 8  | - 10454 | 66792 | 12518 | 18623 | 40    |       |       |  |
| 9  | 46640   | 02146 | 30456 | 30257 |       |       |       |  |
| 10 | - 10541 | 33005 | 41959 | 6191  |       |       |       |  |
| 11 | 14320   | 85828 | 61581 | 35    |       |       |       |  |
| 12 | - 19599 | 18401 | 7255  |       |       |       |       |  |
| 13 | - 54436 | 57372 | 066   |       |       |       |       |  |
| 14 | 18901   | 59360 | 11    |       |       |       |       |  |
| 15 | - 40077 | 58688 |       |       |       |       |       |  |
| 16 | 54721   | 078   |       |       |       |       |       |  |
| 17 | - 15554 | 3     |       |       |       |       |       |  |
| 18 | - 17858 |       |       |       |       |       |       |  |
| 19 | 677     |       |       |       |       |       |       |  |
| 20 | - 15    |       |       |       |       |       |       |  |

S = 34

| I  | D SUB I |       |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|-------|
| 0  |         | 49275 | 88545 | 73978 | 09362 | 47214 | 88152 | 28354 |
| 1  |         | 14299 | 66887 | 08450 | 87467 | 94994 | 21642 | 6541  |
| 2  | -       | 20423 | 04230 | 62182 | 53616 | 18741 | 45746 | 25    |
| 3  |         | 14608 | 44474 | 31139 | 92154 | 96595 | 0798  |       |
| 4  |         | 78143 | 48647 | 01708 | 39338 | 52771 | 737   |       |
| 5  | -       | 23779 | 40921 | 19331 | 87633 | 13228 | 07    |       |
| 6  |         | 39820 | 48412 | 80414 | 88812 | 52417 |       |       |
| 7  | -       | 24827 | 07214 | 17577 | 71529 | 194   |       |       |
| 8  | -       | 84486 | 79419 | 26381 | 84208 | 5     |       |       |
| 9  |         | 36109 | 30329 | 92887 | 17764 |       |       |       |
| 10 | -       | 78575 | 42722 | 40787 | 801   |       |       |       |
| 11 |         | 10183 | 00668 | 02152 | 47    |       |       |       |
| 12 | -       | 70137 | 48023 | 245   |       |       |       |       |
| 13 | -       | 38635 | 08997 | 983   |       |       |       |       |
| 14 |         | 12707 | 91411 | 40    |       |       |       |       |
| 15 | -       | 25678 | 62613 |       |       |       |       |       |
| 16 |         | 32852 | 841   |       |       |       |       |       |
| 17 | -       | 51023 |       |       |       |       |       |       |
| 18 | -       | 11441 |       |       |       |       |       |       |
| 19 |         | 400   |       |       |       |       |       |       |
| 20 | -       | 8     |       |       |       |       |       |       |

S = 35

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49296   | 25677 | 11893 | 21354 | 25690 | 27815 | 65169 |
| 1  | 13901   | 72741 | 49796 | 87810 | 72585 | 28002 | 1448  |
| 2  | - 19303 | 36953 | 31483 | 16135 | 50428 | 84930 | 96    |
| 3  | 13095   | 60297 | 52836 | 96962 | 09126 | 8158  |       |
| 4  | 69926   | 08962 | 55598 | 87220 | 62311 | 728   |       |
| 5  | - 20655 | 29610 | 84087 | 85981 | 45931 | 22    |       |
| 6  | 33508   | 33119 | 63164 | 74342 | 94522 |       |       |
| 7  | - 19873 | 04981 | 87769 | 23284 | 459   |       |       |
| 8  | - 68631 | 03762 | 69089 | 33275 | 5     |       |       |
| 9  | 28151   | 94523 | 35621 | 64750 |       |       |       |
| 10 | - 59052 | 22851 | 43684 | 783   |       |       |       |
| 11 | 73091   | 01749 | 24590 | 5     |       |       |       |
| 12 | - 37804 | 32187 | 91    |       |       |       |       |
| 13 | - 27623 | 75515 | 096   |       |       |       |       |
| 14 | 86318   | 95187 | 7     |       |       |       |       |
| 15 | - 16647 | 94006 |       |       |       |       |       |
| 16 | 19964   | 224   |       |       |       |       |       |
| 17 | - 5657  |       |       |       |       |       |       |
| 18 | - 7360  |       |       |       |       |       |       |
| 19 | 239     |       |       |       |       |       |       |
| 20 | - 4     |       |       |       |       |       |       |

S = 36

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49315   | 51378 | 12711 | 32670 | 85595 | 20989 | 86310 |  |
| 1  | 13525   | 35192 | 22763 | 95924 | 48243 | 61415 | 0385  |  |
| 2  | - 18273 | 33522 | 38304 | 79309 | 66882 | 07424 | 31    |  |
| 3  | 11773   | 76207 | 61823 | 56361 | 11936 | 1755  |       |  |
| 4  | 62761   | 60734 | 66180 | 57146 | 39652 | 437   |       |  |
| 5  | - 18011 | 04444 | 22300 | 09676 | 23370 | 89    |       |  |
| 6  | 28332   | 20632 | 61775 | 42215 | 27327 |       |       |  |
| 7  | - 16003 | 96210 | 45470 | 65545 | 336   |       |       |  |
| 8  | - 56028 | 78032 | 27840 | 59036 | 3     |       |       |  |
| 9  | 22093   | 67797 | 03197 | 37169 |       |       |       |  |
| 10 | - 44725 | 29396 | 48613 | 534   |       |       |       |  |
| 11 | 52931   | 50338 | 11400 | 9     |       |       |       |  |
| 12 | 28920   | 47523 | 875   |       |       |       |       |  |
| 13 | - 19894 | 23747 | 601   |       |       |       |       |  |
| 14 | 59208   | 70272 | 4     |       |       |       |       |  |
| 15 | - 10914 | 66042 |       |       |       |       |       |  |
| 16 | 12270   | 972   |       |       |       |       |       |  |
| 17 | 11955   |       |       |       |       |       |       |  |
| 18 | - 4761  |       |       |       |       |       |       |  |
| 19 | 144     |       |       |       |       |       |       |  |
| 20 | - 2     |       |       |       |       |       |       |  |

S = 37

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49333   | 74544 | 68640 | 54336 | 30974 | 48250 | 68827 |
| 1  | 13168   | 83429 | 30490 | 69100 | 09148 | 67922 | 4751  |
| 2  | - 17323 | 61789 | 77431 | 27053 | 81899 | 57236 | 03    |
| 3  | 10614   | 68260 | 31093 | 36617 | 78396 | 8075  |       |
| 4  | 56492   | 12913 | 38387 | 59208 | 47932 | 469   |       |
| 5  | - 15762 | 81830 | 83747 | 24085 | 87460 | 68    |       |
| 6  | 24064   | 52314 | 83217 | 36705 | 64824 |       |       |
| 7  | - 12962 | 09981 | 18329 | 18715 | 063   |       |       |
| 8  | - 45958 | 98353 | 27451 | 07275 | 0     |       |       |
| 9  | 17448   | 22644 | 24004 | 56903 |       |       |       |
| 10 | - 34124 | 12386 | 94639 | 562   |       |       |       |
| 11 | 38656   | 72615 | 33109 | 8     |       |       |       |
| 12 | 42866   | 41606 | 639   |       |       |       |       |
| 13 | - 14429 | 05018 | 706   |       |       |       |       |
| 14 | 40993   | 62679 | 4     |       |       |       |       |
| 15 | - 72323 | 8816  |       |       |       |       |       |
| 16 | 76235   | 58    |       |       |       |       |       |
| 17 | 16980   |       |       |       |       |       |       |
| 18 | - 3098  |       |       |       |       |       |       |
| 19 | 88      |       |       |       |       |       |       |
| 20 | - 1     |       |       |       |       |       |       |

S = 38

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49351   | 03150 | 63191 | 75028 | 28147 | 22519 | 81083 |
| 1  | 12830   | 64228 | 68022 | 62674 | 79077 | 96634 | 9194  |
| 2  | - 16446 | 07727 | 65273 | 98943 | 75192 | 26773 | 40    |
| 3  | 95948   | 81368 | 69608 | 81480 | 69474 | 535   |       |
| 4  | 50986   | 71012 | 98683 | 24456 | 77286 | 650   |       |
| 5  | - 13843 | 11211 | 05138 | 30219 | 80775 | 30    |       |
| 6  | 20527   | 69221 | 87816 | 00219 | 95114 |       |       |
| 7  | - 10555 | 52283 | 27739 | 25748 | 496   |       |       |
| 8  | - 37871 | 47703 | 28689 | 34882 | 5     |       |       |
| 9  | 13861   | 88781 | 95019 | 13347 |       |       |       |
| 10 | - 26217 | 94147 | 57893 | 511   |       |       |       |
| 11 | 28458   | 38817 | 53211 | 9     |       |       |       |
| 12 | 46639   | 07540 | 912   |       |       |       |       |
| 13 | - 10537 | 28635 | 244   |       |       |       |       |
| 14 | 28636   | 12584 | 7     |       |       |       |       |
| 15 | - 48411 | 9357  |       |       |       |       |       |
| 16 | 47842   | 20    |       |       |       |       |       |
| 17 | 16665   |       |       |       |       |       |       |
| 18 | - 2030  |       |       |       |       |       |       |
| 19 | 54      |       |       |       |       |       |       |



S = 39

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49367   | 44364 | 13464 | 39962 | 11770 | 88932 | 41816 |
| 1  | 12509   | 39744 | 47207 | 53302 | 70704 | 93643 | 7727  |
| 2  | - 15633 | 57907 | 40373 | 73375 | 89691 | 31662 | 30    |
| 3  | 86947   | 37022 | 81511 | 85426 | 22995 | 743   |       |
| 4  | 46136   | 23206 | 92464 | 16100 | 55883 | 243   |       |
| 5  | - 12197 | 25727 | 21959 | 11171 | 98587 | 06    |       |
| 6  | 17582   | 21693 | 74283 | 77719 | 93608 |       |       |
| 7  | - 86401 | 65925 | 63150 | 38477 | 11    |       |       |
| 8  | - 31344 | 02483 | 33889 | 04398 | 5     |       |       |
| 9  | 11075   | 29364 | 60879 | 81044 |       |       |       |
| 10 | - 20277 | 47470 | 33589 | 008   |       |       |       |
| 11 | 21110   | 45244 | 05935 | 5     |       |       |       |
| 12 | 45153   | 38296 | 380   |       |       |       |       |
| 13 | - 77465 | 99457 | 88    |       |       |       |       |
| 14 | 20174   | 65581 | 0     |       |       |       |       |
| 15 | - 32720 | 1348  |       |       |       |       |       |
| 16 | 30309   | 35    |       |       |       |       |       |
| 17 | 14396   |       |       |       |       |       |       |
| 18 | - 1339  |       |       |       |       |       |       |
| 19 | 34      |       |       |       |       |       |       |

S = 40

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49383   | 04646 | 92299 | 41629 | 21854 | 62791 | 97367 |  |
| 1  | 12203   | 85625 | 84210 | 40689 | 65145 | 01811 | 3279  |  |
| 2  | - 14879 | 84938 | 11764 | 83143 | 22971 | 25256 | 55    |  |
| 3  | 78977   | 80589 | 37438 | 52891 | 95709 | 686   |       |  |
| 4  | 41849   | 34074 | 78978 | 29418 | 02900 | 806   |       |  |
| 5  | - 10780 | 73992 | 18547 | 26236 | 70599 | 84    |       |  |
| 6  | 15117   | 83266 | 12386 | 07083 | 76003 |       |       |  |
| 7  | - 71071 | 01564 | 82342 | 75665 | 26    |       |       |  |
| 8  | - 26050 | 74675 | 31057 | 57474 | 7     |       |       |  |
| 9  | 88967   | 77786 | 63156 | 0599  |       |       |       |  |
| 10 | - 15782 | 20424 | 17235 | 449   |       |       |       |  |
| 11 | 15773   | 45909 | 84875 | 6     |       |       |       |  |
| 12 | 41191   | 99652 | 846   |       |       |       |       |  |
| 13 | - 57318 | 34742 | 31    |       |       |       |       |  |
| 14 | 14329   | 43991 | 7     |       |       |       |       |  |
| 15 | - 22319 | 0792  |       |       |       |       |       |  |
| 16 | 19373   | 33    |       |       |       |       |       |  |
| 17 | 11691   |       |       |       |       |       |       |  |
| 18 | - 889   |       |       |       |       |       |       |  |
| 19 | 21      |       |       |       |       |       |       |  |

S = 41

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49397   | 89839 | 19627 | 91929 | 83778 | 95087 | 59562 |
| 1  | 11912   | 89404 | 11322 | 34620 | 25858 | 86782 | 4946  |
| 2  | - 14179 | 35306 | 61254 | 77729 | 71864 | 25507 | 06    |
| 3  | 71901   | 29399 | 55465 | 24564 | 12905 | 261   |       |
| 4  | 38049   | 21507 | 39706 | 05100 | 38579 | 628   |       |
| 5  | - 95571 | 27163 | 19963 | 93686 | 82016 | 6     |       |
| 6  | 13046   | 86009 | 09359 | 55066 | 44829 |       |       |
| 7  | - 58733 | 94076 | 66828 | 65272 | 95    |       |       |
| 8  | - 21738 | 75475 | 12460 | 29192 | 0     |       |       |
| 9  | 71836   | 60312 | 28852 | 3004  |       |       |       |
| 10 | - 12357 | 48651 | 10575 | 015   |       |       |       |
| 11 | 11867   | 24717 | 17668 | 3     |       |       |       |
| 12 | 36298   | 28696 | 090   |       |       |       |       |
| 13 | - 42676 | 15723 | 58    |       |       |       |       |
| 14 | 10257   | 23991 | 0     |       |       |       |       |
| 15 | - 15358 | 7343  |       |       |       |       |       |
| 16 | 12486   | 93    |       |       |       |       |       |
| 17 | 9172    |       |       |       |       |       |       |
| 18 | - 595   |       |       |       |       |       |       |
| 19 | 13      |       |       |       |       |       |       |

S = 42

| I  | D SUB I |       |       |       |       |       |       |    |
|----|---------|-------|-------|-------|-------|-------|-------|----|
| 0  | 49412   | 05232 | 58039 | 58297 | 88036 | 16906 | 96863 |    |
| 1  | 11635   | 49105 | 92075 | 14942 | 34720 | 24711 | 0135  |    |
| 2  | -       | 13527 | 19176 | 68699 | 37606 | 23378 | 92930 | 61 |
| 3  | 65600   | 32912 | 92411 | 28602 | 34178 | 612   |       |    |
| 4  | 34670   | 98271 | 81833 | 97489 | 63839 | 809   |       |    |
| 5  | -       | 84964 | 53418 | 45784 | 93799 | 46381 | 6     |    |
| 6  | 11299   | 18305 | 30527 | 34690 | 68356 |       |       |    |
| 7  | -       | 48754 | 77800 | 94297 | 88972 | 57    |       |    |
| 8  | -       | 18210 | 76608 | 43644 | 87816 | 1     |       |    |
| 9  | 58289   | 81477 | 74571 | 8152  |       |       |       |    |
| 10 | -       | 97315 | 15327 | 36799 | 43    |       |       |    |
| 11 | 89872   | 83500 | 92754 |       |       |       |       |    |
| 12 | 31298   | 26804 | 924   |       |       |       |       |    |
| 13 | -       | 31966 | 55931 | 97    |       |       |       |    |
| 14 | 73971   | 79021 |       |       |       |       |       |    |
| 15 | -       | 10658 | 1950  |       |       |       |       |    |
| 16 | 81115   | 1     |       |       |       |       |       |    |
| 17 | 7050    |       |       |       |       |       |       |    |
| 18 | -       | 401   |       |       |       |       |       |    |
| 19 | 8       |       |       |       |       |       |       |    |

S = 43

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49425   | 55633 | 04492 | 13999 | 42738 | 65654 | 14962 |  |
| 1  | 11370   | 72056 | 26715 | 72363 | 01413 | 89684 | 5987  |  |
| 2  | - 12919 | 01794 | 89230 | 45333 | 39993 | 86989 | 37    |  |
| 3  | 59975   | 06372 | 59164 | 95249 | 16230 | 046   |       |  |
| 4  | 31659   | 64167 | 22541 | 40291 | 95354 | 210   |       |  |
| 5  | - 75739 | 57008 | 52590 | 21490 | 63684 | 2     |       |  |
| 6  | 98184   | 27251 | 53033 | 29287 | 1793  |       |       |  |
| 7  | - 40643 | 24761 | 77096 | 74261 | 98    |       |       |  |
| 8  | - 15312 | 09015 | 31375 | 36118 | 2     |       |       |  |
| 9  | 47520   | 21755 | 60337 | 4809  |       |       |       |  |
| 10 | - 77055 | 90812 | 62702 | 63    |       |       |       |  |
| 11 | 68490   | 98810 | 05070 |       |       |       |       |  |
| 12 | 26606   | 38665 | 730   |       |       |       |       |  |
| 13 | - 24084 | 46797 | 64    |       |       |       |       |  |
| 14 | 53727   | 99590 |       |       |       |       |       |  |
| 15 | - 74559 | 476   |       |       |       |       |       |  |
| 16 | 53078   | 6     |       |       |       |       |       |  |
| 17 | 5351    |       |       |       |       |       |       |  |
| 18 | - 272   |       |       |       |       |       |       |  |
| 19 | 5       |       |       |       |       |       |       |  |

S = 44

| I  |   | D SUB I |       |       |       |       |       |       |
|----|---|---------|-------|-------|-------|-------|-------|-------|
| 0  |   | 49438   | 45415 | 35673 | 77365 | 82549 | 78154 | 77461 |
| 1  |   | 11117   | 73841 | 80632 | 01833 | 00742 | 03856 | 7361  |
| 2  | - | 12350   | 96219 | 98672 | 00833 | 16264 | 87799 | 47    |
| 3  |   | 54940   | 33811 | 06669 | 67664 | 27088 | 178   |       |
| 4  |   | 28968   | 37998 | 93769 | 08896 | 48012 | 450   |       |
| 5  | - | 67690   | 85131 | 00017 | 34758 | 33920 | 0     |       |
| 6  |   | 85590   | 33530 | 78976 | 38333 | 6713  |       |       |
| 7  | - | 34018   | 91676 | 37384 | 81842 | 75    |       |       |
| 8  | - | 12920   | 83424 | 48024 | 23847 | 3     |       |       |
| 9  |   | 38914   | 74487 | 25953 | 9219  |       |       |       |
| 10 | - | 61334   | 00322 | 61662 | 12    |       |       |       |
| 11 |   | 52510   | 31425 | 19071 |       |       |       |       |
| 12 |   | 22404   | 69057 | 405   |       |       |       |       |
| 13 | - | 18248   | 31327 | 95    |       |       |       |       |
| 14 |   | 39292   | 21567 |       |       |       |       |       |
| 15 | - | 52561   | 135   |       |       |       |       |       |
| 16 |   | 34969   | 9     |       |       |       |       |       |
| 17 |   | 4031    |       |       |       |       |       |       |
| 18 | - | 185     |       |       |       |       |       |       |
| 19 |   | 3       |       |       |       |       |       |       |

S = 45

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49450   | 78570 | 36907 | 99318 | 19648 | 88641 | 14051 |  |
| 1  | 10875   | 77409 | 86887 | 10961 | 18768 | 46619 | 8629  |  |
| 2  | - 11819 | 57148 | 05556 | 56137 | 53022 | 81440 | 01    |  |
| 3  | 50423   | 26115 | 23522 | 97912 | 99191 | 764   |       |  |
| 4  | 26557   | 21069 | 34976 | 92116 | 68612 | 876   |       |  |
| 5  | - 60647 | 05823 | 96052 | 20665 | 10469 | 2     |       |  |
| 6  | 74840   | 02103 | 20673 | 84099 | 3683  |       |       |  |
| 7  | - 28584 | 88846 | 72519 | 89385 | 88    |       |       |  |
| 8  | - 10940 | 49166 | 49417 | 92154 | 7     |       |       |  |
| 9  | 32004   | 92227 | 28914 | 9063  |       |       |       |  |
| 10 | - 49064 | 58529 | 45803 | 97    |       |       |       |  |
| 11 | 40490   | 15624 | 43161 |       |       |       |       |  |
| 12 | 18747   | 50141 | 321   |       |       |       |       |  |
| 13 | - 13901 | 74994 | 00    |       |       |       |       |  |
| 14 | 28924   | 34796 |       |       |       |       |       |  |
| 15 | - 37327 | 608   |       |       |       |       |       |  |
| 16 | 23185   | 2     |       |       |       |       |       |  |
| 17 | 3024    |       |       |       |       |       |       |  |
| 18 | - 127   |       |       |       |       |       |       |  |
| 19 | 2       |       |       |       |       |       |       |  |

S = 46

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49462   | 58746 | 22200 | 39962 | 45665 | 46520 | 16470 |
| 1  | 10644   | 12282 | 92776 | 08814 | 29672 | 70105 | 8162  |
| 2  | - 11321 | 75648 | 54387 | 20358 | 83491 | 94802 | 72    |
| 3  | 46361   | 23034 | 17955 | 10924 | 06931 | 840   |       |
| 4  | 24391   | 85749 | 72244 | 77262 | 17859 | 503   |       |
| 5  | - 54464 | 80519 | 59398 | 89140 | 81570 | 4     |       |
| 6  | 65631   | 43451 | 62888 | 53886 | 2101  |       |       |
| 7  | - 24108 | 18389 | 50500 | 50543 | 68    |       |       |
| 8  | - 92943 | 02919 | 62116 | 09430 |       |       |       |
| 9  | 26430   | 66926 | 58102 | 7935  |       |       |       |
| 10 | - 39437 | 93746 | 06156 | 45    |       |       |       |
| 11 | 31393   | 70170 | 76867 |       |       |       |       |
| 12 | 15622   | 14851 | 032   |       |       |       |       |
| 13 | - 10646 | 25080 | 15    |       |       |       |       |
| 14 | 21426   | 85678 |       |       |       |       |       |
| 15 | - 26697 | 363   |       |       |       |       |       |
| 16 | 15461   | 8     |       |       |       |       |       |
| 17 | 2263    |       |       |       |       |       |       |
| 18 | - 88    |       |       |       |       |       |       |
| 19 | 1       |       |       |       |       |       |       |



S = 47

| I  | D SUE I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49473   | 89284 | 34949 | 04933 | 10736 | 35143 | 77827 |  |
| 1  | 10422   | 13871 | 60175 | 90553 | 42087 | 89872 | 7192  |  |
| 2  | - 10854 | 74660 | 77692 | 49026 | 52430 | 73834 | 71    |  |
| 3  | 42700   | 30434 | 25907 | 55331 | 65971 | 874   |       |  |
| 4  | 22442   | 84113 | 94070 | 04485 | 57060 | 720   |       |  |
| 5  | - 49023 | 61909 | 84060 | 53998 | 06996 | 2     |       |  |
| 6  | 57717   | 14304 | 55176 | 56135 | 6448  |       |       |  |
| 7  | - 20405 | 01958 | 68361 | 34151 | 21    |       |       |  |
| 8  | - 79209 | 43622 | 07010 | 84240 |       |       |       |  |
| 9  | 21913   | 66742 | 41792 | 2489  |       |       |       |  |
| 10 | - 31845 | 86168 | 71180 | 02    |       |       |       |  |
| 11 | 24469   | 49331 | 52061 |       |       |       |       |  |
| 12 | 12983   | 77278 | 830   |       |       |       |       |  |
| 13 | - 81945 | 80754 | 7     |       |       |       |       |  |
| 14 | 15969   | 23825 |       |       |       |       |       |  |
| 15 | - 19224 | 556   |       |       |       |       |       |  |
| 16 | 10366   | 5     |       |       |       |       |       |  |
| 17 | 1692    |       |       |       |       |       |       |  |
| 18 | - 61    |       |       |       |       |       |       |  |
| 19 | 1       |       |       |       |       |       |       |  |

S = 48

| I  | C SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49484   | 73251 | 04108 | 63314 | 25400 | 28085 | 51368 |  |
| 1  | 10209   | 22872 | 06596 | 73529 | 20881 | 95116 | 9855  |  |
| 2  | - 10416 | 05127 | 92825 | 01697 | 85170 | 43294 | 71    |  |
| 3  | 39393   | 85962 | 49934 | 78434 | 64889 | 454   |       |  |
| 4  | 20684   | 72698 | 67150 | 31812 | 15363 | 324   |       |  |
| 5  | - 44221 | 90134 | 62640 | 01802 | 17782 | 3     |       |  |
| 6  | 50893   | 48063 | 38352 | 88362 | 3188  |       |       |  |
| 7  | - 17329 | 68912 | 54809 | 47943 | 93    |       |       |  |
| 8  | - 67712 | 10412 | 69644 | 02498 |       |       |       |  |
| 9  | 18237   | 63850 | 52222 | 4707  |       |       |       |  |
| 10 | - 25828 | 74651 | 65789 | 48    |       |       |       |  |
| 11 | 19169   | 19824 | 82605 |       |       |       |       |  |
| 12 | 10774   | 85872 | 578   |       |       |       |       |  |
| 13 | - 63384 | 77411 | 5     |       |       |       |       |  |
| 14 | 11971   | 25594 |       |       |       |       |       |  |
| 15 | - 13934 | 074   |       |       |       |       |       |  |
| 16 | 69841   |       |       |       |       |       |       |  |
| 17 | 1266    |       |       |       |       |       |       |  |
| 18 | - 43    |       |       |       |       |       |       |  |

S = 49

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49495   | 13465 | 18539 | 13594 | 73493 | 15978 | 46159 |
| 1  | 10004   | 84736 | 00870 | 26836 | 51230 | 33430 | 7069  |
| 2  | - 10003 | 42667 | 34866 | 84223 | 57719 | 75909 | 39    |
| 3  | 36401   | 47711 | 62252 | 12149 | 76122 | 733   |       |
| 4  | 19095   | 50287 | 44448 | 63769 | 49147 | 362   |       |
| 5  | - 39973 | 66522 | 60827 | 57807 | 11543 | 0     |       |
| 6  | 44992   | 11709 | 36838 | 06078 | 2956  |       |       |
| 7  | - 14766 | 11653 | 65067 | 04752 | 23    |       |       |
| 8  | - 58054 | 61501 | 49899 | 87550 |       |       |       |
| 9  | 15233   | 64813 | 32785 | 9573  |       |       |       |
| 10 | - 21037 | 24080 | 74980 | 17    |       |       |       |
| 11 | 15090   | 10038 | 37998 |       |       |       |       |
| 12 | 89358   | 18959 | 70    |       |       |       |       |
| 13 | - 49260 | 59205 | 7     |       |       |       |       |
| 14 | 90246   | 3137  |       |       |       |       |       |
| 15 | - 10163 | 060   |       |       |       |       |       |
| 16 | 47258   |       |       |       |       |       |       |
| 17 | 948     |       |       |       |       |       |       |
| 18 | - 30    |       |       |       |       |       |       |

S = 50

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49505   | 12522 | 72354 | 23803 | 22919 | 86150 | 73791 |  |
| 1  | 98084   | 92031 | 41983 | 72152 | 86925 | 78264 | 128   |  |
| 2  | - 96148 | 46938 | 55729 | 08880 | 99823 | 14262 | 2     |  |
| 3  | 33688   | 01591 | 12780 | 50789 | 59122 | 169   |       |  |
| 4  | 17656   | 06260 | 47908 | 91552 | 12240 | 346   |       |  |
| 5  | - 36205 | 88810 | 41646 | 23634 | 89820 | 2     |       |  |
| 6  | 39873   | 37887 | 74582 | 70125 | 8507  |       |       |  |
| 7  | - 12621 | 40259 | 45488 | 24719 | 32    |       |       |  |
| 8  | - 49916 | 30668 | 07038 | 16711 |       |       |       |  |
| 9  | 12769   | 08855 | 01918 | 1305  |       |       |       |  |
| 10 | - 17204 | 31643 | 64487 | 75    |       |       |       |  |
| 11 | 11934   | 58453 | 88439 |       |       |       |       |  |
| 12 | 74103   | 87893 | 66    |       |       |       |       |  |
| 13 | - 38459 | 35741 | 7     |       |       |       |       |  |
| 14 | 68401   | 0970  |       |       |       |       |       |  |
| 15 | - 74574 | 84    |       |       |       |       |       |  |
| 16 | 32099   |       |       |       |       |       |       |  |
| 17 | 712     |       |       |       |       |       |       |  |
| 18 | - 21    |       |       |       |       |       |       |  |

S = 51

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49514   | 72818 | 25898 | 13068 | 09560 | 07561 | 79637 |  |
| 1  | 96196   | 98878 | 16085 | 34708 | 28531 | 63049 | 866   |  |
| 2  | - 92484 | 79268 | 95654 | 07267 | 74331 | 80273 | 3     |  |
| 3  | 31222   | 83975 | 32289 | 54671 | 86293 | 290   |       |  |
| 4  | 16349   | 77553 | 09057 | 77814 | 91414 | 070   |       |  |
| 5  | - 32856 | 35333 | 50116 | 67609 | 62969 | 0     |       |  |
| 6  | 35420   | 93217 | 33794 | 87774 | 7291  |       |       |  |
| 7  | - 10820 | 86670 | 50478 | 51175 | 92    |       |       |  |
| 8  | - 43036 | 79178 | 00286 | 31994 |       |       |       |  |
| 9  | 10739   | 37171 | 22575 | 7170  |       |       |       |  |
| 10 | - 14124 | 77242 | 87447 | 09    |       |       |       |  |
| 11 | 94813   | 89334 | 7438  |       |       |       |       |  |
| 12 | 61480   | 52572 | 55    |       |       |       |       |  |
| 13 | - 30159 | 64620 | 2     |       |       |       |       |  |
| 14 | 52114   | 0594  |       |       |       |       |       |  |
| 15 | - 55040 | 73    |       |       |       |       |       |  |
| 16 | 21874   |       |       |       |       |       |       |  |
| 17 | 535     |       |       |       |       |       |       |  |
| 18 | - 15    |       |       |       |       |       |       |  |

S = 52

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49523   | 96564 | 20193 | 11734 | 91231 | 66810 | 53519 |
| 1  | 94380   | 39125 | 68731 | 47936 | 85836 | 49898 | 094   |
| 2  | - 89026 | 62241 | 24282 | 58584 | 17449 | 79763 | 0     |
| 3  | 28979   | 16878 | 40839 | 07796 | 59745 | 788   |       |
| 4  | 15162   | 12657 | 12598 | 68874 | 75059 | 191   |       |
| 5  | - 29871 | 88406 | 83200 | 44194 | 15577 | 1     |       |
| 6  | 31537   | 53081 | 88141 | 92824 | 5711  |       |       |
| 7  | - 93042 | 17669 | 91199 | 95596 | 2     |       |       |
| 8  | - 37203 | 83699 | 58339 | 03970 |       |       |       |
| 9  | 90616   | 31195 | 96007 | 301   |       |       |       |
| 10 | - 11040 | 10501 | 68073 | 95    |       |       |       |
| 11 | 25650   | 71154 | 9127  |       |       |       |       |
| 12 | 51048   | 37308 | 66    |       |       |       |       |
| 13 | - 23752 | 49128 | 2     |       |       |       |       |
| 14 | 39904   | 6823  |       |       |       |       |       |
| 15 | - 40851 | 48    |       |       |       |       |       |
| 16 | 14945   |       |       |       |       |       |       |
| 17 | 403     |       |       |       |       |       |       |
| 18 | - 11    |       |       |       |       |       |       |

S = 53

| I  | D SUE I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49532   | 85807 | 77053 | 21910 | 52304 | 52043 | 43741 |
| 1  | 92631   | 15825 | 05414 | 83106 | 42514 | 43262 | 668   |
| 2  | - 85758 | 86934 | 50708 | 93380 | 03377 | 47720 | 9     |
| 3  | 26933   | 53441 | 71797 | 30260 | 66468 | 675   |       |
| 4  | 14080   | 41407 | 52659 | 79771 | 60691 | 719   |       |
| 5  | - 27206 | 89207 | 06667 | 36794 | 58202 | 8     |       |
| 6  | 28141   | 60066 | 12995 | 28396 | 5362  |       |       |
| 7  | - 80225 | 81312 | 92315 | 28671 | 7     |       |       |
| 8  | - 32243 | 83213 | 20477 | 46605 |       |       |       |
| 9  | 76699   | 21642 | 23718 | 567   |       |       |       |
| 10 | - 96272 | 73576 | 23056 | 6     |       |       |       |
| 11 | 60612   | 37727 | 9703  |       |       |       |       |
| 12 | 42432   | 14043 | 05    |       |       |       |       |
| 13 | - 18784 | 09874 | 2     |       |       |       |       |
| 14 | 30703   | 8610  |       |       |       |       |       |
| 15 | - 30484 | 28    |       |       |       |       |       |
| 16 | 10232   |       |       |       |       |       |       |
| 17 | 305     |       |       |       |       |       |       |
| 18 | - 8     |       |       |       |       |       |       |

S = 54

| I  | O SUB I |       |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|-------|
| 0  |         | 49541 | 42446 | 12342 | 44439 | 43329 | 24995 | 41189 |
| 1  |         | 90945 | 60952 | 98166 | 20246 | 66522 | 20727 | 762   |
| 2  | -       | 82667 | 80433 | 71440 | 60682 | 62626 | 22188 | 9     |
| 3  |         | 25065 | 31941 | 61525 | 16160 | 36042 | 171   |       |
| 4  |         | 13093 | 49538 | 95350 | 52966 | 47601 | 969   |       |
| 5  | -       | 24822 | 18084 | 36301 | 65921 | 69563 | 3     |       |
| 6  |         | 25164 | 48410 | 29568 | 27290 | 1099  |       |       |
| 7  | -       | 69361 | 81980 | 64248 | 84049 | 5     |       |       |
| 8  | -       | 28014 | 26449 | 63916 | 05055 |       |       |       |
| 9  |         | 65115 | 40859 | 09649 | 325   |       |       |       |
| 10 | -       | 79903 | 07889 | 78660 | 6     |       |       |       |
| 11 |         | 48758 | 63405 | 8935  |       |       |       |       |
| 12 |         | 35315 | 84710 | 69    |       |       |       |       |
| 13 | -       | 14914 | 61237 | 5     |       |       |       |       |
| 14 |         | 23735 | 0020  |       |       |       |       |       |
| 15 | -       | 22866 | 83    |       |       |       |       |       |
| 16 |         | 7014  |       |       |       |       |       |       |
| 17 |         | 231   |       |       |       |       |       |       |
| 18 | -       | 5     |       |       |       |       |       |       |



S = 55

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49549   | 68239 | 85903 | 10595 | 08390 | 42362 | 44933 |
| 1  | 89320   | 32823 | 37236 | 05500 | 55595 | 70933 | 244   |
| 2  | - 79740 | 91378 | 27882 | 16202 | 29037 | 98115 | 0     |
| 3  | 23356   | 36863 | 13923 | 56505 | 78175 | 960   |       |
| 4  | 12191   | 57189 | 98347 | 51204 | 11260 | 432   |       |
| 5  | - 22683 | 95486 | 69705 | 33013 | 69457 | 1     |       |
| 6  | 22548   | 20809 | 22080 | 25758 | 9832  |       |       |
| 7  | - 60125 | 25595 | 63648 | 22195 | 1     |       |       |
| 8  | - 24397 | 75265 | 94709 | 65249 |       |       |       |
| 9  | 55441   | 98093 | 49360 | 295   |       |       |       |
| 10 | - 66540 | 09108 | 62064 | 9     |       |       |       |
| 11 | 39375   | 11049 | 0744  |       |       |       |       |
| 12 | 29435   | 89465 | 85    |       |       |       |       |
| 13 | - 11888 | 26854 | 0     |       |       |       |       |
| 14 | 18430   | 7638  |       |       |       |       |       |
| 15 | - 17239 | 29    |       |       |       |       |       |
| 16 | 4809    |       |       |       |       |       |       |
| 17 | 176     |       |       |       |       |       |       |
| 18 | - 4     |       |       |       |       |       |       |

S = 56

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49557   | 64825 | 08354 | 76174 | 83595 | 82536 | 77354 |  |
| 1  | 87752   | 13771 | 98904 | 16915 | 42453 | 96045 | 908   |  |
| 2  | - 76966 | 77271 | 09905 | 96958 | 76986 | 89930 | 4     |  |
| 3  | 21790   | 65853 | 23560 | 72080 | 61529 | 802   |       |  |
| 4  | 11366   | 00685 | 76759 | 06320 | 38824 | 032   |       |  |
| 5  | - 20762 | 99658 | 12587 | 41361 | 02253 | 3     |       |  |
| 6  | 20243   | 66897 | 41747 | 81048 | 1294  |       |       |  |
| 7  | - 52249 | 69334 | 12433 | 24683 | 1     |       |       |  |
| 8  | - 21297 | 29795 | 35501 | 18504 |       |       |       |  |
| 9  | 47338   | 23397 | 06618 | 124   |       |       |       |  |
| 10 | - 55591 | 91851 | 73980 | 4     |       |       |       |  |
| 11 | 31916   | 36697 | 1806  |       |       |       |       |  |
| 12 | 24573   | 78732 | 93    |       |       |       |       |  |
| 13 | - 95116 | 80423 |       |       |       |       |       |  |
| 14 | 14374   | 3834  |       |       |       |       |       |  |
| 15 | - 13059 | 96    |       |       |       |       |       |  |
| 16 | 3296    |       |       |       |       |       |       |  |
| 17 | 134     |       |       |       |       |       |       |  |
| 18 | - 3     |       |       |       |       |       |       |  |

S = 57

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49565   | 33724 | 22158 | 94662 | 21015 | 33591 | 55724 |  |
| 1  | 86238   | 08081 | 23487 | 07676 | 03165 | 01001 | 659   |  |
| 2  | - 74334 | 93307 | 13092 | 33709 | 94206 | 57200 | 0     |  |
| 3  | 20354   | 01582 | 88397 | 53117 | 44351 | 115   |       |  |
| 4  | 10609   | 17052 | 74058 | 46634 | 34335 | 423   |       |  |
| 5  | - 19033 | 98039 | 24381 | 17206 | 42994 | 1     |       |  |
| 6  | 18209   | 15072 | 24878 | 58770 | 1907  |       |       |  |
| 7  | - 45515 | 90760 | 89303 | 18043 | 3     |       |       |  |
| 8  | - 18632 | 49081 | 82569 | 68224 |       |       |       |  |
| 9  | 40528   | 65149 | 36938 | 588   |       |       |       |  |
| 10 | - 46590 | 74858 | 45530 | 8     |       |       |       |  |
| 11 | 25963   | 95856 | 5351  |       |       |       |       |  |
| 12 | 20549   | 21132 | 37    |       |       |       |       |  |
| 13 | - 76379 | 55786 |       |       |       |       |       |  |
| 14 | 11258   | 0769  |       |       |       |       |       |  |
| 15 | - 99403 | 7     |       |       |       |       |       |  |
| 16 | 2255    |       |       |       |       |       |       |  |
| 17 | 102     |       |       |       |       |       |       |  |
| 18 | - 2     |       |       |       |       |       |       |  |

S = 58

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49572   | 76355 | 71970 | 23810 | 77461 | 77165 | 80088 |  |
| 1  | 84775   | 40116 | 47220 | 79913 | 12246 | 78228 | 758   |  |
| 2  | - 71835 | 82517 | 04417 | 95977 | 79283 | 21511 | 6     |  |
| 3  | 19033   | 87720 | 88854 | 42893 | 20425 | 770   |       |  |
| 4  | 99143   | 08175 | 18494 | 14670 | 27997 | 24    |       |  |
| 5  | - 17474 | 89901 | 66574 | 05494 | 75310 | 0     |       |  |
| 6  | 16409   | 11088 | 04607 | 05095 | 7674  |       |       |  |
| 7  | - 39742 | 89976 | 04237 | 44327 | 7     |       |       |  |
| 8  | - 16336 | 46883 | 28869 | 28735 |       |       |       |  |
| 9  | 34789   | 61085 | 55989 | 494   |       |       |       |  |
| 10 | - 39165 | 28537 | 16686 | 3     |       |       |       |  |
| 11 | 21195   | 38715 | 6310  |       |       |       |       |  |
| 12 | 17213   | 80167 | 04    |       |       |       |       |  |
| 13 | - 61550 | 22839 |       |       |       |       |       |  |
| 14 | 88533   | 689   |       |       |       |       |       |  |
| 15 | - 76003 | 6     |       |       |       |       |       |  |
| 16 | 1537    |       |       |       |       |       |       |  |
| 17 | 79      |       |       |       |       |       |       |  |
| 18 | - 1     |       |       |       |       |       |       |  |

S = 59

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49579   | 94042 | 77278 | 10361 | 54153 | 43247 | 20610 |  |
| 1  | 83361   | 52649 | 13646 | 68925 | 68840 | 17692 | 007   |  |
| 2  | - 69460 | 67051 | 94990 | 40260 | 49664 | 97708 | 4     |  |
| 3  | 17819   | 08362 | 27656 | 83616 | 16696 | 661   |       |  |
| 4  | 92754   | 27215 | 91743 | 26265 | 68739 | 89    |       |  |
| 5  | - 16066 | 58225 | 54556 | 58069 | 45608 | 7     |       |  |
| 6  | 14813   | 18232 | 24276 | 78880 | 3461  |       |       |  |
| 7  | - 34780 | 73877 | 53673 | 72142 | 4     |       |       |  |
| 8  | - 14353 | 46878 | 53964 | 26019 |       |       |       |  |
| 9  | 29938   | 96439 | 46484 | 962   |       |       |       |  |
| 10 | - 33019 | 66093 | 79518 | 9     |       |       |       |  |
| 11 | 17360   | 99496 | 5044  |       |       |       |       |  |
| 12 | 14445   | 71061 | 55    |       |       |       |       |  |
| 13 | - 49770 | 07349 |       |       |       |       |       |  |
| 14 | 69898   | 100   |       |       |       |       |       |  |
| 15 | - 58367 | 7     |       |       |       |       |       |  |
| 16 | 1043    |       |       |       |       |       |       |  |
| 17 | 60      |       |       |       |       |       |       |  |
| 18 | - 1     |       |       |       |       |       |       |  |

S = 60

| I  | D SUB I |       |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|-------|
| 0  |         | 49586 | 88021 | 18627 | 25795 | 93574 | 40548 | 26755 |
| 1  |         | 81994 | 05345 | 15549 | 94396 | 92574 | 53015 | 790   |
| 2  | -       | 67201 | 40460 | 66892 | 16309 | 30285 | 64659 | 9     |
| 3  |         | 16699 | 70367 | 95554 | 56252 | 54222 | 922   |       |
| 4  |         | 86872 | 00477 | 49008 | 37212 | 96480 | 29    |       |
| 5  | -       | 14792 | 29207 | 95943 | 96639 | 84621 | 7     |       |
| 6  |         | 13395 | 34966 | 43296 | 04527 | 4857  |       |       |
| 7  | -       | 30504 | 83371 | 27723 | 26383 | 9     |       |       |
| 8  | -       | 12636 | 84995 | 13847 | 84592 |       |       |       |
| 9  |         | 25827 | 83790 | 44081 | 084   |       |       |       |
| 10 | -       | 27917 | 20326 | 04189 | 6     |       |       |       |
| 11 |         | 14266 | 68117 | 3494  |       |       |       |       |
| 12 |         | 12144 | 97498 | 07    |       |       |       |       |
| 13 | -       | 40378 | 33244 |       |       |       |       |       |
| 14 |         | 55396 | 254   |       |       |       |       |       |
| 15 | -       | 45015 | 0     |       |       |       |       |       |
| 16 |         | 702   |       |       |       |       |       |       |
| 17 |         | 47    |       |       |       |       |       |       |

S = 61

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49593   | 59446 | 47238 | 33101 | 33833 | 53720 | 53011 |
| 1  | 80670   | 73399 | 96541 | 13778 | 07152 | 62429 | 586   |
| 2  | - 65050 | 60832 | 41573 | 47130 | 01026 | 28741 | 2     |
| 3  | 15666   | 88164 | 84858 | 01177 | 63833 | 131   |       |
| 4  | 81448   | 83064 | 31085 | 40403 | 72528 | 55    |       |
| 5  | - 13637 | 38091 | 94199 | 41905 | 84868 | 1     |       |
| 6  | 12133   | 26752 | 47579 | 97820 | 5663  |       |       |
| 7  | - 26811 | 33249 | 32113 | 91787 | 3     |       |       |
| 8  | - 11147 | 49251 | 31795 | 25803 |       |       |       |
| 9  | 22334   | 14851 | 55627 | 127   |       |       |       |
| 10 | - 23667 | 88683 | 83776 | 5     |       |       |       |
| 11 | 11760   | 91095 | 6421  |       |       |       |       |
| 12 | 10229   | 62212 | 68    |       |       |       |       |
| 13 | - 32864 | 51443 |       |       |       |       |       |
| 14 | 44065   | 822   |       |       |       |       |       |
| 15 | - 34860 | 2     |       |       |       |       |       |
| 16 | 467     |       |       |       |       |       |       |
| 17 | 36      |       |       |       |       |       |       |

S = 62

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49600   | 09400 | 26595 | 45093 | 92446 | 28423 | 97040 |
| 1  | 79389   | 46303 | 79575 | 74066 | 89844 | 80419 | 894   |
| 2  | - 63001 | 44695 | 80274 | 11086 | 05955 | 47331 | 8     |
| 3  | 14712   | 70631 | 35062 | 79401 | 54046 | 602   |       |
| 4  | 76442   | 40728 | 27246 | 06678 | 05595 | 42    |       |
| 5  | - 12589 | 00247 | 59639 | 99965 | 82356 | 2     |       |
| 6  | 11007   | 69440 | 52334 | 09789 | 6081  |       |       |
| 7  | - 23613 | 41226 | 17780 | 81399 | 4     |       |       |
| 8  | - 98524 | 95691 | 50528 | 8987  |       |       |       |
| 9  | 19357   | 46168 | 58798 | 055   |       |       |       |
| 10 | - 20118 | 58876 | 61472 | 8     |       |       |       |
| 11 | 97249   | 04716 | 830   |       |       |       |       |
| 12 | 86324   | 29796 | 4     |       |       |       |       |
| 13 | - 26832 | 66646 |       |       |       |       |       |
| 14 | 35178   | 749   |       |       |       |       |       |
| 15 | - 27104 | 1     |       |       |       |       |       |
| 16 | 306     |       |       |       |       |       |       |
| 17 | 28      |       |       |       |       |       |       |



S = 63

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49606   | 38896 | 13489 | 76077 | 25049 | 28941 | 86984 |  |
| 1  | 78148   | 26722 | 94318 | 70541 | 78134 | 44536 | 071   |  |
| 2  | - 61047 | 61580 | 30240 | 50743 | 27175 | 62447 | 8     |  |
| 3  | 13830   | 09754 | 93698 | 07043 | 87561 | 313   |       |  |
| 4  | 71814   | 88003 | 90738 | 22582 | 40535 | 81    |       |  |
| 5  | - 11635 | 86630 | 78778 | 97172 | 62031 | 0     |       |  |
| 6  | 10002   | 02113 | 17872 | 40814 | 3028  |       |       |  |
| 7  | - 20838 | 27801 | 92242 | 23566 | 4     |       |       |  |
| 8  | - 87241 | 16150 | 30996 | 6826  |       |       |       |  |
| 9  | 16814   | 89536 | 69853 | 017   |       |       |       |  |
| 10 | - 17145 | 49165 | 56050 | 4     |       |       |       |  |
| 11 | 80651   | 95123 | 940   |       |       |       |       |  |
| 12 | 72982   | 49232 | 5     |       |       |       |       |  |
| 13 | - 21974 | 49619 |       |       |       |       |       |  |
| 14 | 28181   | 802   |       |       |       |       |       |  |
| 15 | - 21155 | 3     |       |       |       |       |       |  |
| 16 | 196     |       |       |       |       |       |       |  |
| 17 | 22      |       |       |       |       |       |       |  |

S = 64

| I  | D SUE I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49612   | 48884 | 85080 | 41646 | 72305 | 04740 | 31839 |  |
| 1  | 76945   | 29484 | 51464 | 46575 | 21807 | 08151 | 909   |  |
| 2  | - 59183 | 29159 | 21055 | 83937 | 20432 | 54481 | 3     |  |
| 3  | 13012   | 70799 | 73353 | 05472 | 83773 | 093   |       |  |
| 4  | 67532   | 34650 | 69151 | 45176 | 96867 | 96    |       |  |
| 5  | - 10768 | 02901 | 39838 | 75858 | 80318 | 6     |       |  |
| 6  | 91018   | 76891 | 24416 | 75609 | 054   |       |       |  |
| 7  | - 18424 | 72600 | 48495 | 63372 | 4     |       |       |  |
| 8  | - 77388 | 99666 | 15360 | 7939  |       |       |       |  |
| 9  | 14637   | 84629 | 43984 | 891   |       |       |       |  |
| 10 | - 14648 | 13657 | 25749 | 9     |       |       |       |  |
| 11 | 67079   | 55495 | 778   |       |       |       |       |  |
| 12 | 61818   | 04753 | 4     |       |       |       |       |  |
| 13 | - 18049 | 06934 |       |       |       |       |       |  |
| 14 | 22652   | 798   |       |       |       |       |       |  |
| 15 | - 16574 | 2     |       |       |       |       |       |  |
| 16 | 121     |       |       |       |       |       |       |  |
| 17 | 17      |       |       |       |       |       |       |  |

S = 65

| I  | D SUB I |       |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|-------|
| 0  |         | 49618 | 40259 | 17734 | 38239 | 92045 | 13120 | 68322 |
| 1  |         | 75778 | 80653 | 64234 | 02175 | 66211 | 20041 | 822   |
| 2  | -       | 57403 | 08904 | 11746 | 20024 | 06306 | 79450 | 2     |
| 3  |         | 12254 | 83763 | 91422 | 92720 | 27903 | 113   |       |
| 4  |         | 63564 | 39181 | 13549 | 99064 | 10653 | 90    |       |
| 5  | -       | 99767 | 16097 | 08703 | 96394 | 59533 |       |       |
| 6  |         | 82947 | 99143 | 77082 | 89309 | 329   |       |       |
| 7  | -       | 16321 | 15902 | 71294 | 76965 | 9     |       |       |
| 8  | -       | 68769 | 68754 | 76497 | 5227  |       |       |       |
| 9  |         | 12769 | 36418 | 44796 | 304   |       |       |       |
| 10 | -       | 12544 | 74948 | 49264 | 0     |       |       |       |
| 11 |         | 55946 | 59439 | 001   |       |       |       |       |
| 12 |         | 52458 | 91301 | 1     |       |       |       |       |
| 13 | -       | 14867 | 41019 |       |       |       |       |       |
| 14 |         | 18268 | 231   |       |       |       |       |       |
| 15 | -       | 13032 | 5     |       |       |       |       |       |
| 16 |         | 70    |       |       |       |       |       |       |
| 17 |         | 13    |       |       |       |       |       |       |

S = 66

| I  | C SUE I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49624   | 13858 | 22714 | 24361 | 98150 | 36162 | 55147 |  |
| 1  | 74647   | 16693 | 48896 | 21806 | 55466 | 93197 | 679   |  |
| 2  | - 55702 | 02190 | 23137 | 75720 | 23103 | 01028 | 3     |  |
| 3  | 11551   | 35941 | 59240 | 98615 | 74185 | 564   |       |  |
| 4  | 59883   | 68447 | 99394 | 91343 | 35981 | 97    |       |  |
| 5  | - 92541 | 69622 | 29325 | 09746 | 86751 |       |       |  |
| 6  | 75699   | 56281 | 68163 | 52057 | 037   |       |       |  |
| 7  | - 14483 | 96473 | 97012 | 60734 | 1     |       |       |  |
| 8  | - 61214 | 36545 | 89251 | 4492  |       |       |       |  |
| 9  | 11162   | 03843 | 35896 | 354   |       |       |       |  |
| 10 | - 10768 | 55464 | 98251 | 7     |       |       |       |  |
| 11 | 46787   | 45473 | 664   |       |       |       |       |  |
| 12 | 44599   | 01465 | 1     |       |       |       |       |  |
| 13 | - 12280 | 77390 |       |       |       |       |       |  |
| 14 | 14779   | 217   |       |       |       |       |       |  |
| 15 | - 10283 | 8     |       |       |       |       |       |  |
| 16 | 37      |       |       |       |       |       |       |  |
| 17 | 10      |       |       |       |       |       |       |  |

S = 67

| I  | O SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49629   | 70471 | 43183 | 29836 | 25948 | 97318 | 18918 |  |
| 1  | 73548   | 83699 | 50320 | 78674 | 00036 | 25247 | 377   |  |
| 2  | - 54075 | 46799 | 87338 | 13681 | 73556 | 98099 | 5     |  |
| 3  | 10897   | 65432 | 75599 | 72886 | 01634 | 476   |       |  |
| 4  | 56465   | 62425 | 23728 | 97519 | 43511 | 65    |       |  |
| 5  | - 85935 | 17620 | 02524 | 06505 | 85255 |       |       |  |
| 6  | 69179   | 13974 | 65174 | 57101 | 796   |       |       |  |
| 7  | - 12876 | 18637 | 09184 | 05778 | 9     |       |       |  |
| 8  | - 54579 | 23170 | 25780 | 6584  |       |       |       |  |
| 9  | 97762   | 91670 | 08992 | 74    |       |       |       |  |
| 10 | - 92648 | 55884 | 23197 |       |       |       |       |  |
| 11 | 39230   | 43624 | 763   |       |       |       |       |  |
| 12 | 37986   | 23558 | 1     |       |       |       |       |  |
| 13 | - 10171 | 68032 |       |       |       |       |       |  |
| 14 | 11993   | 531   |       |       |       |       |       |  |
| 15 | - 81428 |       |       |       |       |       |       |  |
| 16 | 15      |       |       |       |       |       |       |  |
| 17 | 8       |       |       |       |       |       |       |  |

S = 68

| I  | D SUB I |       |       |       |       |       |       |
|----|---------|-------|-------|-------|-------|-------|-------|
| 0  | 49635   | 10842 | 16475 | 94918 | 65438 | 31833 | 18002 |
| 1  | 72482   | 36700 | 37804 | 17382 | 57903 | 27935 | 119   |
| 2  | - 52519 | 13778 | 28806 | 16108 | 69612 | 64546 | 2     |
| 3  | 10289   | 55468 | 83723 | 13760 | 39379 | 134   |       |
| 4  | 53288   | 03451 | 48096 | 62839 | 87307 | 32    |       |
| 5  | - 79886 | 61867 | 77820 | 53324 | 74087 |       |       |
| 6  | 63304   | 37802 | 96144 | 93127 | 282   |       |       |
| 7  | - 11466 | 42990 | 81551 | 26840 | 8     |       |       |
| 8  | - 48741 | 55633 | 33722 | 5678  |       |       |       |
| 9  | 85789   | 97415 | 01786 | 91    |       |       |       |
| 10 | - 79887 | 17578 | 37994 |       |       |       |       |
| 11 | 32977   | 82155 | 853   |       |       |       |       |
| 12 | 32412   | 61882 | 5     |       |       |       |       |
| 13 | - 84470 | 3292  |       |       |       |       |       |
| 14 | 97621   | 51    |       |       |       |       |       |
| 15 | - 64690 |       |       |       |       |       |       |
| 16 | 0       |       |       |       |       |       |       |
| 17 | 6       |       |       |       |       |       |       |

S = 69

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49640   | 35671 | 05127 | 56868 | 19801 | 53226 | 69037 |  |
| 1  | 71446   | 39019 | 02853 | 59145 | 01890 | 36155 | 664   |  |
| 2  | - 51029 | 04601 | 77183 | 27059 | 50537 | 24308 | 7     |  |
| 3  | 97232   | 94415 | 73007 | 69407 | 01689 | 19    |       |  |
| 4  | 50330   | 89316 | 27553 | 62370 | 98236 | 04    |       |  |
| 5  | - 74341 | 81245 | 14752 | 67315 | 95717 |       |       |  |
| 6  | 58003   | 26118 | 40254 | 16821 | 919   |       |       |  |
| 7  | - 10227 | 96302 | 34221 | 42705 | 7     |       |       |  |
| 8  | - 43596 | 35878 | 89017 | 8100  |       |       |       |  |
| 9  | 75423   | 56809 | 07330 | 13    |       |       |       |  |
| 10 | - 69031 | 15874 | 41670 |       |       |       |       |  |
| 11 | 27790   | 37809 | 272   |       |       |       |       |  |
| 12 | 27706   | 37038 | 9     |       |       |       |       |  |
| 13 | - 70328 | 1827  |       |       |       |       |       |  |
| 14 | 79691   | 21    |       |       |       |       |       |  |
| 15 | - 51560 |       |       |       |       |       |       |  |
| 16 | - 7     |       |       |       |       |       |       |  |
| 17 | 5       |       |       |       |       |       |       |  |

S = 70

| I  | D SUB I |       |       |       |       |       |       |  |
|----|---------|-------|-------|-------|-------|-------|-------|--|
| 0  | 49645   | 45618 | 99762 | 02944 | 92641 | 67416 | 34942 |  |
| 1  | 70439   | 61687 | 66075 | 98029 | 25281 | 36674 | 498   |  |
| 2  | - 49601 | 48623 | 15802 | 45403 | 62728 | 43923 | 7     |  |
| 3  | 91954   | 65396 | 04803 | 80746 | 49586 | 65    |       |  |
| 4  | 47576   | 09663 | 00779 | 01682 | 52778 | 88    |       |  |
| 5  | - 69252 | 48317 | 43018 | 16555 | 45476 |       |       |  |
| 6  | 53212   | 68153 | 54428 | 88249 | 820   |       |       |  |
| 7  | - 91379 | 70021 | 74880 | 73075 |       |       |       |  |
| 8  | - 39053 | 64705 | 27594 | 1398  |       |       |       |  |
| 9  | 66429   | 83096 | 49653 | 15    |       |       |       |  |
| 10 | - 59774 | 59761 | 24495 |       |       |       |       |  |
| 11 | 23475   | 26439 | 757   |       |       |       |       |  |
| 12 | 23725   | 36896 | 1     |       |       |       |       |  |
| 13 | - 58700 | 0837  |       |       |       |       |       |  |
| 14 | 65238   | 96    |       |       |       |       |       |  |
| 15 | - 41225 |       |       |       |       |       |       |  |
| 16 | - 12    |       |       |       |       |       |       |  |
| 17 | 4       |       |       |       |       |       |       |  |



APPENDIX B  
VALUES OF  $\Pi_{s+1}(s)$

TABLE 4— $\Pi_{s+1}(s)$  TO 33 DECIMAL PLACES FOR  $s = 1(1)70$

| $s$ |    | $\Pi_{s+1}(s)$ |       |       |       |       |       |     |
|-----|----|----------------|-------|-------|-------|-------|-------|-----|
| 1   | 0. | 18927          | 51878 | 82093 | 32118 | 03671 | 35892 | 330 |
| 2   | 0. | 28121          | 25252 | 33780 | 21211 | 01257 | 13387 | 264 |
| 3   | 0. | 33107          | 18207 | 57297 | 57403 | 96445 | 04243 | 578 |
| 4   | 0. | 36234          | 77109 | 30150 | 41806 | 24897 | 98150 | 113 |
| 5   | 0. | 38381          | 35230 | 66598 | 99050 | 60316 | 80043 | 921 |
| 6   | 0. | 39946          | 78498 | 64246 | 19181 | 32889 | 13640 | 946 |
| 7   | 0. | 41139          | 37882 | 53067 | 68776 | 44516 | 94770 | 425 |
| 8   | 0. | 42078          | 39223 | 27607 | 49424 | 80917 | 28837 | 913 |
| 9   | 0. | 42837          | 06049 | 14723 | 28266 | 78893 | 32891 | 149 |
| 10  | 0. | 43462          | 86186 | 56620 | 59289 | 61348 | 53475 | 084 |
| 11  | 0. | 43987          | 93542 | 19413 | 10305 | 58450 | 13253 | 220 |
| 12  | 0. | 44434          | 81780 | 57968 | 30769 | 29839 | 53993 | 445 |
| 13  | 0. | 44819          | 78298 | 88886 | 96046 | 33589 | 61570 | 798 |
| 14  | 0. | 45154          | 87794 | 63734 | 23189 | 51342 | 86097 | 413 |
| 15  | 0. | 45449          | 21231 | 00126 | 13265 | 38379 | 62923 | 535 |
| 16  | 0. | 45709          | 80274 | 88442 | 11242 | 59120 | 41783 | 262 |
| 17  | 0. | 45942          | 14175 | 81479 | 01975 | 16278 | 75007 | 598 |
| 18  | 0. | 46150          | 59042 | 79618 | 29366 | 20249 | 99240 | 751 |
| 19  | 0. | 46338          | 65565 | 13054 | 01880 | 86880 | 44928 | 381 |
| 20  | 0. | 46509          | 18960 | 03773 | 84625 | 06853 | 99018 | 443 |
| 21  | 0. | 46664          | 53577 | 45605 | 86994 | 12593 | 13404 | 848 |
| 22  | 0. | 46806          | 63760 | 81585 | 38061 | 44761 | 73415 | 886 |
| 23  | 0. | 46937          | 12038 | 05492 | 33636 | 76180 | 48188 | 668 |
| 24  | 0. | 47057          | 35378 | 63878 | 17896 | 97589 | 84742 | 077 |
| 25  | 0. | 47168          | 50029 | 32419 | 66515 | 27559 | 25603 | 593 |
| 26  | 0. | 47271          | 55291 | 67563 | 97837 | 78613 | 41673 | 717 |
| 27  | 0. | 47367          | 36502 | 08385 | 52941 | 09116 | 90768 | 922 |
| 28  | 0. | 47456          | 67404 | 08816 | 47666 | 49270 | 58888 | 022 |
| 29  | 0. | 47540          | 12052 | 86421 | 56212 | 83451 | 19715 | 499 |
| 30  | 0. | 47618          | 26356 | 11387 | 92503 | 91055 | 99968 | 335 |
| 31  | 0. | 47691          | 59329 | 86460 | 13692 | 67473 | 83086 | 414 |
| 32  | 0. | 47760          | 54128 | 88845 | 91697 | 19203 | 46973 | 181 |
| 33  | 0. | 47825          | 48897 | 57110 | 72096 | 24500 | 39044 | 602 |
| 34  | 0. | 47886          | 77476 | 70871 | 43722 | 72844 | 01478 | 426 |
| 35  | 0. | 47944          | 69993 | 91774 | 07261 | 54744 | 48704 | 332 |
| 36  | 0. | 47999          | 53359 | 42388 | 34689 | 01441 | 77717 | 049 |
| 37  | 0. | 48051          | 51684 | 46461 | 18660 | 77452 | 11110 | 868 |
| 38  | 0. | 48100          | 86636 | 04256 | 21229 | 19929 | 37206 | 665 |
| 39  | 0. | 48147          | 77739 | 04861 | 66515 | 10377 | 15802 | 150 |
| 40  | 0. | 48192          | 42634 | 64571 | 57171 | 69157 | 55298 | 186 |
| 41  | 0. | 48234          | 97302 | 12808 | 35693 | 09826 | 06139 | 781 |
| 42  | 0. | 48275          | 56250 | 14162 | 47536 | 06970 | 47051 | 474 |
| 43  | 0. | 48314          | 32682 | 09154 | 01245 | 76918 | 66207 | 700 |
| 44  | 0. | 48351          | 38639 | 71345 | 30964 | 37588 | 33777 | 672 |
| 45  | 0. | 48386          | 85128 | 09929 | 90637 | 21073 | 71037 | 023 |
| 46  | 0. | 48420          | 82224 | 91418 | 05908 | 29144 | 30722 | 574 |
| 47  | 0. | 48453          | 39176 | 08848 | 49191 | 41823 | 57802 | 075 |
| 48  | 0. | 48484          | 64479 | 89993 | 03458 | 33150 | 62033 | 238 |
| 49  | 0. | 48514          | 65961 | 05653 | 84964 | 75672 | 58702 | 252 |
| 50  | 0. | 48543          | 50836 | 14099 | 49566 | 43636 | 27540 | 305 |
| 51  | 0. | 48571          | 25771 | 56932 | 67823 | 84126 | 40001 | 115 |
| 52  | 0. | 48597          | 96936 | 04424 | 43113 | 64502 | 70622 | 856 |
| 53  | 0. | 48623          | 70041 | 33944 | 51798 | 55257 | 61952 | 156 |
| 54  | 0. | 48648          | 50393 | 13051 | 35804 | 28421 | 57737 | 357 |
| 55  | 0. | 48672          | 42917 | 48662 | 39469 | 63201 | 53719 | 355 |
| 56  | 0. | 48695          | 52198 | 55172 | 54534 | 96512 | 06715 | 972 |
| 57  | 0. | 48717          | 82506 | 87152 | 26328 | 15260 | 09357 | 575 |
| 58  | 0. | 48739          | 37825 | 76116 | 20313 | 32358 | 32871 | 349 |
| 59  | 0. | 48760          | 21875 | 05627 | 24450 | 43893 | 17073 | 235 |
| 60  | 0. | 48780          | 38132 | 54539 | 88146 | 12991 | 70518 | 604 |
| 61  | 0. | 48799          | 89853 | 34369 | 13594 | 81214 | 77751 | 465 |
| 62  | 0. | 48818          | 80087 | 43494 | 86428 | 50419 | 24013 | 489 |
| 63  | 0. | 48837          | 11695 | 58092 | 56101 | 60483 | 27847 | 218 |
| 64  | 0. | 48854          | 87363 | 77250 | 61249 | 67474 | 94690 | 823 |
| 65  | 0. | 48872          | 09616 | 37632 | 07763 | 94802 | 14219 | 180 |
| 66  | 0. | 48888          | 80828 | 11217 | 65400 | 90200 | 98587 | 768 |
| 67  | 0. | 48905          | 03234 | 98084 | 54943 | 44213 | 32187 | 075 |
| 68  | 0. | 48920          | 78944 | 24799 | 03848 | 79708 | 25702 | 805 |
| 69  | 0. | 48936          | 09943 | 57799 | 44042 | 33997 | 18441 | 727 |
| 70  | 0. | 48950          | 98109 | 40096 | 49161 | 53941 | 71702 | 657 |

APPENDIX C

VALUES OF  $\Omega_s(s)$  AND OF  $\Omega_{s+1}(s)$

TABLE 5— $\Omega_s(s)$  TO 33 DECIMAL PLACES FOR  $s = 1(1)70$

| $s$ |    | $\Omega_s(s)$ |       |       |       |       |       |     |  |
|-----|----|---------------|-------|-------|-------|-------|-------|-----|--|
| 1   | 0. | 37855         | 03757 | 64186 | 64236 | 07342 | 71784 | 661 |  |
| 2   | 0. | 42181         | 87878 | 50670 | 31816 | 51885 | 70080 | 896 |  |
| 3   | 0. | 44142         | 90943 | 43063 | 43205 | 28593 | 38991 | 437 |  |
| 4   | 0. | 45293         | 46386 | 62688 | 02257 | 81122 | 47687 | 641 |  |
| 5   | 0. | 46057         | 62276 | 79918 | 78860 | 72380 | 16052 | 705 |  |
| 6   | 0. | 46604         | 58248 | 41620 | 55711 | 55037 | 32581 | 103 |  |
| 7   | 0. | 47016         | 43294 | 32077 | 35744 | 50876 | 51166 | 200 |  |
| 8   | 0. | 47338         | 19126 | 18558 | 43102 | 91031 | 94942 | 652 |  |
| 9   | 0. | 47596         | 73387 | 94136 | 98074 | 20992 | 58767 | 943 |  |
| 10  | 0. | 47809         | 14805 | 22282 | 65218 | 57483 | 38822 | 593 |  |
| 11  | 0. | 47986         | 83864 | 21177 | 93060 | 63763 | 78094 | 421 |  |
| 12  | 0. | 48137         | 71928 | 96132 | 33333 | 40659 | 50159 | 566 |  |
| 13  | 0. | 48267         | 45860 | 34185 | 95742 | 20788 | 81691 | 629 |  |
| 14  | 0. | 48380         | 22637 | 11143 | 81988 | 76438 | 77961 | 514 |  |
| 15  | 0. | 48479         | 15979 | 73467 | 87483 | 07604 | 93785 | 104 |  |
| 16  | 0. | 48566         | 66542 | 06469 | 74445 | 25315 | 44394 | 716 |  |
| 17  | 0. | 48644         | 62068 | 50977 | 78561 | 93706 | 91184 | 515 |  |
| 18  | 0. | 48714         | 51211 | 84041 | 53219 | 88041 | 65865 | 237 |  |
| 19  | 0. | 48777         | 53226 | 45320 | 01979 | 86168 | 89398 | 296 |  |
| 20  | 0. | 48834         | 64908 | 03962 | 53856 | 32196 | 68969 | 365 |  |
| 21  | 0. | 48886         | 65652 | 57301 | 38755 | 75097 | 56900 | 317 |  |
| 22  | 0. | 48934         | 21204 | 48930 | 17064 | 24069 | 08571 | 154 |  |
| 23  | 0. | 48977         | 86474 | 49209 | 39447 | 05579 | 63327 | 306 |  |
| 24  | 0. | 49018         | 07686 | 08206 | 43642 | 68322 | 75772 | 997 |  |
| 25  | 0. | 49055         | 24030 | 49716 | 45175 | 88661 | 62627 | 736 |  |
| 26  | 0. | 49089         | 68956 | 74008 | 74677 | 70098 | 54815 | 013 |  |
| 27  | 0. | 49121         | 71187 | 34622 | 03050 | 02047 | 16352 | 957 |  |
| 28  | 0. | 49151         | 55525 | 66274 | 20797 | 43887 | 39562 | 594 |  |
| 29  | 0. | 49179         | 43502 | 96298 | 16771 | 89777 | 10050 | 517 |  |
| 30  | 0. | 49205         | 53901 | 31767 | 52254 | 04091 | 19967 | 279 |  |
| 31  | 0. | 49230         | 03179 | 21507 | 23811 | 79327 | 82540 | 814 |  |
| 32  | 0. | 49253         | 05820 | 41622 | 35187 | 72928 | 57816 | 093 |  |
| 33  | 0. | 49274         | 74621 | 73992 | 86402 | 19182 | 22045 | 953 |  |
| 34  | 0. | 49295         | 20931 | 90602 | 95008 | 69104 | 13286 | 615 |  |
| 35  | 0. | 49314         | 54850 | 88681 | 90326 | 16308 | 61524 | 456 |  |
| 36  | 0. | 49332         | 85397 | 18565 | 80097 | 04259 | 60431 | 411 |  |
| 37  | 0. | 49350         | 20648 | 90960 | 13759 | 71437 | 30330 | 081 |  |
| 38  | 0. | 49366         | 67863 | 30684 | 00735 | 23085 | 40817 | 367 |  |
| 39  | 0. | 49382         | 33578 | 51140 | 16938 | 56797 | 08515 | 026 |  |
| 40  | 0. | 49397         | 23700 | 51185 | 86100 | 98386 | 49180 | 640 |  |
| 41  | 0. | 49411         | 43577 | 78974 | 41441 | 71041 | 33118 | 800 |  |
| 42  | 0. | 49424         | 98065 | 62118 | 72477 | 40469 | 76743 | 176 |  |
| 43  | 0. | 49437         | 91581 | 67506 | 43135 | 20567 | 93328 | 810 |  |
| 44  | 0. | 49450         | 28154 | 25239 | 52122 | 65715 | 34545 | 346 |  |
| 45  | 0. | 49462         | 11464 | 27928 | 34873 | 59319 | 79282 | 291 |  |
| 46  | 0. | 49473         | 44881 | 97753 | 23428 | 03690 | 92260 | 021 |  |
| 47  | 0. | 49484         | 31498 | 98398 | 45982 | 72500 | 67542 | 544 |  |
| 48  | 0. | 49494         | 74156 | 56451 | 22280 | 38007 | 92492 | 263 |  |
| 49  | 0. | 49504         | 75470 | 46585 | 56086 | 48645 | 49696 | 176 |  |
| 50  | 0. | 49514         | 37852 | 86381 | 48557 | 76509 | 00091 | 111 |  |
| 51  | 0. | 49523         | 63531 | 79617 | 63271 | 36756 | 32942 | 313 |  |
| 52  | 0. | 49532         | 54568 | 41047 | 97788 | 90743 | 14288 | 680 |  |
| 53  | 0. | 49541         | 12872 | 30811 | 39568 | 33658 | 70668 | 234 |  |
| 54  | 0. | 49549         | 40215 | 22552 | 30911 | 77096 | 05102 | 864 |  |
| 55  | 0. | 49557         | 38243 | 25910 | 80187 | 26168 | 83786 | 980 |  |
| 56  | 0. | 49565         | 08487 | 81157 | 76937 | 37521 | 21121 | 614 |  |
| 57  | 0. | 49572         | 52375 | 41312 | 82930 | 40089 | 21802 | 445 |  |
| 58  | 0. | 49579         | 71236 | 55014 | 75835 | 96709 | 33438 | 096 |  |
| 59  | 0. | 49586         | 66313 | 61654 | 82491 | 97179 | 49566 | 001 |  |
| 60  | 0. | 49593         | 38768 | 08782 | 21281 | 89874 | 90027 | 247 |  |
| 61  | 0. | 49599         | 89687 | 00506 | 33489 | 80906 | 82304 | 768 |  |
| 62  | 0. | 49606         | 20088 | 84518 | 97499 | 93167 | 93755 | 642 |  |
| 63  | 0. | 49612         | 30928 | 84411 | 49055 | 59856 | 02892 | 412 |  |
| 64  | 0. | 49618         | 23103 | 83145 | 15331 | 70091 | 74295 | 367 |  |
| 65  | 0. | 49623         | 97456 | 62826 | 41729 | 54722 | 17514 | 860 |  |
| 66  | 0. | 49629         | 54780 | 05327 | 01240 | 30961 | 60687 | 583 |  |
| 67  | 0. | 49634         | 95820 | 57757 | 45315 | 73231 | 43115 | 241 |  |
| 68  | 0. | 49640         | 21281 | 66340 | 20081 | 86762 | 79021 | 964 |  |
| 69  | 0. | 49645         | 31826 | 81825 | 51927 | 01156 | 56390 | 158 |  |
| 70  | 0. | 49650         | 28082 | 39240 | 72720 | 98998 | 02726 | 981 |  |

TABLE 6— $\Omega_{s+1}(s)$  TO 33 DECIMAL PLACES FOR  $s = 1(1)70$

| $s$ | $\Omega_{s+1}(s)$ |       |       |       |       |       |       |     |
|-----|-------------------|-------|-------|-------|-------|-------|-------|-----|
| 1   | 0.                | 32831 | 10192 | 21786 | 48358 | 37319 | 54362 | 913 |
| 2   | 0.                | 39738 | 93029 | 17823 | 59171 | 37773 | 62032 | 204 |
| 3   | 0.                | 42711 | 79017 | 89185 | 94444 | 23749 | 80529 | 562 |
| 4   | 0.                | 44356 | 03447 | 62812 | 42491 | 94003 | 53226 | 658 |
| 5   | 0.                | 45396 | 91176 | 62568 | 92727 | 14273 | 16197 | 742 |
| 6   | 0.                | 46114 | 21975 | 29594 | 40596 | 77057 | 54494 | 642 |
| 7   | 0.                | 46638 | 26028 | 20938 | 97302 | 64716 | 89538 | 318 |
| 8   | 0.                | 47037 | 76779 | 37254 | 64596 | 68230 | 10259 | 464 |
| 9   | 0.                | 47352 | 38104 | 17725 | 26505 | 91914 | 30579 | 098 |
| 10  | 0.                | 47606 | 54704 | 32718 | 39072 | 35206 | 81971 | 967 |
| 11  | 0.                | 47816 | 15542 | 66257 | 33622 | 68550 | 47858 | 570 |
| 12  | 0.                | 47991 | 97838 | 99778 | 75677 | 39533 | 25193 | 061 |
| 13  | 0.                | 48141 | 57601 | 88702 | 04263 | 53453 | 74255 | 921 |
| 14  | 0.                | 48270 | 40988 | 18879 | 67510 | 22116 | 68149 | 137 |
| 15  | 0.                | 48382 | 52363 | 17696 | 21425 | 52780 | 75400 | 410 |
| 16  | 0.                | 48480 | 97497 | 48567 | 96695 | 72051 | 55266 | 815 |
| 17  | 0.                | 48568 | 11884 | 61598 | 61337 | 60970 | 23942 | 948 |
| 18  | 0.                | 48645 | 79831 | 62151 | 87526 | 27651 | 45107 | 715 |
| 19  | 0.                | 48715 | 47648 | 67813 | 90737 | 27925 | 33725 | 369 |
| 20  | 0.                | 48778 | 32960 | 81883 | 39373 | 94471 | 81255 | 988 |
| 21  | 0.                | 48835 | 31409 | 54568 | 45518 | 24475 | 97789 | 256 |
| 22  | 0.                | 48887 | 21559 | 64247 | 75745 | 90204 | 92394 | 972 |
| 23  | 0.                | 48934 | 68547 | 93890 | 03658 | 31230 | 64982 | 933 |
| 24  | 0.                | 48978 | 26834 | 87328 | 34563 | 29097 | 11182 | 629 |
| 25  | 0.                | 49018 | 42306 | 08563 | 70352 | 82098 | 99452 | 995 |
| 26  | 0.                | 49055 | 53896 | 37119 | 69437 | 60377 | 61411 | 059 |
| 27  | 0.                | 49089 | 94858 | 01689 | 61942 | 34674 | 53109 | 878 |
| 28  | 0.                | 49121 | 93761 | 17374 | 74425 | 79896 | 15554 | 971 |
| 29  | 0.                | 49151 | 75290 | 06798 | 06106 | 12844 | 47716 | 575 |
| 30  | 0.                | 49179 | 60882 | 06366 | 87736 | 55472 | 52924 | 354 |
| 31  | 0.                | 49205 | 69244 | 61157 | 17741 | 11496 | 69960 | 855 |
| 32  | 0.                | 49230 | 16776 | 46804 | 27948 | 89554 | 88599 | 744 |
| 33  | 0.                | 49253 | 17913 | 24803 | 62862 | 09409 | 95666 | 890 |
| 34  | 0.                | 49274 | 85412 | 70992 | 70905 | 02705 | 54366 | 353 |
| 35  | 0.                | 49295 | 30591 | 68992 | 70905 | 58356 | 67401 | 450 |
| 36  | 0.                | 49314 | 63523 | 98443 | 03347 | 27528 | 98496 | 349 |
| 37  | 0.                | 49332 | 93206 | 48955 | 26040 | 96156 | 42492 | 751 |
| 38  | 0.                | 49350 | 27699 | 38428 | 55100 | 64882 | 19083 | 261 |
| 39  | 0.                | 49366 | 74244 | 96872 | 21036 | 93523 | 38290 | 892 |
| 40  | 0.                | 49382 | 39368 | 85561 | 54508 | 07946 | 70446 | 855 |
| 41  | 0.                | 49397 | 28966 | 49887 | 03116 | 11072 | 92890 | 680 |
| 42  | 0.                | 49411 | 48377 | 47961 | 33755 | 55871 | 64881 | 566 |
| 43  | 0.                | 49425 | 02449 | 52428 | 13591 | 46869 | 04019 | 808 |
| 44  | 0.                | 49437 | 95593 | 87341 | 19908 | 97062 | 43581 | 998 |
| 45  | 0.                | 49450 | 31833 | 33459 | 57188 | 72082 | 61111 | 928 |
| 46  | 0.                | 49462 | 14844 | 12314 | 50249 | 51050 | 82129 | 201 |
| 47  | 0.                | 49473 | 47992 | 40779 | 05586 | 33237 | 32255 | 050 |
| 48  | 0.                | 49484 | 34366 | 32709 | 91039 | 09811 | 96977 | 456 |
| 49  | 0.                | 49494 | 76804 | 11831 | 64677 | 15976 | 70341 | 108 |
| 50  | 0.                | 49504 | 77918 | 89848 | 78624 | 28509 | 93969 | 865 |
| 51  | 0.                | 49514 | 40120 | 55369 | 14106 | 29085 | 31045 | 161 |
| 52  | 0.                | 49523 | 65635 | 12263 | 35656 | 31244 | 40110 | 418 |
| 53  | 0.                | 49532 | 56522 | 00299 | 61828 | 56071 | 48920 | 330 |
| 54  | 0.                | 49541 | 14689 | 26063 | 78186 | 73822 | 19095 | 414 |
| 55  | 0.                | 49549 | 41907 | 28130 | 87808 | 39973 | 69108 | 309 |
| 56  | 0.                | 49557 | 39820 | 97054 | 97091 | 38923 | 39963 | 872 |
| 57  | 0.                | 49565 | 09960 | 67878 | 27659 | 55209 | 06642 | 780 |
| 58  | 0.                | 49572 | 53752 | 00436 | 03711 | 44190 | 12277 | 687 |
| 59  | 0.                | 49579 | 72524 | 60676 | 53144 | 48415 | 79140 | 247 |
| 60  | 0.                | 49586 | 67520 | 14464 | 99217 | 11238 | 28968 | 917 |
| 61  | 0.                | 49593 | 39899 | 43846 | 15819 | 65099 | 26178 | 188 |
| 62  | 0.                | 49599 | 90748 | 94461 | 61971 | 05846 | 51392 | 283 |
| 63  | 0.                | 49606 | 21086 | 61721 | 01673 | 95654 | 60572 | 847 |
| 64  | 0.                | 49612 | 31867 | 22382 | 35917 | 07268 | 87640 | 302 |
| 65  | 0.                | 49618 | 23987 | 17382 | 80521 | 29046 | 46161 | 145 |
| 66  | 0.                | 49623 | 98288 | 91057 | 61076 | 25702 | 62884 | 651 |
| 67  | 0                 | 49629 | 55564 | 91275 | 27955 | 45020 | 86465 | 902 |
| 68  | 0                 | 49634 | 96561 | 34487 | 47036 | 68843 | 39642 | 663 |
| 69  | 0.                | 49640 | 21981 | 39231 | 39658 | 49052 | 77533 | 691 |
| 70  | 0.                | 49645 | 32488 | 31220 | 53434 | 57958 | 91279 | 656 |

**APPENDIX D**  
**VALUES OF THE SINE AND COSINE INTEGRALS**

TABLE 7— $si(x)$  TO 33 DECIMAL PLACES FOR  $x = 1(1)70$

| $x$ |     | $si(x)$ |       |       |       |       |     |
|-----|-----|---------|-------|-------|-------|-------|-----|
| 1   | -0. | 62471   | 32564 | 27713 | 60428 | 99683 | 778 |
| 2   | 0.  | 03461   | 66500 | 07798 | 22934 | 53984 | 566 |
| 3   | 0.  | 27785   | 62012 | 04571 | 63716 | 64085 | 595 |
| 4   | 0.  | 18740   | 68121 | 54156 | 43887 | 42376 | 117 |
| 5   | -0. | 02086   | 50818 | 50222 | 48195 | 69132 | 909 |
| 6   | -0. | 14610   | 87755 | 14390 | 08346 | 22906 | 637 |
| 7   | -0. | 11619   | 97125 | 46803 | 02861 | 65531 | 978 |
| 8   | 0.  | 00339   | 04949 | 12045 | 43285 | 16497 | 596 |
| 9   | 0.  | 09424   | 37490 | 34705 | 87587 | 53317 | 363 |
| 10  | 0.  | 08755   | 12674 | 23977 | 43009 | 96501 | 877 |
| 11  | 0.  | 00751   | 04801 | 50830 | 79648 | 79540 | 535 |
| 12  | -0. | 06582   | 50852 | 68523 | 24870 | 41731 | 595 |
| 13  | -0. | 07143   | 46039 | 32072 | 05500 | 37149 | 094 |
| 14  | -0. | 01458   | 52767 | 17231 | 56552 | 76897 | 988 |
| 15  | 0.  | 04739   | 81169 | 13472 | 11989 | 26669 | 398 |
| 16  | 0.  | 06050   | 59414 | 75136 | 26691 | 52816 | 252 |
| 17  | 0.  | 01934   | 00890 | 75804 | 50320 | 25257 | 183 |
| 18  | -0. | 03418   | 82299 | 33711 | 15687 | 01477 | 978 |
| 19  | -0. | 05216   | 62950 | 25532 | 68765 | 96871 | 414 |
| 20  | -0. | 02255   | 46257 | 51456 | 77906 | 76783 | 495 |
| 21  | 0.  | 02409   | 46412 | 74762 | 70221 | 22667 | 843 |
| 22  | 0.  | 04528   | 74097 | 99469 | 92388 | 31093 | 355 |
| 23  | 0.  | 02466   | 31055 | 18260 | 21956 | 78927 | 114 |
| 24  | -0. | 01605   | 76350 | 71977 | 51917 | 32659 | 077 |
| 25  | -0. | 03931   | 37757 | 94935 | 29660 | 01384 | 986 |
| 26  | -0. | 02592   | 74638 | 08558 | 06134 | 35844 | 313 |
| 27  | 0.  | 00948   | 93571 | 73776 | 11125 | 41737 | 632 |
| 28  | 0.  | 03394   | 94114 | 95475 | 33348 | 92680 | 551 |
| 29  | 0.  | 02651   | 81882 | 49224 | 38162 | 86729 | 478 |
| 30  | -0. | 00403   | 97867 | 64545 | 50824 | 75903 | 827 |
| 31  | -0. | 02902   | 92895 | 01107 | 14690 | 72349 | 174 |
| 32  | -0. | 02655   | 45497 | 35755 | 10385 | 70639 | 013 |
| 33  | -0. | 00051   | 16286 | 26210 | 71451 | 80734 | 751 |
| 34  | 0.  | 02445   | 98583 | 87572 | 00573 | 57929 | 860 |
| 35  | 0.  | 02612   | 58777 | 13409 | 00612 | 20695 | 532 |
| 36  | 0.  | 00431   | 08827 | 61880 | 38152 | 63169 | 366 |
| 37  | -0. | 02018   | 88557 | 69319 | 97574 | 66044 | 853 |
| 38  | -0. | 02530   | 33895 | 59197 | 87866 | 94305 | 609 |
| 39  | -0. | 00745   | 92690 | 98525 | 96467 | 75278 | 911 |
| 40  | 0.  | 01618   | 87925 | 59887 | 88754 | 43442 | 704 |
| 41  | 0.  | 02414   | 70246 | 47298 | 39350 | 70721 | 373 |
| 42  | 0.  | 01003   | 05569 | 20119 | 62773 | 59211 | 237 |
| 43  | -0. | 01244   | 73301 | 65561 | 89987 | 20906 | 100 |
| 44  | -0. | 02270   | 94954 | 70314 | 79949 | 57945 | 025 |
| 45  | -0. | 01208   | 13258 | 98483 | 77281 | 29753 | 503 |
| 46  | 0.  | 00896   | 13635 | 21708 | 92742 | 99872 | 906 |
| 47  | 0.  | 02103   | 87170 | 20935 | 61391 | 13018 | 596 |
| 48  | 0.  | 01365   | 74061 | 74167 | 95711 | 79077 | 921 |
| 49  | -0. | 00573   | 32100 | 58625 | 46653 | 53640 | 049 |
| 50  | -0. | 01917   | 92543 | 08960 | 72450 | 33360 | 968 |
| 51  | -0. | 01479   | 79959 | 62744 | 98483 | 90623 | 664 |
| 52  | 0.  | 00276   | 80565 | 70212 | 01420 | 85714 | 223 |
| 53  | 0.  | 01717   | 31564 | 90128 | 80314 | 66984 | 921 |
| 54  | 0.  | 01553   | 83360 | 67068 | 46608 | 93399 | 618 |
| 55  | -0. | 00007   | 21933 | 96744 | 84196 | 44242 | 888 |
| 56  | -0. | 01506   | 03985 | 88975 | 40875 | 74393 | 911 |
| 57  | -0. | 01591   | 14541 | 69725 | 34659 | 16171 | 650 |
| 58  | -0. | 00234   | 82357 | 00524 | 98962 | 89698 | 116 |
| 59  | 0.  | 01287   | 90685 | 01941 | 72474 | 33178 | 752 |
| 60  | 0.  | 01594   | 92894 | 65050 | 79309 | 51184 | 407 |
| 61  | 0.  | 00448   | 81302 | 69302 | 71332 | 67505 | 525 |
| 62  | -0. | 01066   | 53882 | 57229 | 90227 | 73770 | 974 |
| 63  | -0. | 01568   | 33923 | 47207 | 34735 | 87181 | 263 |
| 64  | -0. | 00634   | 40765 | 82866 | 08706 | 82213 | 305 |
| 65  | 0.  | 00845   | 36290 | 83705 | 75085 | 62118 | 791 |
| 66  | 0.  | 01514   | 53253 | 85134 | 29094 | 97632 | 313 |
| 67  | 0.  | 00791   | 48013 | 70666 | 04146 | 39882 | 175 |
| 68  | -0. | 00627   | 59615 | 01426 | 39967 | 09696 | 243 |
| 69  | -0. | 01436   | 68501 | 65808 | 57961 | 57054 | 532 |
| 70  | -0. | 00920   | 14776 | 16890 | 51370 | 83394 | 869 |

TABLE 8-- $Si(x)$  TO 33 DECIMAL PLACES FOR  $x = 1(1)70$

| $x$ |    | $Si(x)$ |       |       |       |       |     |  |
|-----|----|---------|-------|-------|-------|-------|-----|--|
| 1   | 0. | 94608   | 30703 | 67183 | 01494 | 13533 | 139 |  |
| 2   | 1. | 60641   | 29768 | 02694 | 84857 | 67201 | 482 |  |
| 3   | 1. | 84866   | 25279 | 99468 | 25639 | 77302 | 511 |  |
| 4   | 1. | 75820   | 31389 | 49053 | 06810 | 55593 | 033 |  |
| 5   | 1. | 54993   | 12449 | 44674 | 13727 | 44084 | 007 |  |
| 6   | 1. | 42468   | 75512 | 80506 | 53576 | 90310 | 279 |  |
| 7   | 1. | 45459   | 66142 | 48093 | 59061 | 47684 | 938 |  |
| 8   | 1. | 57418   | 68217 | 06942 | 05208 | 29714 | 512 |  |
| 9   | 1. | 66504   | 00758 | 29602 | 49510 | 66534 | 279 |  |
| 10  | 1. | 65834   | 75942 | 18874 | 04933 | 09718 | 794 |  |
| 11  | 1. | 57830   | 68069 | 45727 | 41571 | 92757 | 452 |  |
| 12  | 1. | 50497   | 12415 | 26373 | 37052 | 71485 | 321 |  |
| 13  | 1. | 49936   | 17228 | 62824 | 56422 | 76067 | 823 |  |
| 14  | 1. | 55621   | 10500 | 77665 | 05370 | 36318 | 928 |  |
| 15  | 1. | 61819   | 44437 | 08368 | 73912 | 39886 | 314 |  |
| 16  | 1. | 63130   | 22682 | 70032 | 88614 | 66033 | 169 |  |
| 17  | 1. | 59013   | 64158 | 70701 | 12243 | 38474 | 100 |  |
| 18  | 1. | 53660   | 80968 | 61185 | 46236 | 11738 | 939 |  |
| 19  | 1. | 51863   | 00317 | 69363 | 93157 | 16345 | 502 |  |
| 20  | 1. | 54824   | 17010 | 43439 | 84016 | 36433 | 422 |  |
| 21  | 1. | 59489   | 09680 | 69659 | 32144 | 35884 | 759 |  |
| 22  | 1. | 61608   | 37365 | 94366 | 54311 | 44310 | 272 |  |
| 23  | 1. | 59545   | 94323 | 13156 | 83879 | 92144 | 030 |  |
| 24  | 1. | 55473   | 86917 | 22919 | 10005 | 80557 | 839 |  |
| 25  | 1. | 53148   | 25509 | 99961 | 32263 | 11831 | 930 |  |
| 26  | 1. | 54486   | 88629 | 86338 | 55788 | 77372 | 603 |  |
| 27  | 1. | 58028   | 56839 | 68672 | 73048 | 54954 | 548 |  |
| 28  | 1. | 60474   | 57382 | 90371 | 95272 | 05897 | 467 |  |
| 29  | 1. | 59731   | 45150 | 44121 | 00085 | 99946 | 394 |  |
| 30  | 1. | 56675   | 65400 | 30351 | 11098 | 37313 | 090 |  |
| 31  | 1. | 54176   | 70372 | 93789 | 47232 | 40867 | 743 |  |
| 32  | 1. | 54424   | 17770 | 59141 | 51537 | 42577 | 904 |  |
| 33  | 1. | 57028   | 46981 | 68685 | 90471 | 32482 | 165 |  |
| 34  | 1. | 59525   | 61851 | 82468 | 62496 | 71146 | 776 |  |
| 35  | 1. | 59692   | 22045 | 08305 | 62535 | 33912 | 448 |  |
| 36  | 1. | 57510   | 72095 | 56777 | 00075 | 76386 | 282 |  |
| 37  | 1. | 55060   | 74710 | 25576 | 64348 | 47172 | 063 |  |
| 38  | 1. | 54549   | 29372 | 35698 | 74056 | 18911 | 308 |  |
| 39  | 1. | 56333   | 70576 | 96370 | 65455 | 37938 | 006 |  |
| 40  | 1. | 58698   | 51193 | 54784 | 50677 | 56659 | 620 |  |
| 41  | 1. | 59494   | 33514 | 42195 | 01273 | 83938 | 289 |  |
| 42  | 1. | 58082   | 68837 | 15016 | 24696 | 72428 | 153 |  |
| 43  | 1. | 55834   | 89966 | 29334 | 71935 | 92310 | 816 |  |
| 44  | 1. | 54808   | 68313 | 24581 | 81973 | 55271 | 892 |  |
| 45  | 1. | 55871   | 50008 | 96412 | 84641 | 83463 | 414 |  |
| 46  | 1. | 57975   | 76903 | 16605 | 54666 | 13089 | 822 |  |
| 47  | 1. | 59183   | 50438 | 15832 | 23314 | 26235 | 512 |  |
| 48  | 1. | 58445   | 37329 | 69064 | 57634 | 92294 | 838 |  |
| 49  | 1. | 56506   | 31167 | 36271 | 15269 | 59576 | 867 |  |
| 50  | 1. | 55161   | 70724 | 85935 | 89472 | 79855 | 949 |  |
| 51  | 1. | 55599   | 83308 | 32151 | 63439 | 22593 | 253 |  |
| 52  | 1. | 57356   | 43833 | 65108 | 63343 | 98931 | 139 |  |
| 53  | 1. | 58796   | 94832 | 85025 | 42237 | 80201 | 837 |  |
| 54  | 1. | 58633   | 46628 | 61965 | 08532 | 06616 | 534 |  |
| 55  | 1. | 57072   | 41333 | 98151 | 77726 | 68974 | 029 |  |
| 56  | 1. | 55573   | 59282 | 05921 | 21047 | 38823 | 005 |  |
| 57  | 1. | 55488   | 48726 | 25171 | 27263 | 97045 | 266 |  |
| 58  | 1. | 56844   | 80910 | 94371 | 62960 | 23518 | 800 |  |
| 59  | 1. | 58367   | 53952 | 96838 | 34397 | 46395 | 668 |  |
| 60  | 1. | 58674   | 56162 | 59947 | 41232 | 64401 | 323 |  |
| 61  | 1. | 57528   | 44570 | 64199 | 33255 | 80722 | 442 |  |
| 62  | 1. | 56013   | 09385 | 37666 | 71695 | 39445 | 942 |  |
| 63  | 1. | 55511   | 29344 | 47689 | 27187 | 26035 | 653 |  |
| 64  | 1. | 56445   | 22502 | 12030 | 53216 | 31003 | 611 |  |
| 65  | 1. | 57924   | 99558 | 78602 | 37008 | 75335 | 708 |  |
| 66  | 1. | 58594   | 16521 | 80030 | 91018 | 10849 | 229 |  |
| 67  | 1. | 57871   | 11281 | 65562 | 66069 | 53099 | 092 |  |
| 68  | 1. | 56452   | 03652 | 93470 | 21956 | 03520 | 674 |  |
| 69  | 1. | 55642   | 94766 | 29088 | 03961 | 56162 | 384 |  |
| 70  | 1. | 56159   | 48491 | 78006 | 10552 | 29822 | 047 |  |



TABLE 9— $Ci(x)$  TO 33 DECIMAL PLACES FOR  $x = 1(1)70$

| $x$ |     | $Ci(x)$ |       |       |       |       |     |  |
|-----|-----|---------|-------|-------|-------|-------|-----|--|
| 1   | 0.  | 33740   | 39229 | 00968 | 13466 | 26462 | 039 |  |
| 2   | 0.  | 42298   | 08287 | 74864 | 99569 | 85651 | 532 |  |
| 3   | 0.  | 11962   | 97860 | 08000 | 32762 | 64722 | 812 |  |
| 4   | -0. | 14098   | 16978 | 86930 | 41163 | 91448 | 987 |  |
| 5   | -0. | 19002   | 97496 | 56643 | 87861 | 84589 | 001 |  |
| 6   | -0. | 06805   | 72438 | 93247 | 12620 | 41683 | 048 |  |
| 7   | 0.  | 07669   | 52784 | 82184 | 51838 | 29157 | 630 |  |
| 8   | 0.  | 12243   | 38825 | 32009 | 55729 | 22959 | 583 |  |
| 9   | 0.  | 05534   | 75313 | 33133 | 60708 | 56416 | 484 |  |
| 10  | -0. | 04545   | 64330 | 04455 | 37263 | 45328 | 300 |  |
| 11  | -0. | 08956   | 31354 | 95479 | 97948 | 24676 | 305 |  |
| 12  | -0. | 04978   | 00068 | 84113 | 67559 | 59212 | 087 |  |
| 13  | 0.  | 02676   | 41255 | 64034 | 55503 | 67498 | 668 |  |
| 14  | 0.  | 06939   | 63559 | 27584 | 54727 | 43832 | 682 |  |
| 15  | 0.  | 04627   | 86776 | 74360 | 43960 | 43108 | 309 |  |
| 16  | -0. | 01420   | 01901 | 20190 | 02239 | 87727 | 863 |  |
| 17  | -0. | 05524   | 26822 | 60813 | 85052 | 73400 | 995 |  |
| 18  | -0. | 04347   | 51029 | 99501 | 00478 | 34411 | 492 |  |
| 19  | 0.  | 00515   | 03710 | 08426 | 12856 | 98550 | 925 |  |
| 20  | 0.  | 04441   | 98208 | 45353 | 31653 | 97687 | 170 |  |
| 21  | 0.  | 04089   | 05001 | 54692 | 36971 | 03028 | 992 |  |
| 22  | 0.  | 00164   | 06919 | 15737 | 74972 | 66809 | 806 |  |
| 23  | -0. | 03565   | 98603 | 82261 | 68292 | 95312 | 957 |  |
| 24  | -0. | 03833   | 30155 | 51247 | 14767 | 84692 | 866 |  |
| 25  | -0. | 00684   | 85971 | 79702 | 59091 | 89387 | 780 |  |
| 26  | 0.  | 02829   | 51510 | 31757 | 13190 | 84211 | 300 |  |
| 27  | 0.  | 03572   | 32177 | 17395 | 86892 | 52412 | 198 |  |
| 28  | 0.  | 01086   | 95343 | 08760 | 86639 | 85990 | 747 |  |
| 29  | -0. | 02194   | 69729 | 74023 | 04438 | 17170 | 542 |  |
| 30  | -0. | 03303   | 24172 | 82071 | 14377 | 92264 | 410 |  |
| 31  | -0. | 01395   | 27170 | 88765 | 38111 | 27878 | 536 |  |
| 32  | 0.  | 01638   | 88233 | 76158 | 67976 | 52215 | 894 |  |
| 33  | 0.  | 03025   | 74341 | 71747 | 31064 | 64190 | 945 |  |
| 34  | 0.  | 01626   | 49164 | 37355 | 76698 | 16563 | 519 |  |
| 35  | -0. | 01147   | 98563 | 55303 | 12949 | 95524 | 260 |  |
| 36  | -0. | 02740   | 89958 | 44977 | 44812 | 19314 | 772 |  |
| 37  | -0. | 01792   | 44197 | 10374 | 87873 | 38841 | 573 |  |
| 38  | 0.  | 00712   | 97618 | 01971 | 37971 | 35513 | 765 |  |
| 39  | 0.  | 02450   | 58334 | 17995 | 32807 | 86490 | 871 |  |
| 40  | 0.  | 01902   | 00078 | 96208 | 76696 | 19812 | 034 |  |
| 41  | -0. | 00327   | 89946 | 01272 | 07220 | 24609 | 597 |  |
| 42  | -0. | 02157   | 13793 | 86110 | 01039 | 32740 | 436 |  |
| 43  | -0. | 01962   | 20686 | 19766 | 02916 | 38534 | 024 |  |
| 44  | -0. | 00011   | 29602 | 15923 | 15149 | 71254 | 859 |  |
| 45  | 0.  | 01863   | 17437 | 03556 | 53210 | 28213 | 528 |  |
| 46  | 0.  | 01978   | 93378 | 69101 | 64954 | 65696 | 877 |  |
| 47  | 0.  | 00307   | 48622 | 02395 | 11907 | 40950 | 517 |  |
| 48  | -0. | 01571   | 43603 | 39703 | 32720 | 89430 | 021 |  |
| 49  | -0. | 01957   | 30908 | 02871 | 69756 | 81183 | 920 |  |
| 50  | -0. | 00562   | 83863 | 24116 | 30544 | 01858 | 955 |  |
| 51  | 0.  | 01284   | 70085 | 40631 | 13274 | 41575 | 407 |  |
| 52  | 0.  | 01901   | 97802 | 86359 | 47487 | 24315 | 938 |  |
| 53  | 0.  | 00779   | 12035 | 06269 | 68417 | 72858 | 007 |  |
| 54  | -0. | 01005   | 70583 | 27335 | 24933 | 98636 | 613 |  |
| 55  | -0. | 01817   | 26961 | 21802 | 92912 | 23331 | 524 |  |
| 56  | -0. | 00957   | 90490 | 58468 | 44996 | 70886 | 149 |  |
| 57  | 0.  | 00737   | 08611 | 60588 | 57036 | 19831 | 016 |  |
| 58  | 0.  | 01707   | 29871 | 71210 | 07125 | 73603 | 436 |  |
| 59  | 0.  | 01100   | 71216 | 77743 | 47251 | 35276 | 728 |  |
| 60  | -0. | 00481   | 32433 | 77443 | 21528 | 88723 | 439 |  |
| 61  | -0. | 01576   | 02584 | 39320 | 85240 | 81906 | 190 |  |
| 62  | -0. | 01209   | 10233 | 69152 | 33626 | 71637 | 466 |  |
| 63  | 0.  | 00240   | 70795 | 07390 | 65877 | 50053 | 950 |  |
| 64  | 0.  | 01427   | 28792 | 13325 | 48725 | 35777 | 047 |  |
| 65  | 0.  | 01284   | 73736 | 99511 | 79921 | 86448 | 815 |  |
| 66  | -0. | 00017   | 29331 | 94092 | 48378 | 73381 | 330 |  |
| 67  | -0. | 01264   | 80926 | 03150 | 42962 | 90900 | 197 |  |
| 68  | -0. | 01329   | 41857 | 91036 | 14117 | 61348 | 849 |  |
| 69  | -0. | 00187   | 12407 | 20841 | 47510 | 74718 | 745 |  |
| 70  | 0.  | 01092   | 19884 | 73464 | 97703 | 78113 | 544 |  |

## REFERENCES

1. "Tables of the Exponential Integral for Complex Arguments," National Bureau of Standards Applied Mathematics Series, 51, U.S. Government Printing Office, Washington, D.C. (1958).
2. "Handbook of Mathematical Functions With Formulas, Graphs, and Mathematical Tables," National Bureau of Standards Applied Mathematics Series, 55, U.S. Government Printing Office, Washington, D.C. (1964).
3. Murnaghan, F.D. and J.W. Wrench, Jr., "The Converging Factor for the Exponential Integral," David Taylor Model Basin Report 1535 (Jan 1963).
4. Bretschneider, C.A., "Berechnung der Grundzahl der natürlichen Logarithmen, so wie mehrerer anderer mit ihr zusammenhängender Zahlwerthe," Archiv der Mathematik und Physik, Vol. 3, pp. 27-34 (1843).
5. Glaisher, J.W.L., "Tables of the Numerical Values of the Sine-integral, Cosine-integral and Exponential Integral," Philosophical Transactions of the Royal Society of London, Vol. 160, pp. 367-388 (1870).
6. "Circular and Hyperbolic Functions, Exponential, Sine and Cosine Integrals, Factorial (Gamma) and Derived Functions, Integrals of Probability Integral," British Association for the Advancement of Science Mathematical Tables, Vol. I, Cambridge University Press, Cambridge, Third Edition (1951).

7. "Tables of Sine, Cosine and Exponential Integrals," National Bureau of Standards, U.S. Government Printing Office, Washington, D.C., (1940), 2 Vols.

8. "Table of Sine and Cosine Integrals for Arguments from 10 to 100," National Bureau of Standards Applied Mathematics Series, 32, U.S. Government Printing Office, Washington, D.C. (1954).

9. Fletcher, A., et al., "An Index of Mathematical Tables," Addison-Wesley Publishing Co., Reading, Massachusetts, Second Edition (1962).

10. Dingle, R.B., "Asymptotic Expansions and Converging Factors II. Error, Dawson, Fresnel, Exponential, Sine and Cosine, and Similar Integrals," Proceedings of the Royal Society of London, Ser. A, Vol. 244, pp. 476-483 (1958).

11. Dingle, R.B., "Asymptotic Expansions and Converging Factors I. General Theory and Basic Converging Factors," Proceedings of the Royal Society of London, Ser. A, Vol. 244, pp. 456-475 (1958).

12. Archibald, R.C., "Gibbs Constant", Mathematical Tables and other Aids to Computation, Vol. 2, pp. 195-196 (1946).

## INITIAL DISTRIBUTION

| Copies |  | Copies |   |
|--------|--|--------|---|
| 2      | U.S. Army Math Res Center<br>Univ of Wis, Madison<br>1 Prof J. B. Rosser<br>1 Tech Lib | 1      | NAVSHIPYD PEARL   |
|        |  | 1      | NAVSHIPYD PHILA   |
|        |  | 1      | NAVSHIPYD PTSMTH  |
| 2      | CHONR<br>1 Dr. L. D. Bram<br>1 Dr. R. J. Lundegard                                     | 1      | Wright-Patterson AFB<br>Aerospace Res Labs<br>Applied Math Lab<br>H. E. Fettis  |
| 1      | DNL  |        |   |
| 2      | USNA<br>1 Dept of Math<br>1 Tech Lib   | 12     | DDC   |
|        |  | 1      | AEC<br>Tech Lib   |
| 1      | NAVPGSCOL<br>Lib   | 3      | BUSTAND<br>1 Dr. F. W. J. Olver<br>1 Ms. I. A. Stegun<br>1 Tech Lib   |
| 1      | NROTC & NAVADMINU, MIT   |        |   |
| 1      | NAVWARCOL  | 1      | Argonne National Lab<br>Applied Math Div  |
| 1      | NRL<br>Tech Lib  | 1      | Harvard University<br>Computation Lab   |
| 1      | NOL<br>Tech Lib  | 3      | Kent State Univ<br>Prof R. S. Varga,<br>Dept of Math  |
| 3      | NWL<br>1 Dr. A. V. Hershey, KXH<br>1 Dr. A. R. DiDonato, KXD<br>1 Tech Lib             | 1      | Los Alamos Sci Lab<br>Tech Lib  |
| 1      | NAVSHIPYD BREM   | 1      | Univ of Maryland<br>1 Computation Lab<br>1 Prof J. L. Walsh<br>1 Prof B. S. Berger<br>1 Inst for Fluid Dynamics<br>& Applied Math |
| 1      | NAVSHIPYD BSN  |        |   |
| 1      | NAVSHIPYD CHASN  |        |   |
| 1      | NAVSHIPYD HUNTERS PT   |        |   |
| 1      | NAVSHIPYD MARE   |        |   |
| 1      | NAVSHIPYD NORVA  |        |   |

**Copies**

- 1 Univ of Missouri-Kansas City  
Prof Y. L. Luke
- 1 New York Univ  
Courant Inst of Math Sci
- 1 Univ of Notre Dame  
Computing Center  
Prof H. C. Thacher, Jr.
- 1 Penn State Univ  
Prof P. C. Hammer
- 1 Univ of Texas  
Prof D. M. Young, Jr.
- 1 Prof F. D. Murnaghan  
6202 Sycamore Road  
Baltimore, Maryland 21212

## CENTER DISTRIBUTION

### Copies:

|    |              |
|----|--------------|
| 1  | 18-1808-1809 |
| 1  | 1802.1       |
| 1  | 1802.2       |
| 1  | 1802.3       |
| 1  | 1802.4       |
| 1  | 1805         |
| 1  | 183          |
| 20 | 184          |
| 10 | 1842         |
| 1  | 1843         |
| 1  | 1844         |
| 1  | 185          |
| 1  | 186          |
| 1  | 188          |
| 1  | 189          |

UNCLASSIFIED

Security Classification

DOCUMENT CONTROL DATA - R & D

(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)

|  |   |  |  |
|--|---|--|--|
| 1 ORIGINATING ACTIVITY (Corporate author)<br><b>Naval Ship Research and Development Center<br/>Bethesda, Maryland 20034</b>  |   | 2a. REPORT SECURITY CLASSIFICATION<br><b>UNCLASSIFIED</b>            |  |
|  |   | 2b. GROUP  |  |
| 3 REPORT TITLE<br><b>The Converging Factors for the Sine and Cosine Integrals</b>  |   |  |  |
| 4 DESCRIPTIVE NOTES (Type of report and inclusive dates)<br><b>Final</b>   |   |  |  |
| 5 AUTHOR(S) (First name, middle initial, last name)<br><b>John W. Wrench, Jr.<br/>Vicki Alley</b>  |   |  |  |
| 6 REPORT DATE<br><b>September 1972</b>   | 7a. TOTAL NO. OF PAGES<br><b>105</b>  | 7b. NO. OF REFS<br><b>12</b>   |  |
| 8a. CONTRACT OR GRANT NO   | 9a. ORIGINATOR'S REPORT NUMBER(S)<br><b>3980</b>                            |  |  |
| b. PROJECT NO  |   |  |  |
| c. <b>SR 0140301 , Task 15324</b>  | 9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report) |  |  |
| d.   |   |  |  |
| 10 DISTRIBUTION STATEMENT<br><b>Approved for public release; distribution unlimited.</b>   |   |  |  |
| 11 SUPPLEMENTARY NOTES   |   | 12 SPONSORING MILITARY ACTIVITY<br><b>Naval Ship Systems Command</b> |  |
| 13 ABSTRACT<br><p>The theory of the converging factors for the sine and cosine integrals is developed and then applied to the calculation on a CDC 6700 system of tables of these factors and their reduced derivatives to about 35 decimal places. The factors are then used in conjunction with appropriately truncated asymptotic series to produce tables of <math>si(x)</math>, <math>Si(x)</math>, and <math>Ci(x)</math> to 28 decimals by a computer program, for successive integer values of <math>x</math> ranging from 1 to 70, inclusive. Interpolation in the tables by Taylor series is illustrated by numerical examples, which include a new, extended calculation of the Gibbs constant.</p> |   |  |  |

| 14<br>KEY WORDS  | LINK A |    | LINK B |    | LINK C |    |
|--|--------|----|--------|----|--------|----|
|  | ROLE   | WT | ROLE   | WT | ROLE   | WT |
| Sine and Cosine Integrals<br>Asymptotic Expansions<br>Converging Factors<br>Gibbs Constant |        |    |        |    |        |    |



MIT LIBRARIES

DUPL



3 9080 02753 7544

